

*The implications of  
non-ideal magnetohydrodynamics on  
star formation*

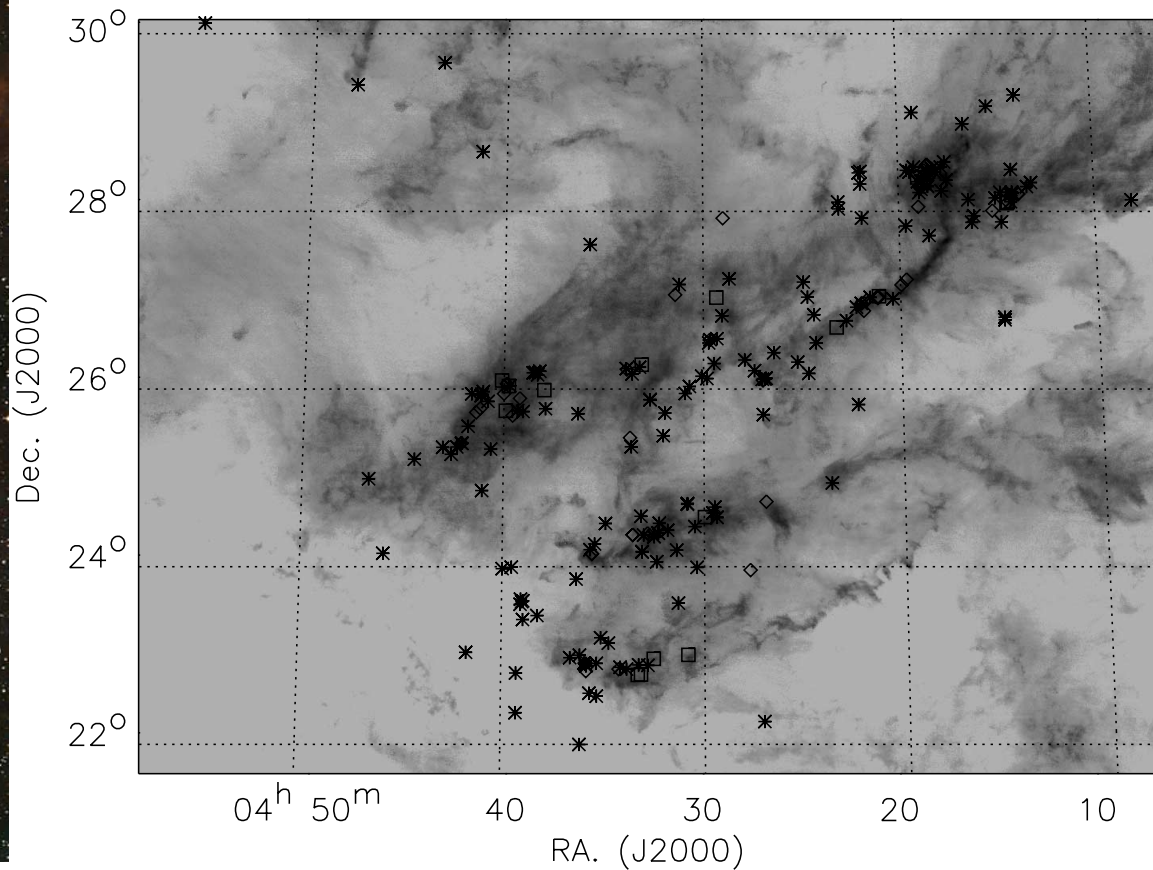
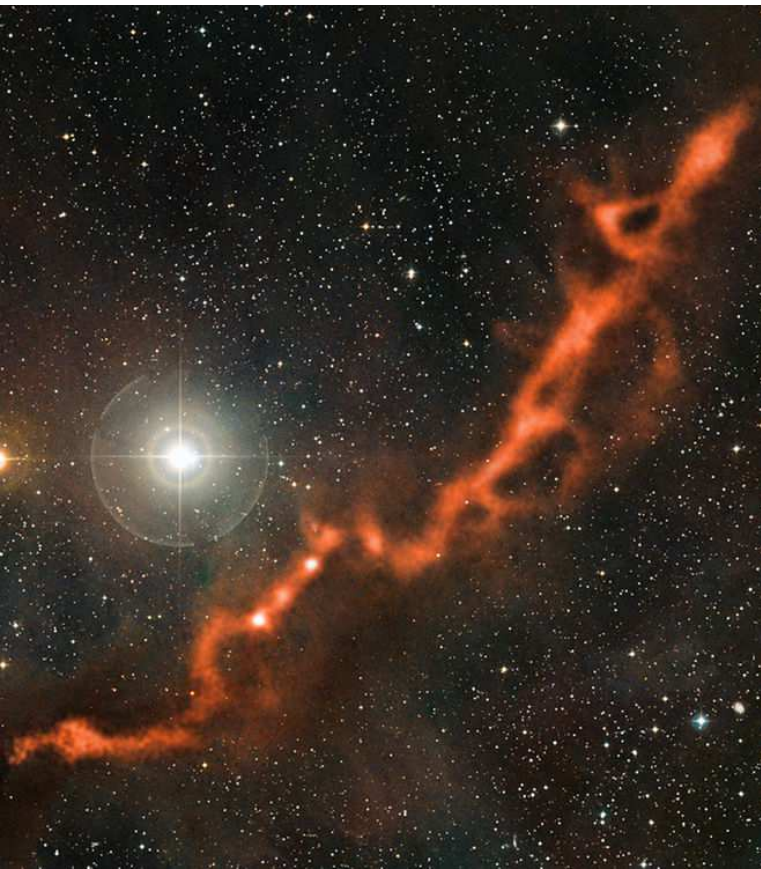
James Wurster

Collaborators: Matthew Bate & Daniel Price

University of Western Ontario  
September 28, 2017



# *Importance of Stars: Stellar Nurseries*

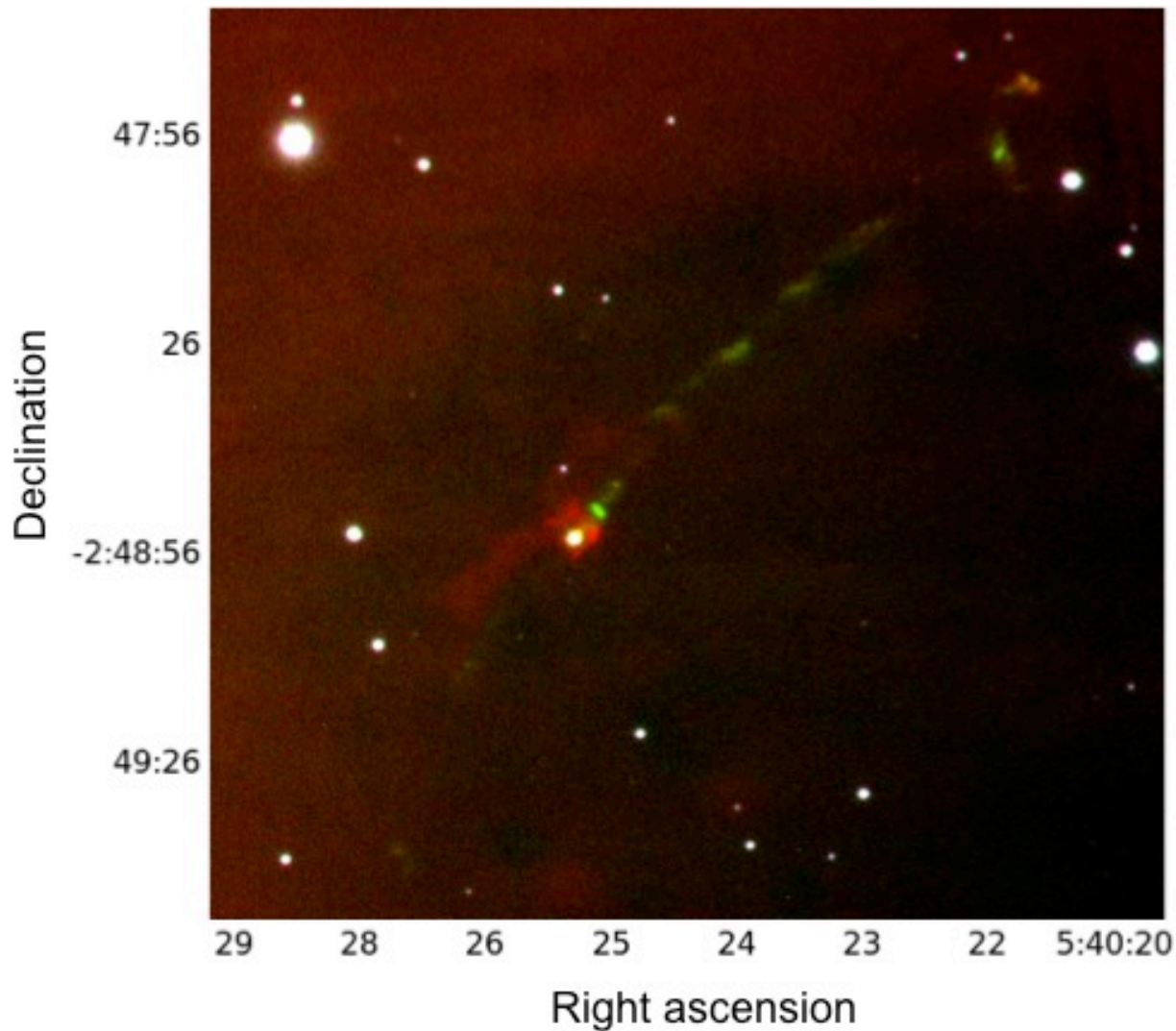


Taurus Molecular Cloud  
(Source: Credit: ESO/APEX (MPIfR/ESO/OSO)/A. Hacar et al./Digitized Sky Survey 2. Acknowledgment: Davide De Martin)

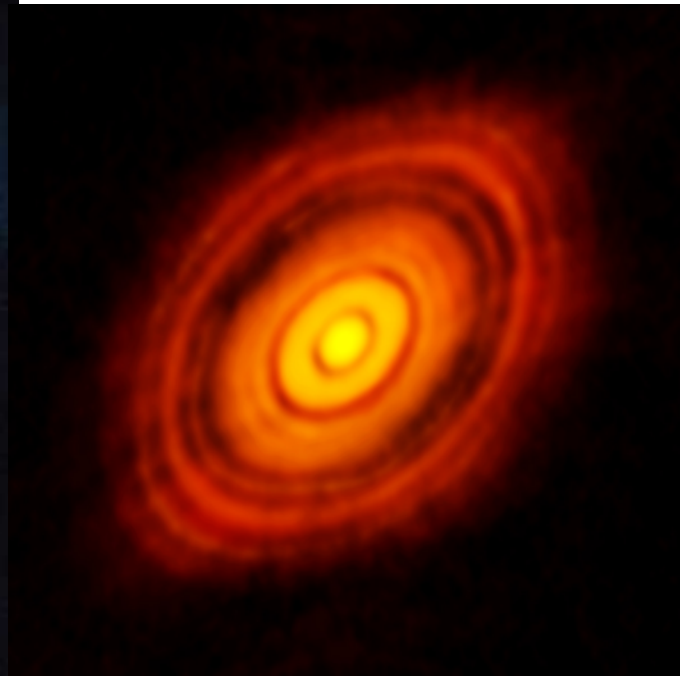
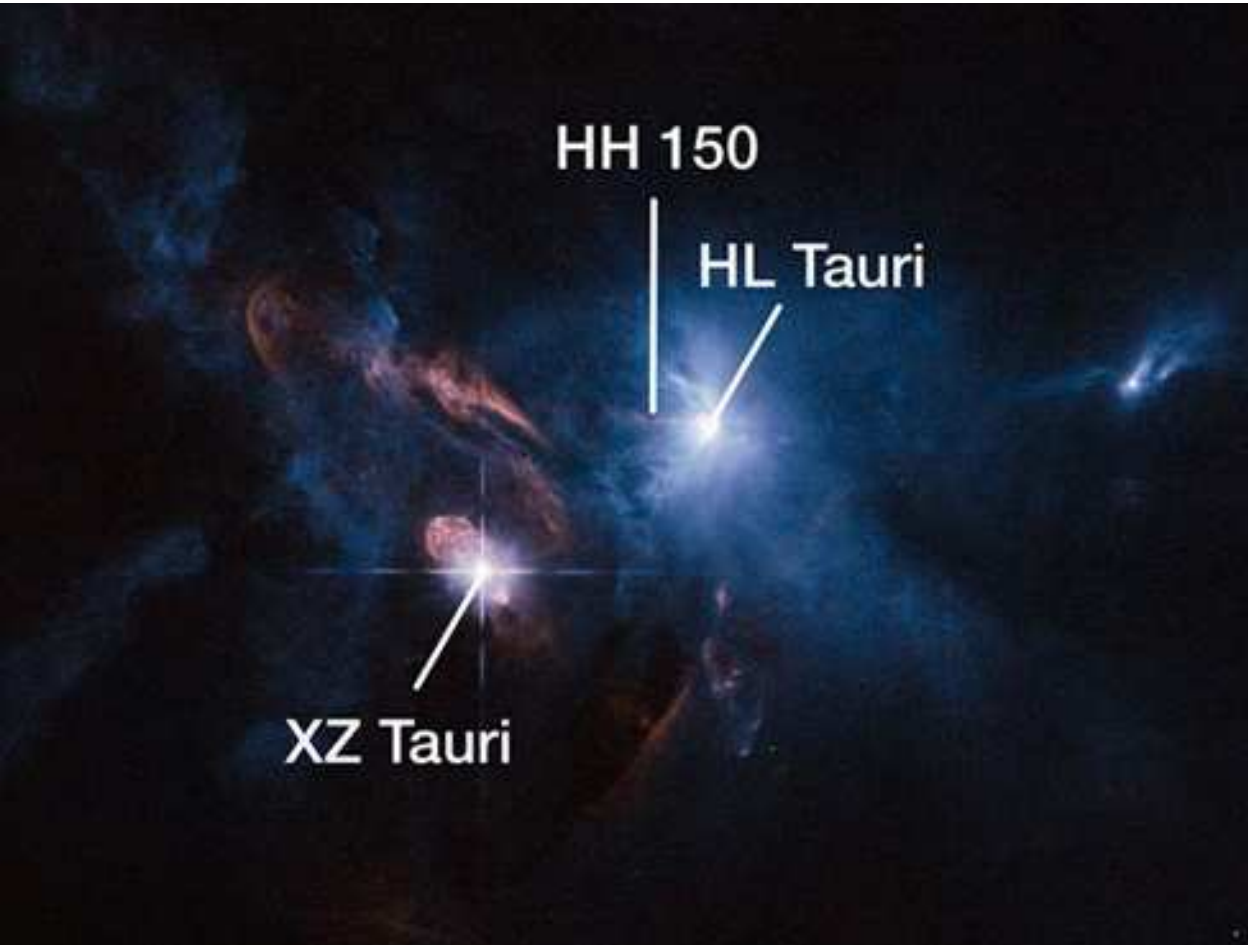
Taurus Molecular Cloud: H<sub>2</sub> column density map with positions of young stars (Goldsmith et. al., 2008)



# *Importance of Stars: Outflows*



# *Importance of Stars: Planetary Discs*



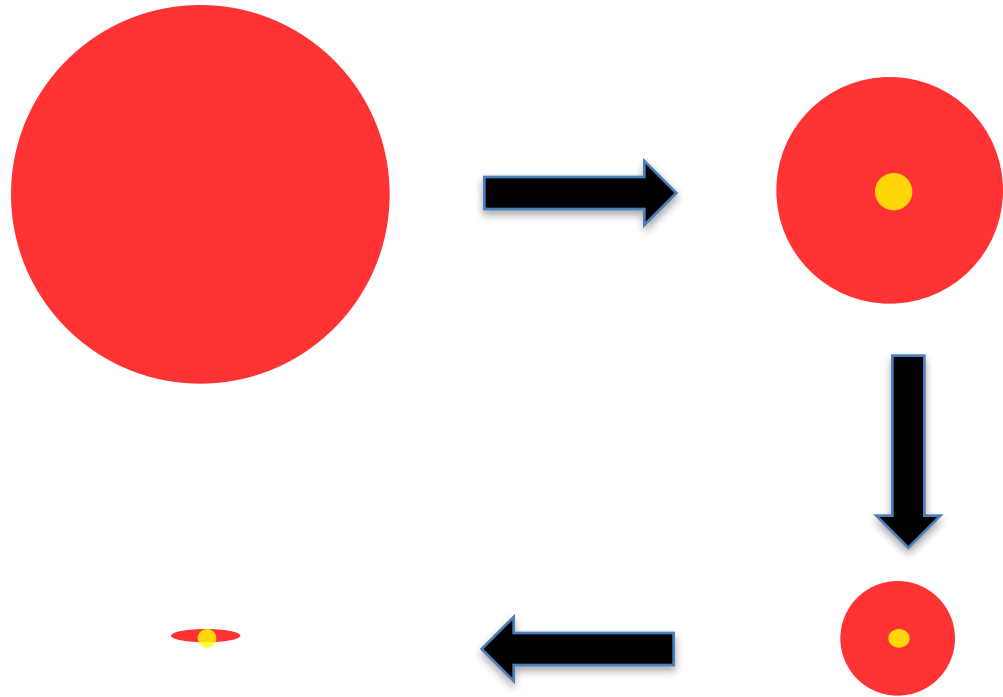


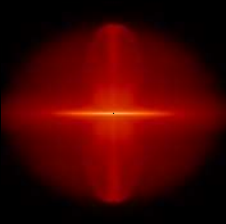


# *Star Formation: from the beginning*

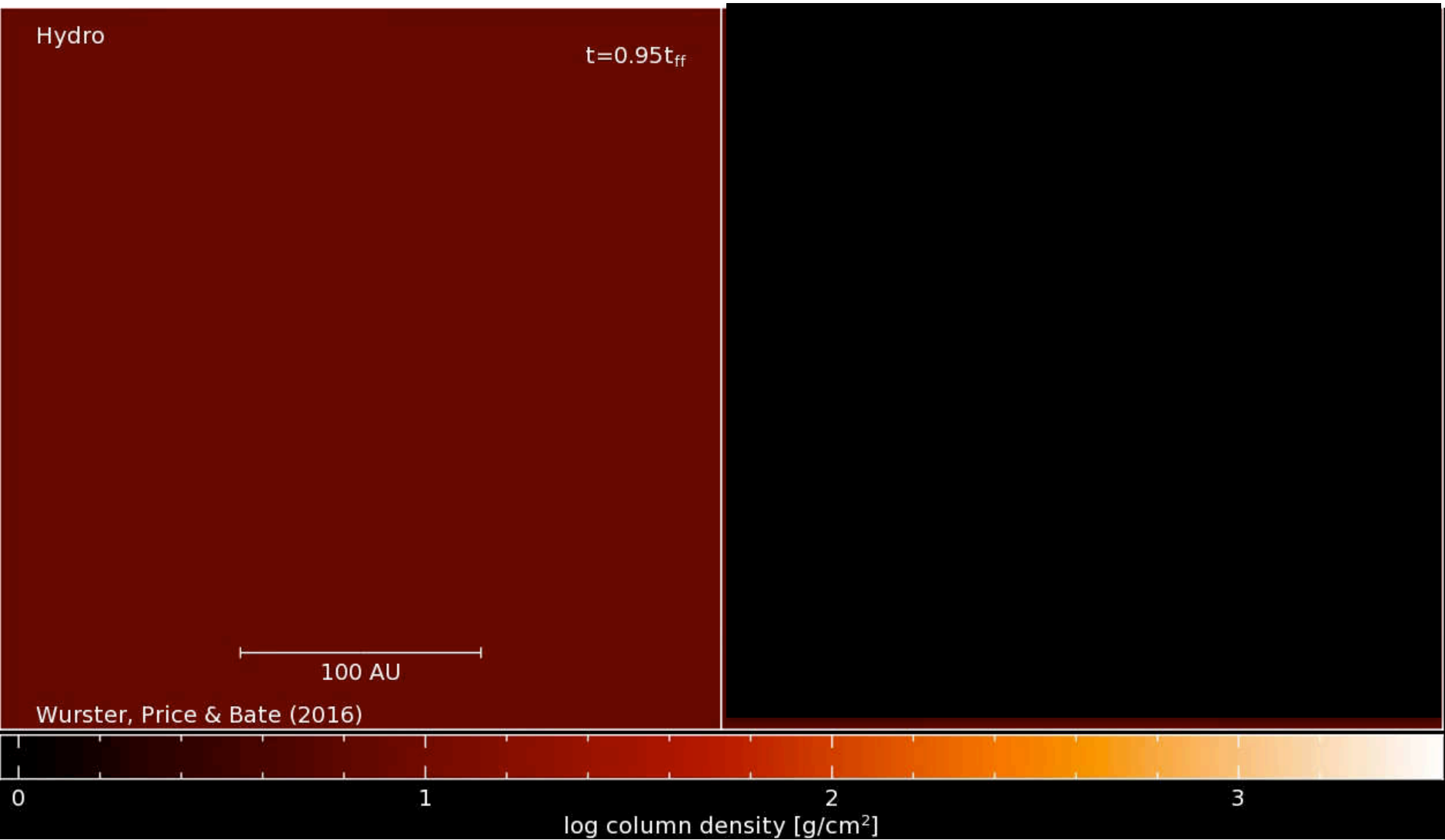


Richard Larson



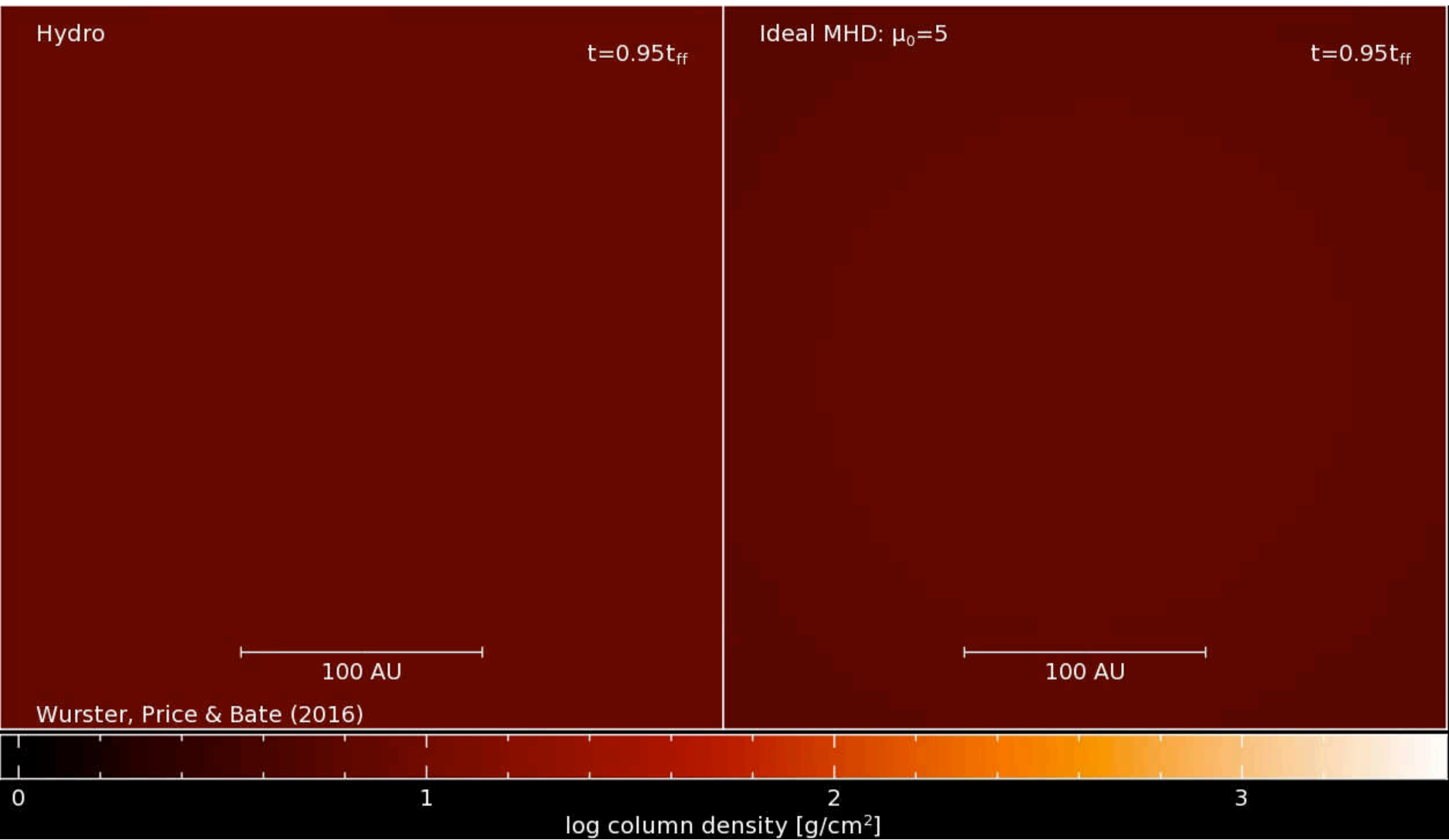


# *Disc Formation: Hydrodynamics*



Video not publically available.

# *Disc Formation: Magnetohydrodynamics*



# *Disc Formation: Magnetohydrodynamics*

## ***The Magnetic Braking Catastrophe:***

discs do not form in numerical simulations containing strong, ideal magnetic fields

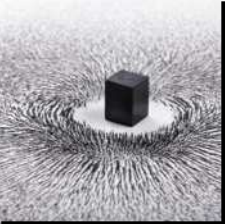


No magnetic field



Strong magnetic field



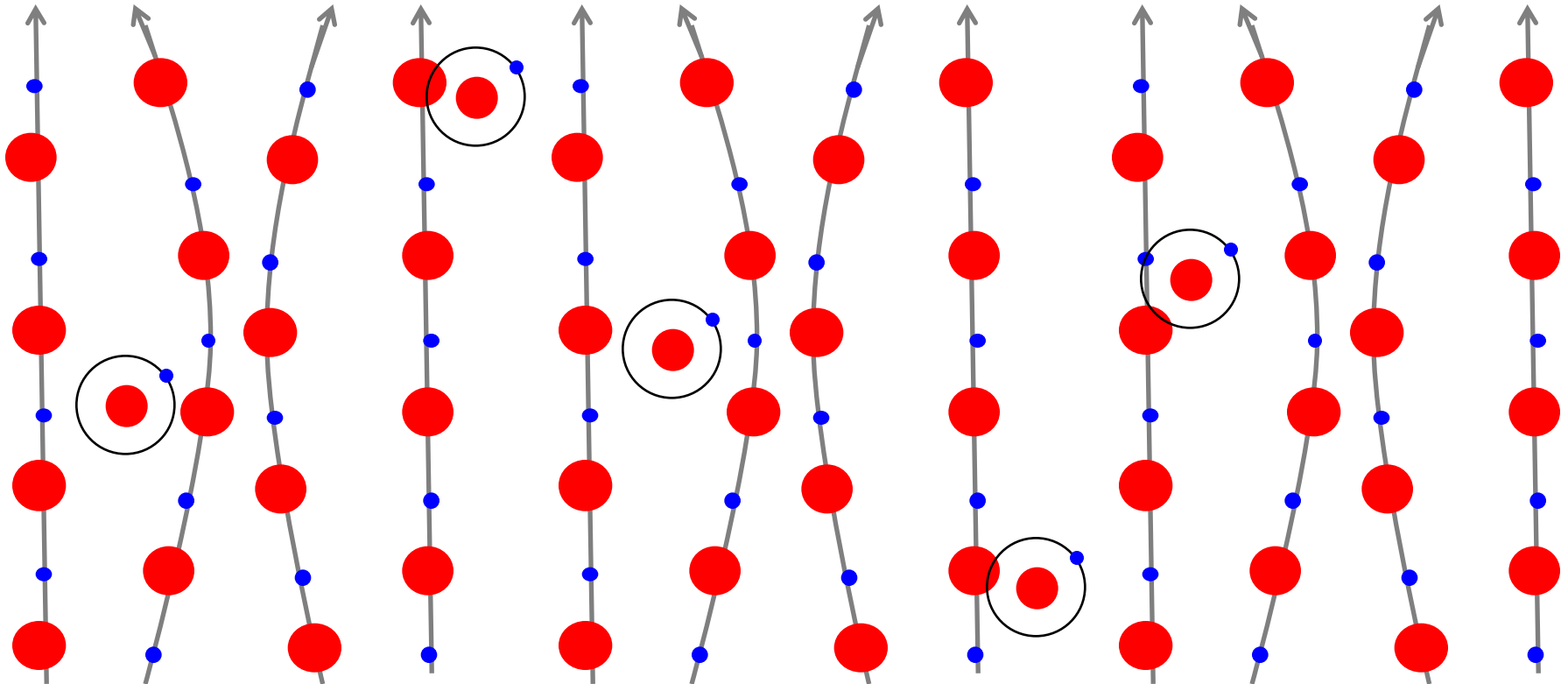


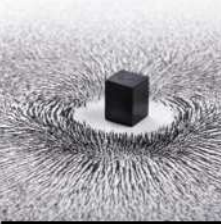
# *Ideal Magnetohydrodynamics*

➤ Fully ionised plasma    ● + ●

➤ Zero resistivity & infinite conductivity

➤ Ions & electrons are tied to the magnetic field





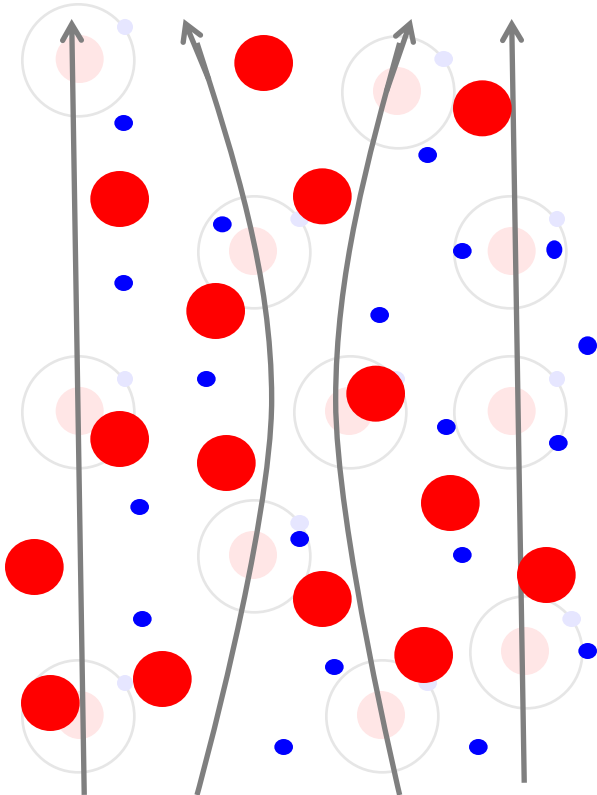
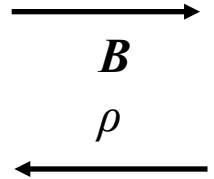
# *Non-ideal Magnetohydrodynamics*

➤ Partially ionised plasma

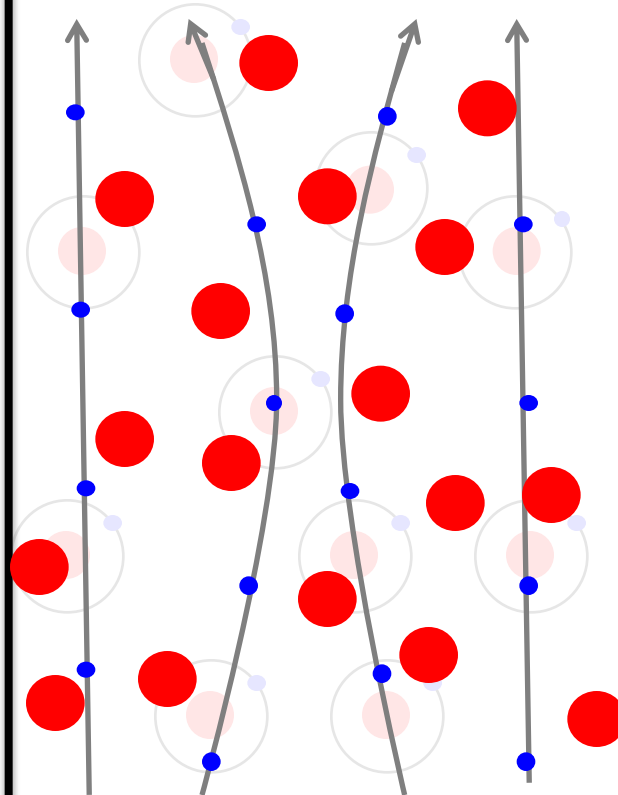


➤ Non-zero resistivity & conductivity

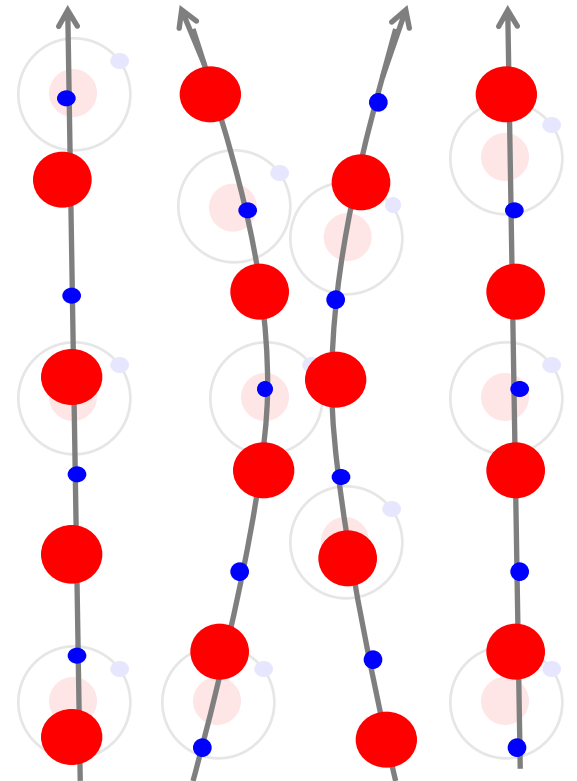
➤ Ions, electrons & neutrals behaviour is environment-dependent



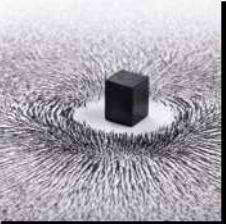
Ohmic Resistivity



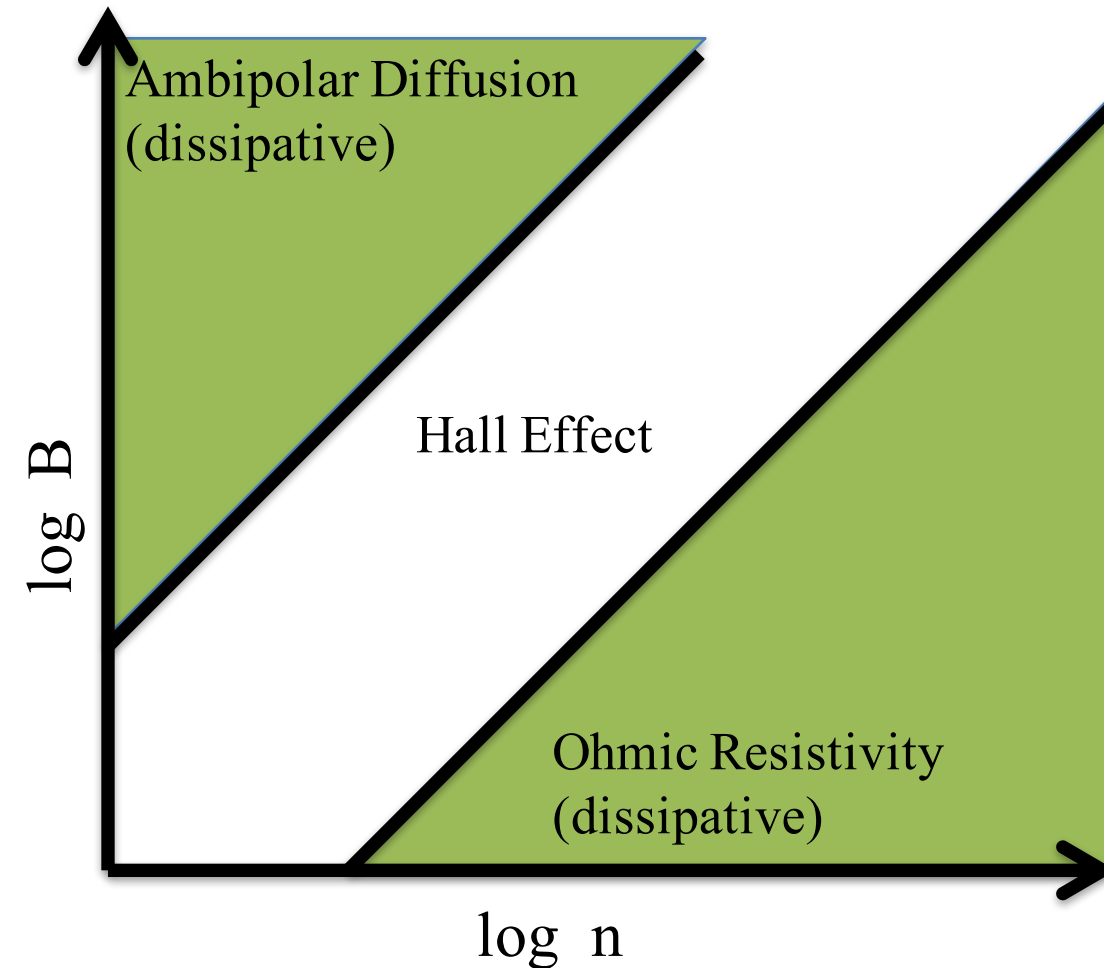
Hall Effect



Ambipolar Diffusion



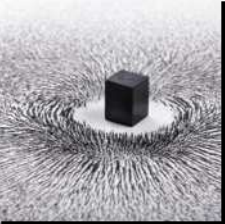
# *Non-ideal Magnetohydrodynamics*



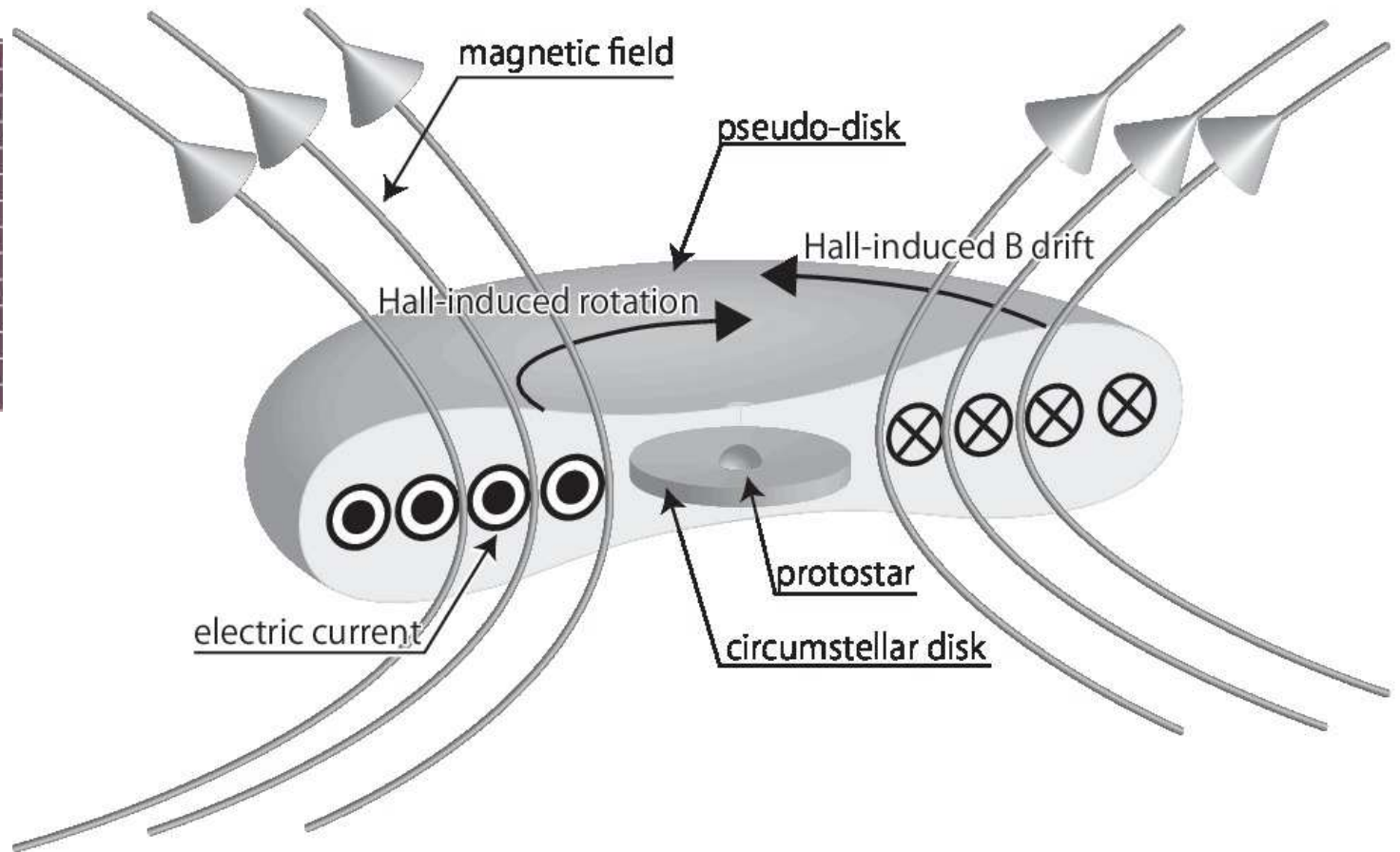
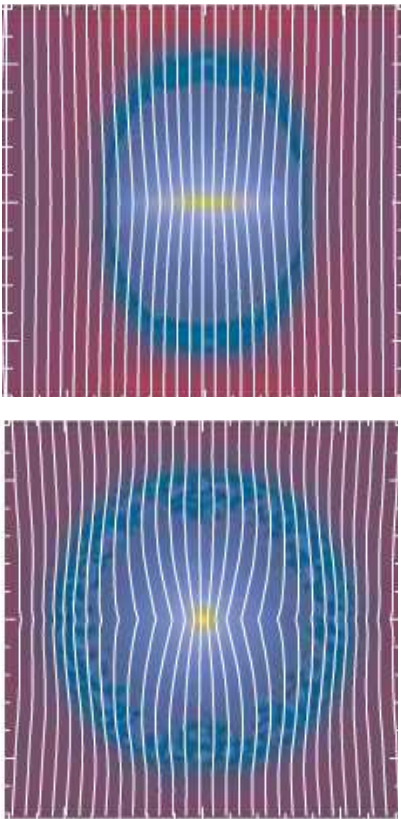
$$\left. \frac{dB}{dt} \right|_{\text{OR}} = -\nabla \times \eta_{\text{OR}} (\nabla \times B),$$

$$\left. \frac{dB}{dt} \right|_{\text{HE}} = -\nabla \times \eta_{\text{HE}} [(\nabla \times B) \times \hat{B}],$$

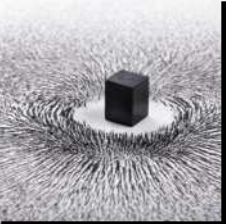
$$\left. \frac{dB}{dt} \right|_{\text{AD}} = \nabla \times \eta_{\text{AD}} \left\{ [(\nabla \times B) \times \hat{B}] \times \hat{B} \right\}.$$



# *Non-ideal Magnetohydrodynamics*

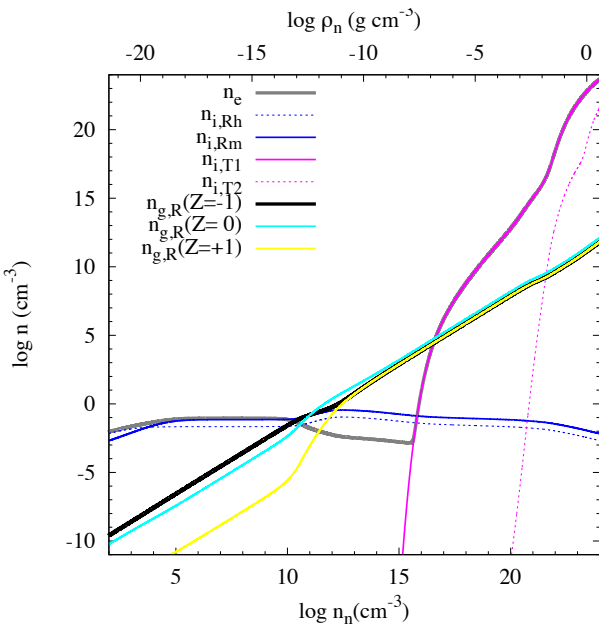


Price & Bate (2007)

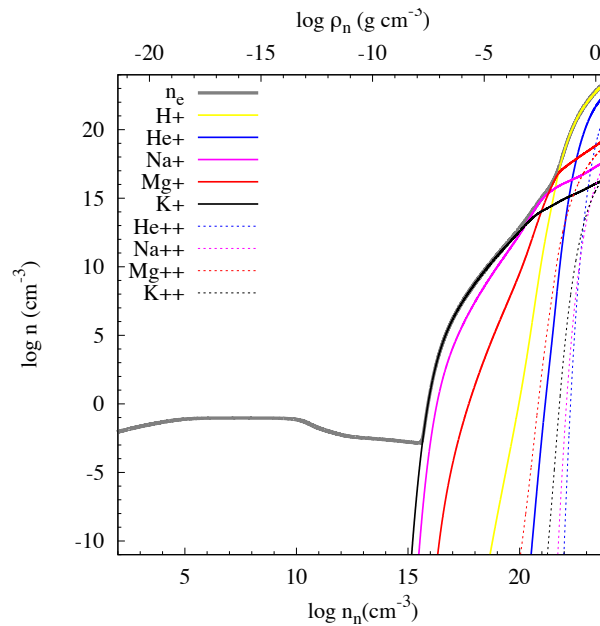


# Non-ideal Magnetohydrodynamics

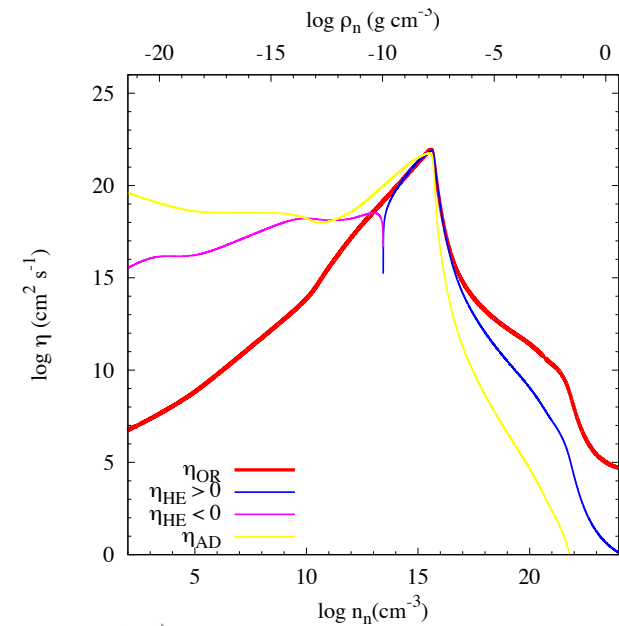
Cosmic ray ionisation:



Thermal ionisation:



Coefficients:



- Includes
  - Heavy & light ions
  - grains

- Includes
  - 5 singly ionised elements
  - 4 doubly ionised elements

$$\left. \frac{dB}{dt} \right|_{OR} = -\nabla \times \eta_{OR} (\nabla \times B),$$

$$\left. \frac{dB}{dt} \right|_{HE} = -\nabla \times \eta_{HE} [(\nabla \times B) \times \hat{B}],$$

$$\left. \frac{dB}{dt} \right|_{AD} = \nabla \times \eta_{AD} \left\{ [(\nabla \times B) \times \hat{B}] \times \hat{B} \right\}.$$





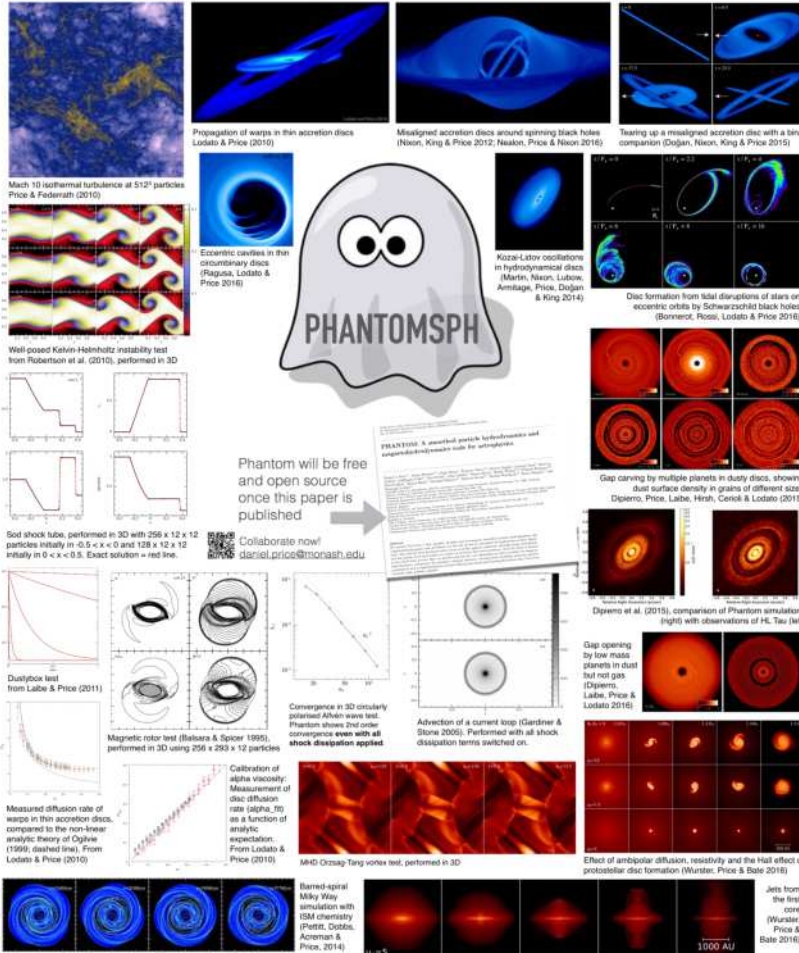
# Phantom

## The Phantom SPH code

MONASH University

MoCA

Daniel Price<sup>1</sup>, James Wurster<sup>1,2</sup>, Chris Nixon<sup>1</sup>, Terenzo Tricco<sup>1,3</sup>, Sébastien Toupin<sup>1</sup>, Conrad Chan<sup>1</sup>, Rebecca Nealon<sup>1</sup>, Guillaume Laibe<sup>4</sup>, Alex Patten<sup>1,5</sup>, Claire Dobbs<sup>1</sup>, Simon Glover<sup>6</sup>, Hauke Worpel<sup>1</sup>, Clement Bonnerot<sup>7</sup>, David Litali<sup>1</sup>, Giovanni D'Angelo<sup>1</sup>, Enrico Ragusa<sup>1</sup>, Duncan Fargnoli<sup>1</sup>, Roberto Iacono<sup>1</sup>, Thomas Reichardt<sup>1</sup> and Giuseppe Lodati<sup>1</sup>  
<sup>1</sup>Maxwell Centre for Astrophysics, School of Physics and Astronomy, Monash University, Australia; <sup>2</sup>School of Physics, University of Exeter, Exeter EX4 4QJ, UK; <sup>3</sup>Department of Physics and Astronomy, University of Lethbridge, Lethbridge, AB T1K 3M4, Canada; <sup>4</sup>Department of Physics and Astronomy, University of Toronto, Toronto, ON M5S 3J4, Canada; <sup>5</sup>Institute of Astrophysics (IAU), Universität Wien (A13), CP08, Boltzmanngasse 5, A-1090 Vienna, Austria; <sup>6</sup>Department of Physics and Astronomy, University of St. Andrews, North Haugh, St. Andrews, Fife KY16 9SS, UK; <sup>7</sup>Department of Physics, Heidelberg University, Heidelberg, Germany; <sup>8</sup>Department of Physics and Astronomy, University of Exeter, Exeter EX4 4QJ, UK; <sup>9</sup>Department of Physics and Astronomy, University of Exeter, Exeter EX4 4QJ, UK; <sup>10</sup>Department of Physics and Astronomy, University of Exeter, Exeter EX4 4QJ, UK; <sup>11</sup>Department of Physics and Astronomy, University of Exeter, Exeter EX4 4QJ, UK; <sup>12</sup>Department of Physics and Astronomy, University of Exeter, Exeter EX4 4QJ, UK; <sup>13</sup>Department of Physics and Astronomy, University of Exeter, Exeter EX4 4QJ, UK; <sup>14</sup>Department of Physics and Astronomy, University of Exeter, Exeter EX4 4QJ, UK; <sup>15</sup>Department of Physics and Astronomy, University of Exeter, Exeter EX4 4QJ, UK

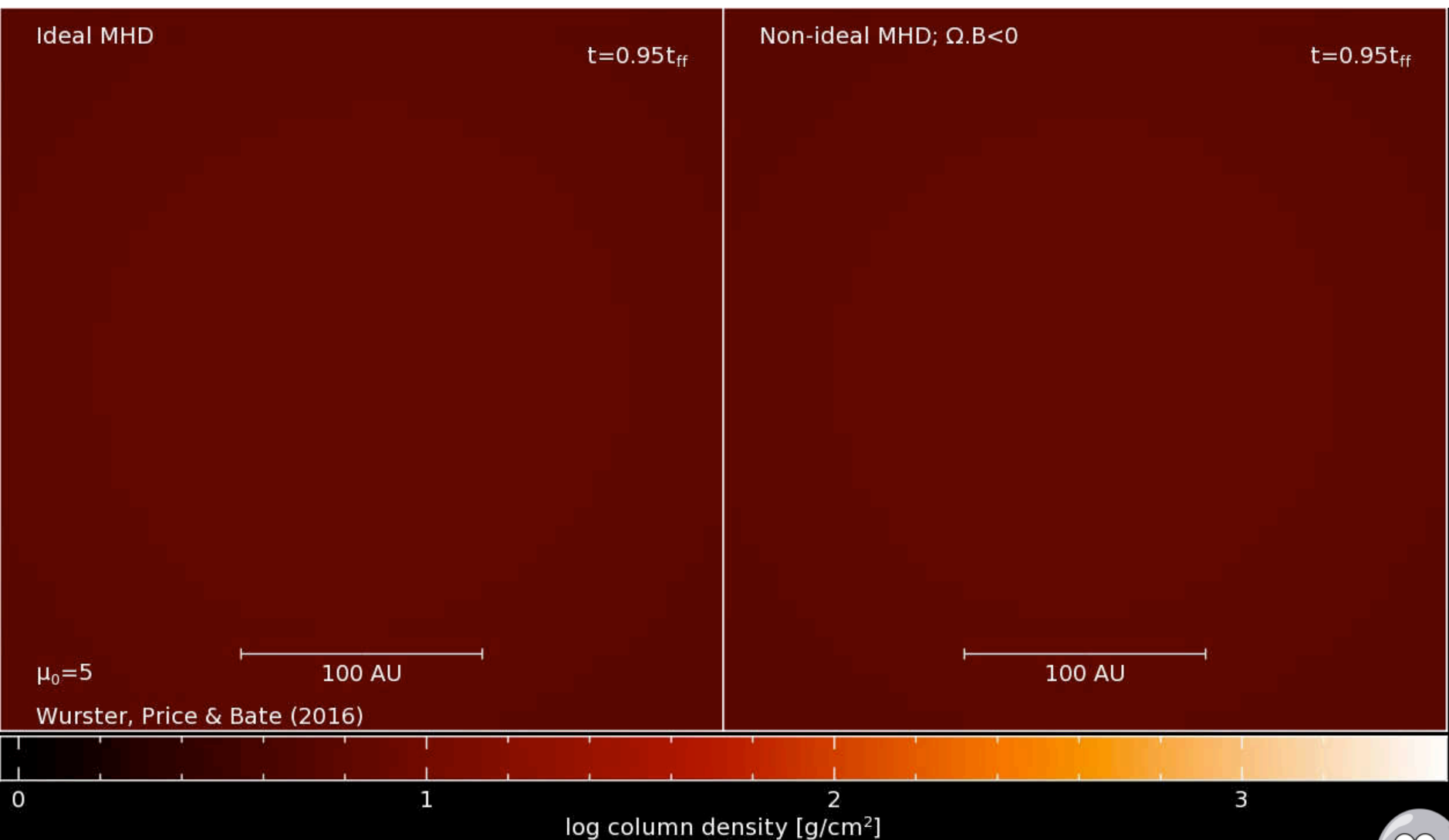


## ➤ Phantom

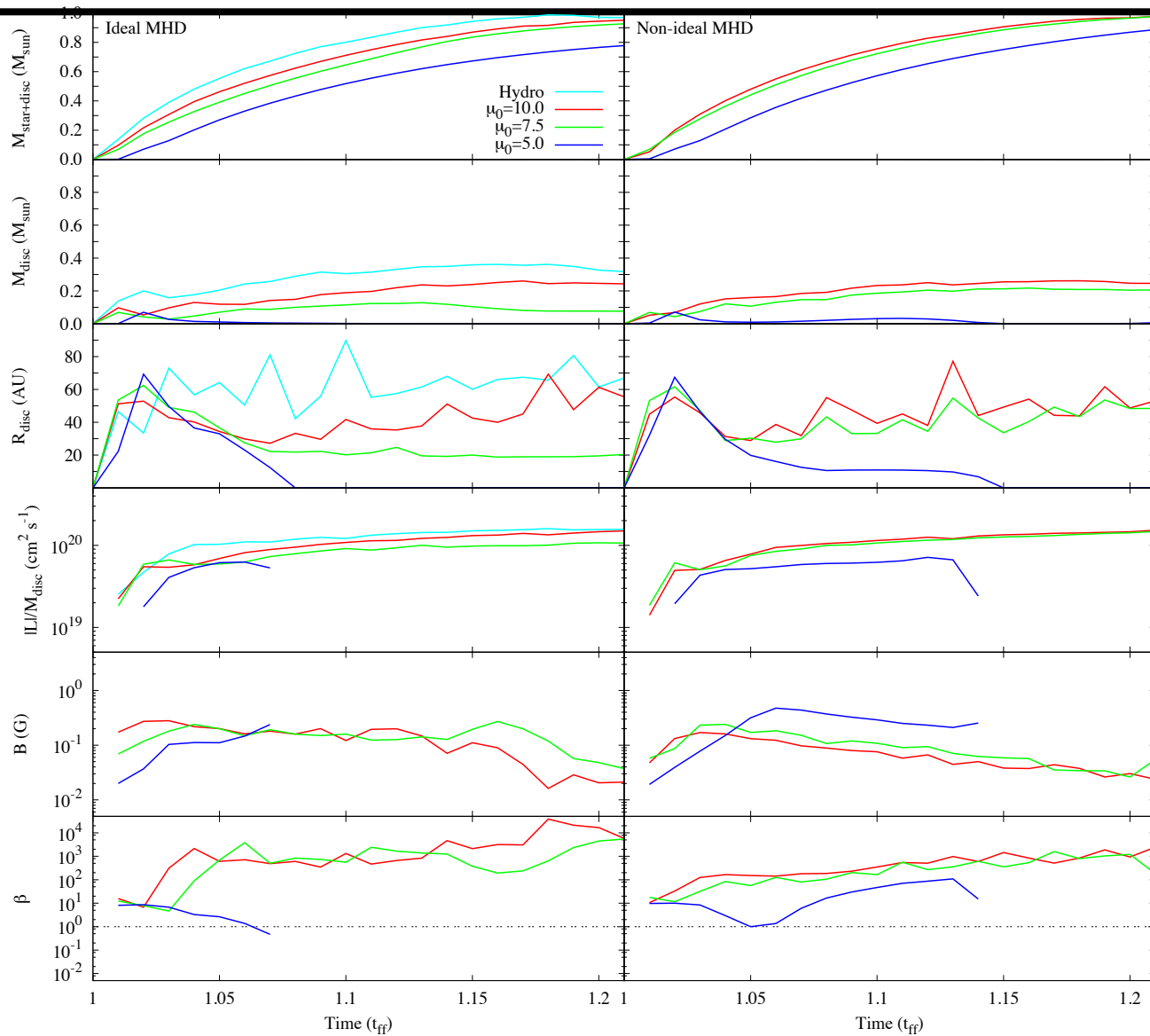
- Publically available at <https://phantomsph.bitbucket.io>
- Reference:
- D. J. Price, J. Wurster, C. Nixon, T. S. Tricco, and 22 others. (arXiv:1702.03930)

Hydrodynamics — Accretion discs — Sink particles — Self-gravity  
 Magnetohydrodynamics (MHD) — Two fluid dust-gas — One fluid dust-gas  
 Non-ideal MHD — H<sub>2</sub> and CO interstellar medium chemistry — Wind injection

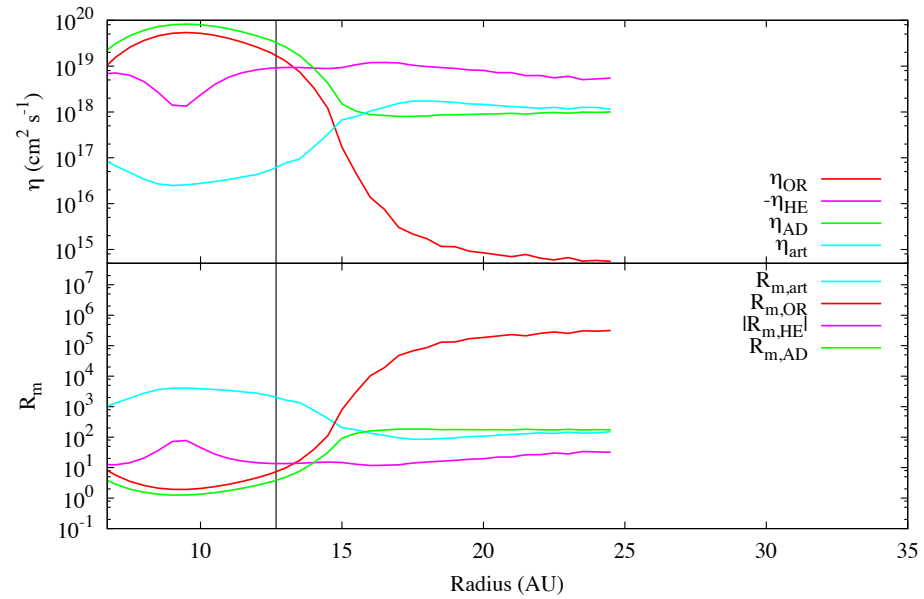
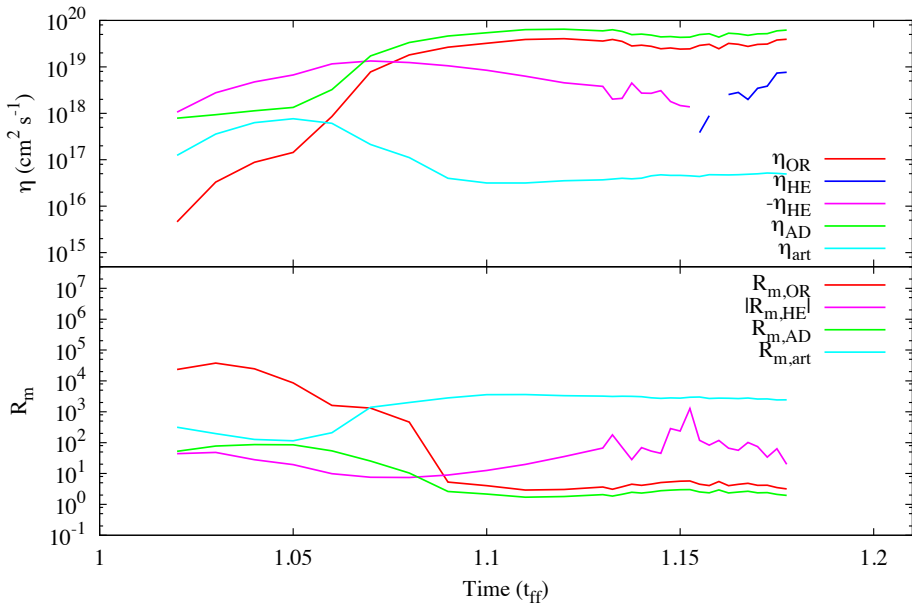
# *Disc Formation: Ideal & Non-ideal MHD*



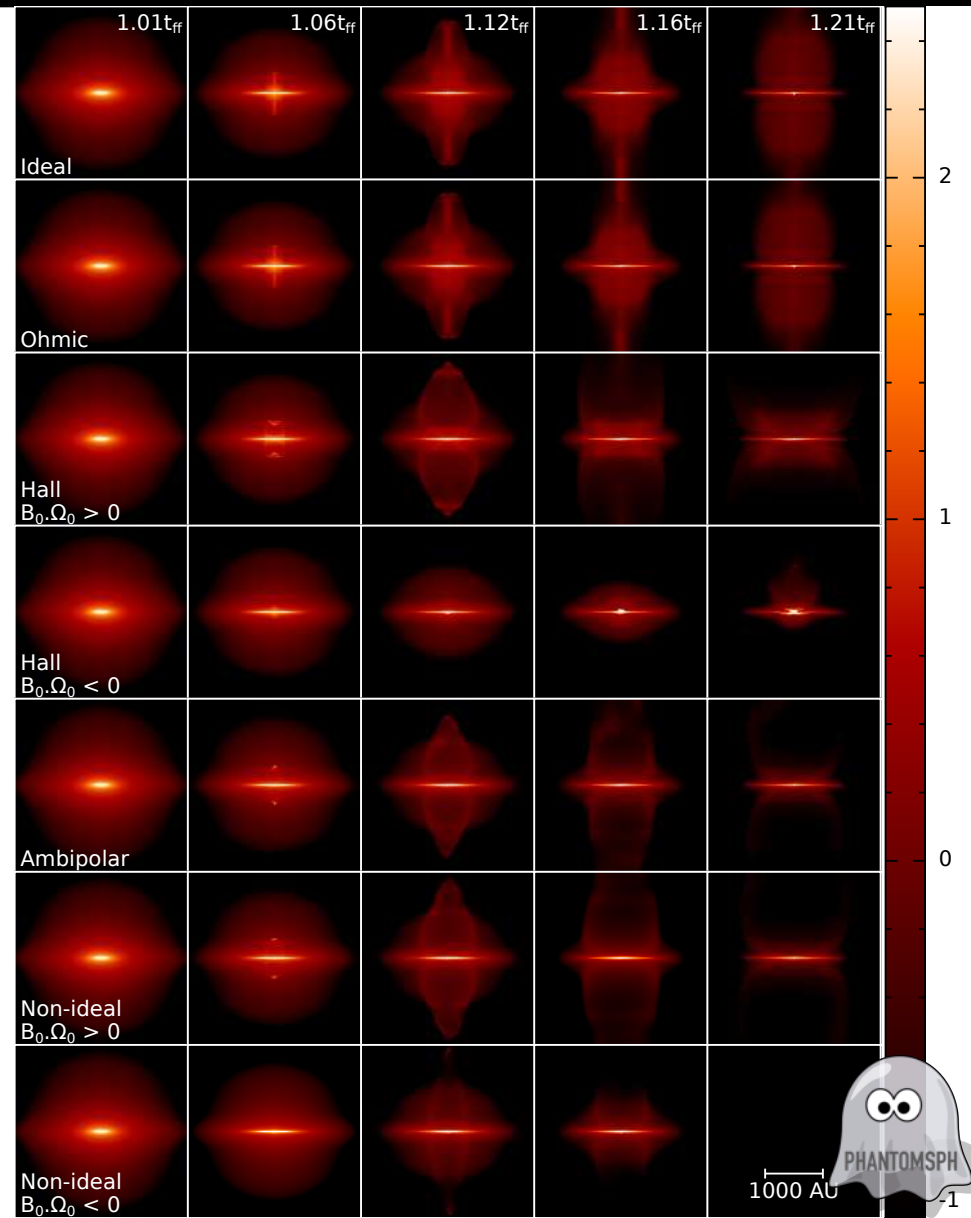
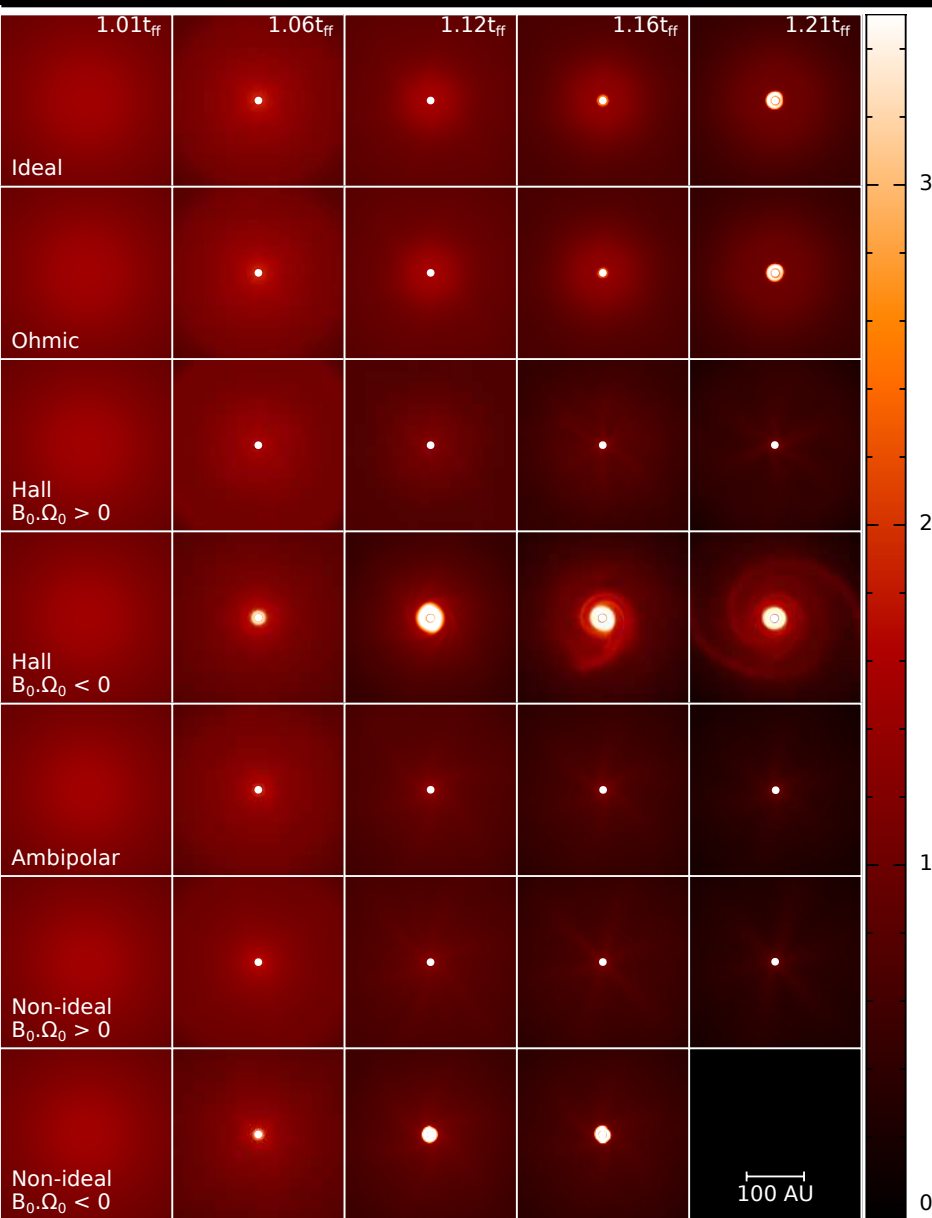
# Disc Properties



# Disc Properties

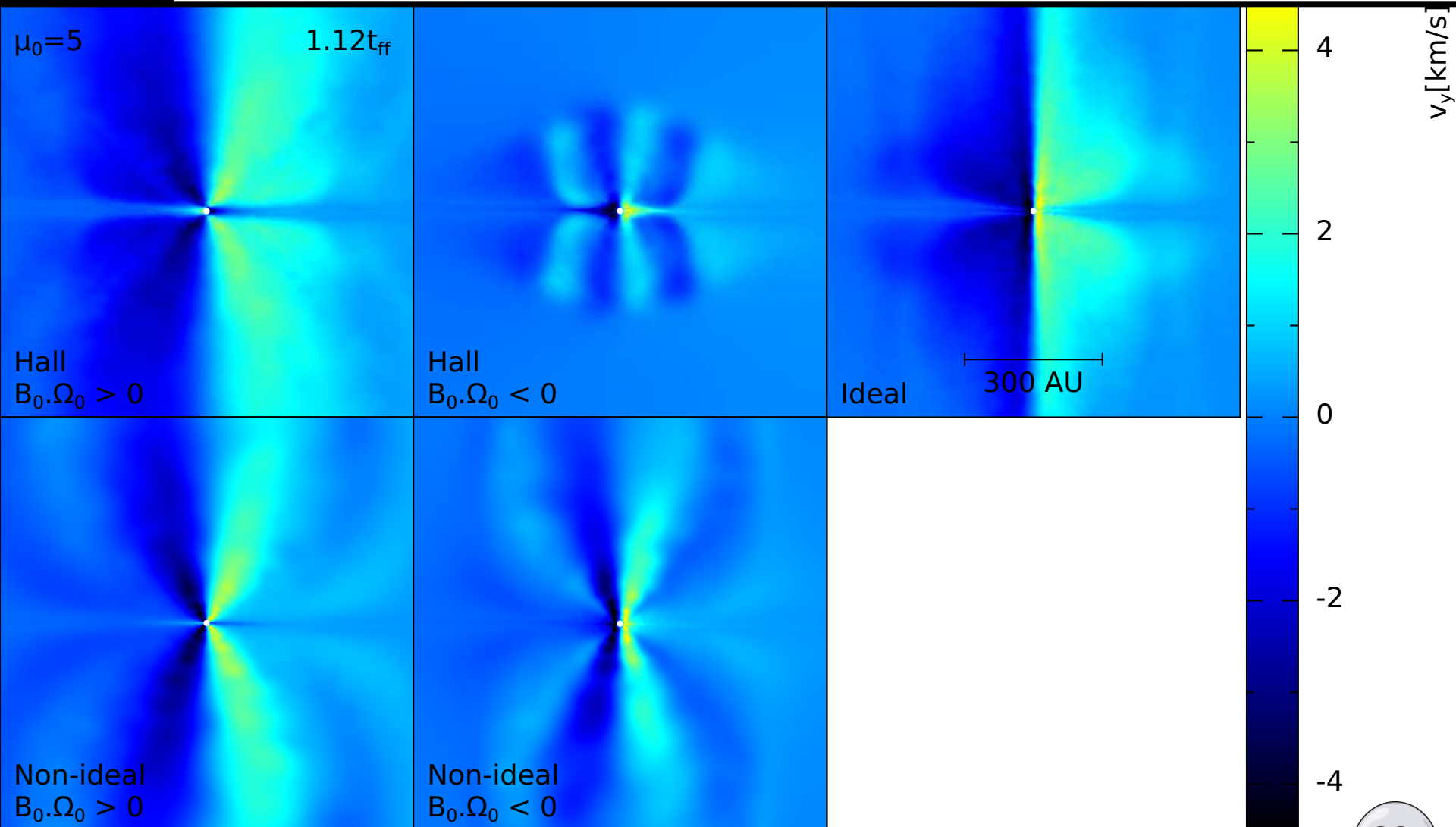


# Non-Ideal MHD Components





# Counter-rotating Envelope

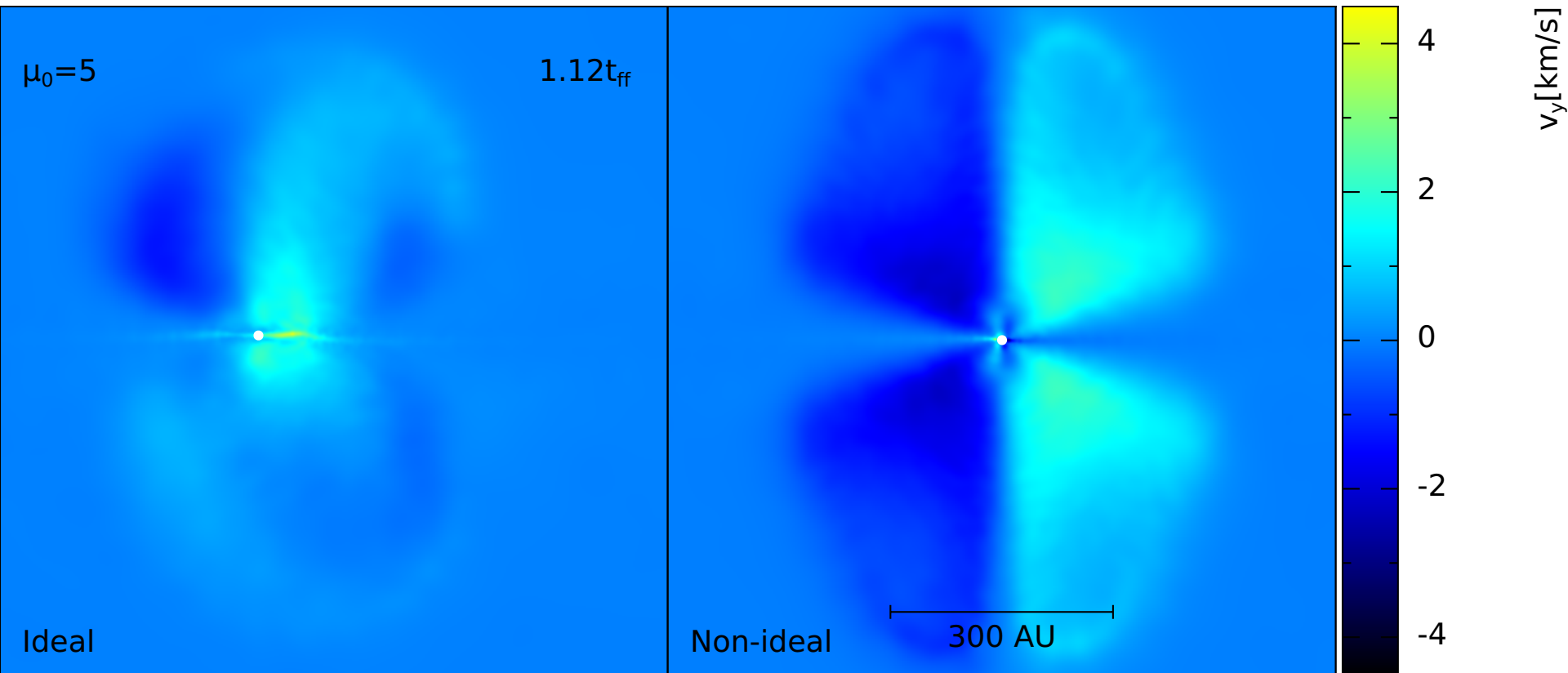


Wurster, Price & Bate (2016); see also Tsukamoto et al (2015)

➤ Hall effect induces the formation of a counter-rotating envelope



# Induced Rotation



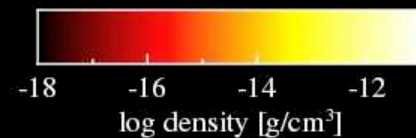
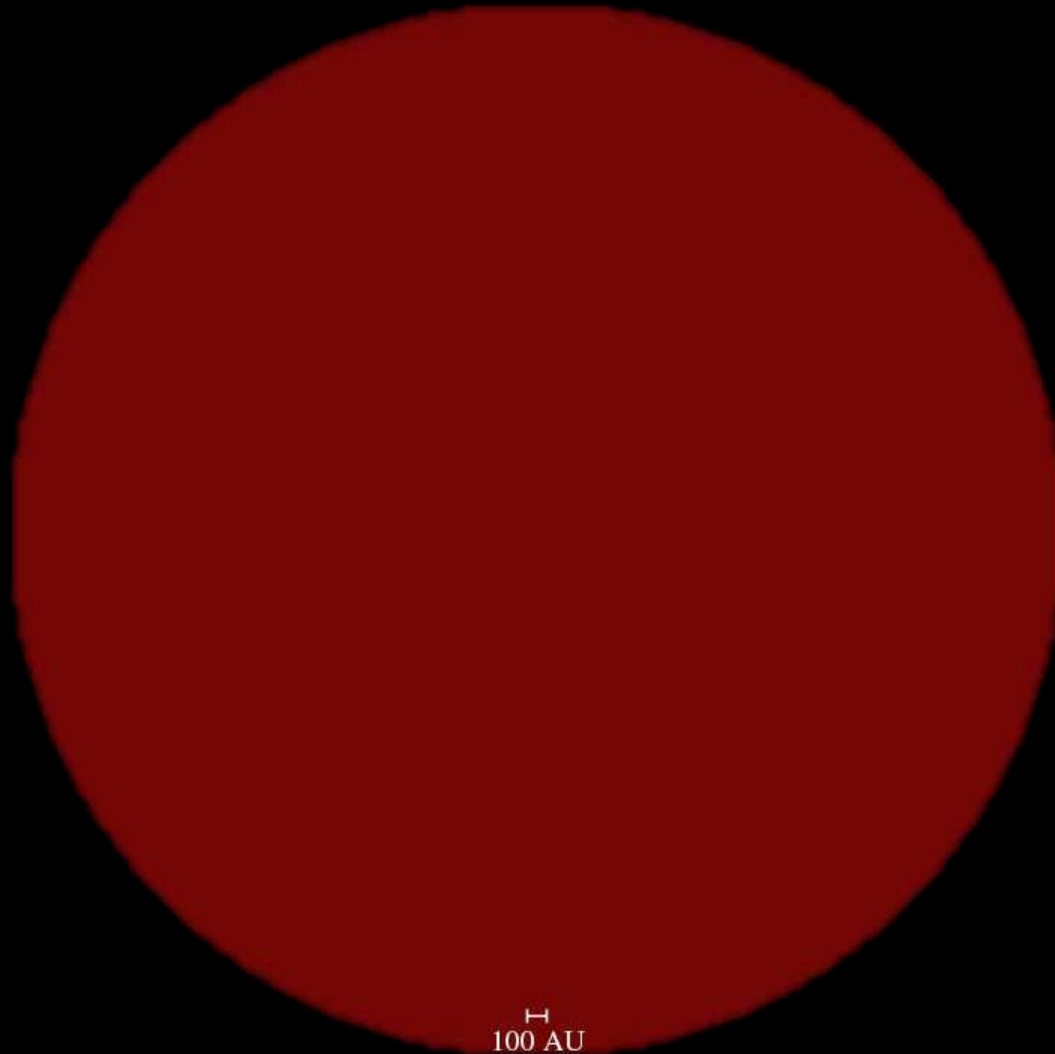
- Hall effect can induce coherent rotation from a zero-angular momentum initial condition



t = 25080 yrs

# *Collapse to stellar densities*

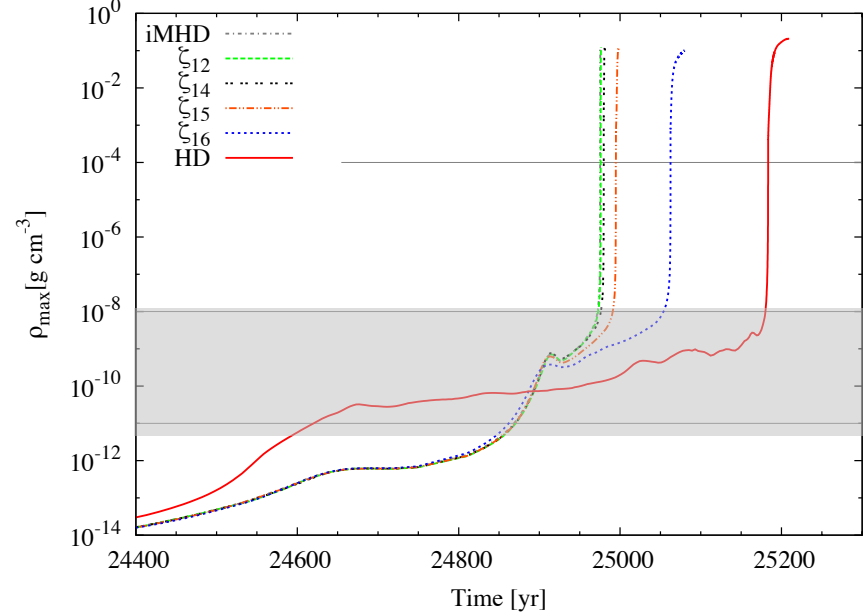
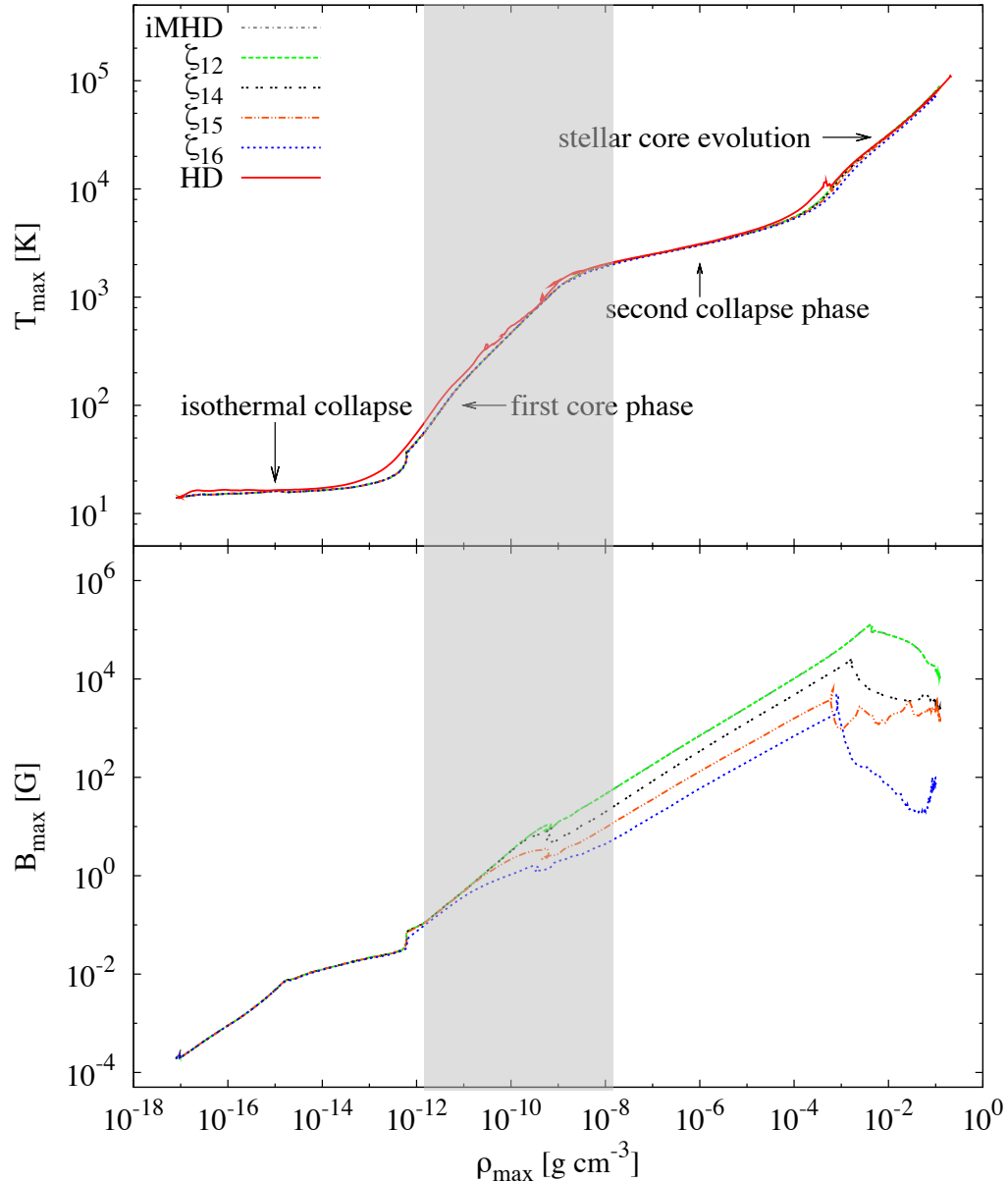
Time: 0 yrs

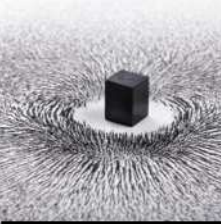


Bate, Tricco & Price (2013)

➤ Ideal MHD. Video available at [https://www.astro.ex.ac.uk/people/mbate/Animations/BateTriccoPrice2013\\_MF05.mov](https://www.astro.ex.ac.uk/people/mbate/Animations/BateTriccoPrice2013_MF05.mov)

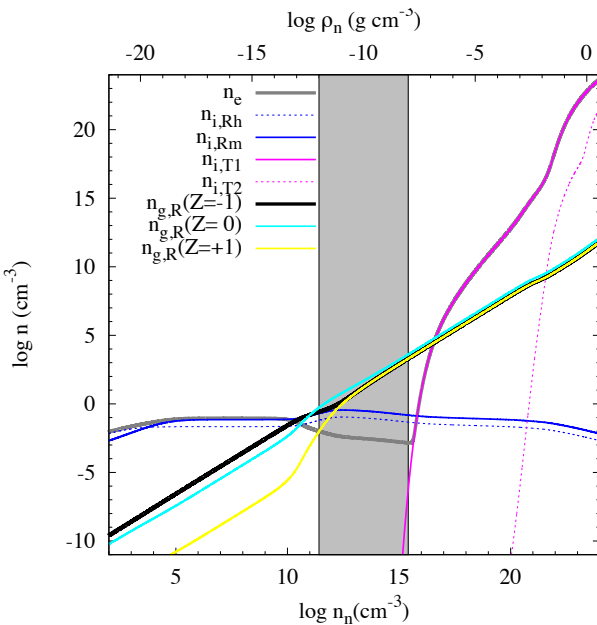
# Collapse to stellar densities: First Hydrostatic Core



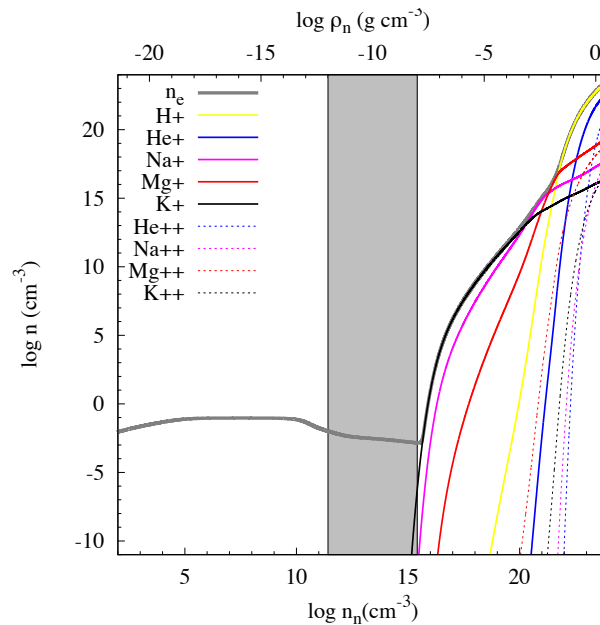


# Collapse to stellar densities: FHC: Non-ideal Magnetohydrodynamics

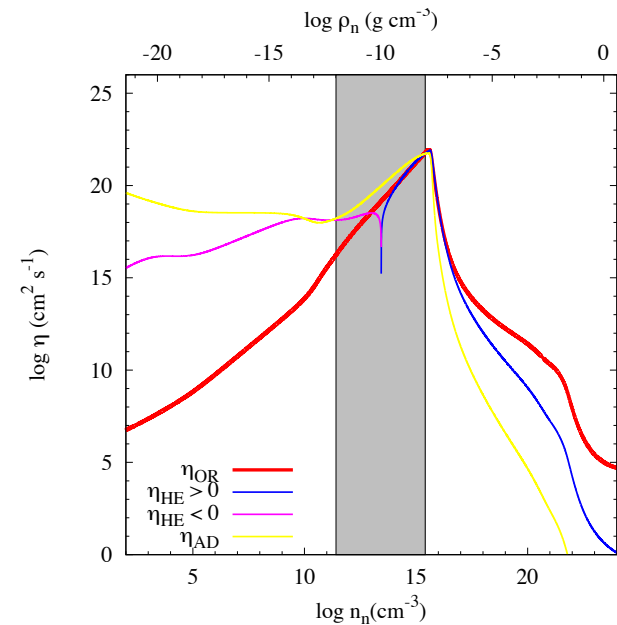
Cosmic ray ionisation:



Thermal ionisation:



Coefficients:



- Includes
  - Heavy & light ions
  - grains

- Includes
  - 5 singly ionised elements
  - 4 doubly ionised elements

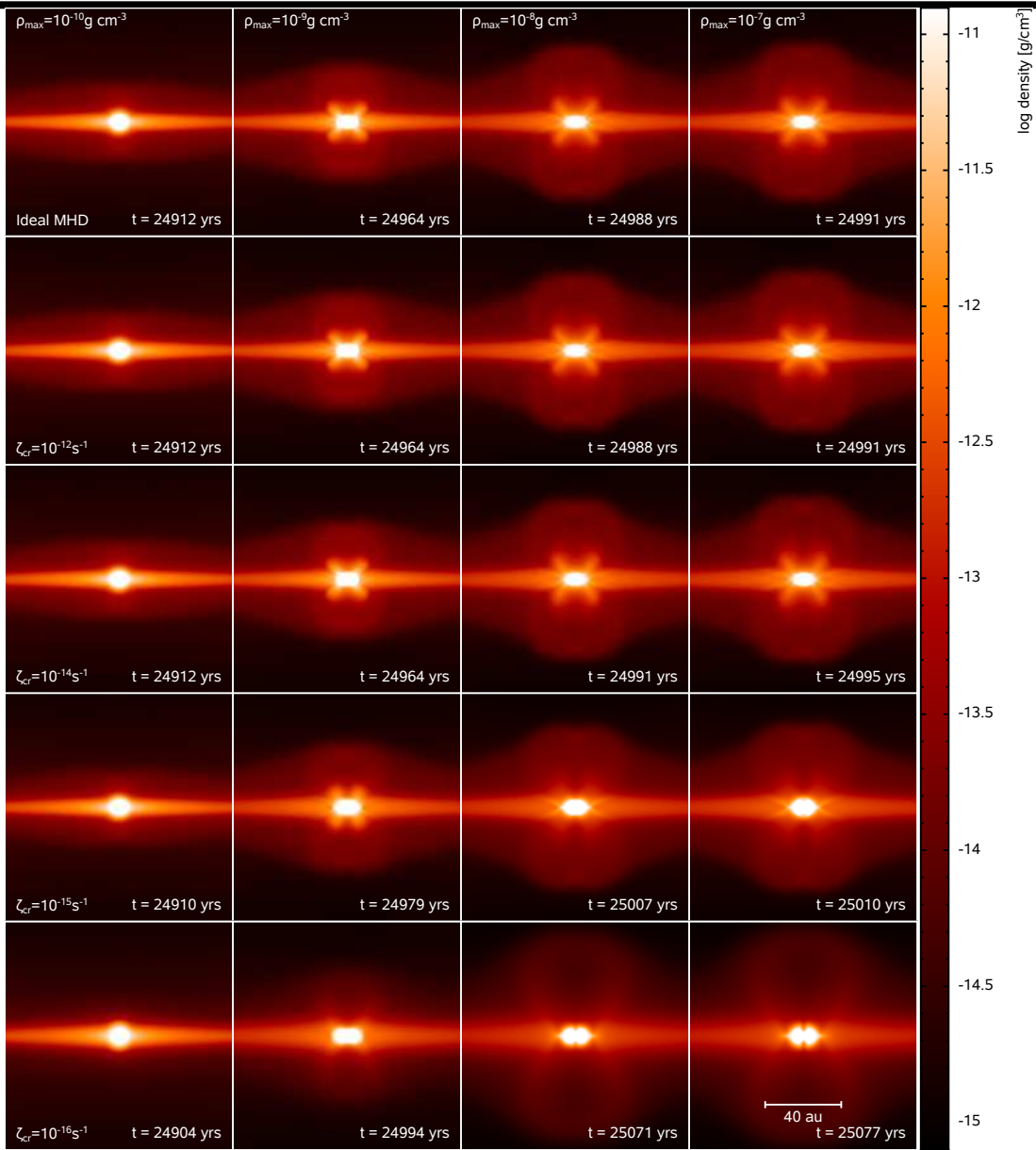
$$\left. \frac{dB}{dt} \right|_{OR} = -\nabla \times \eta_{OR} (\nabla \times B),$$

$$\left. \frac{dB}{dt} \right|_{HE} = -\nabla \times \eta_{HE} [(\nabla \times B) \times \hat{B}],$$

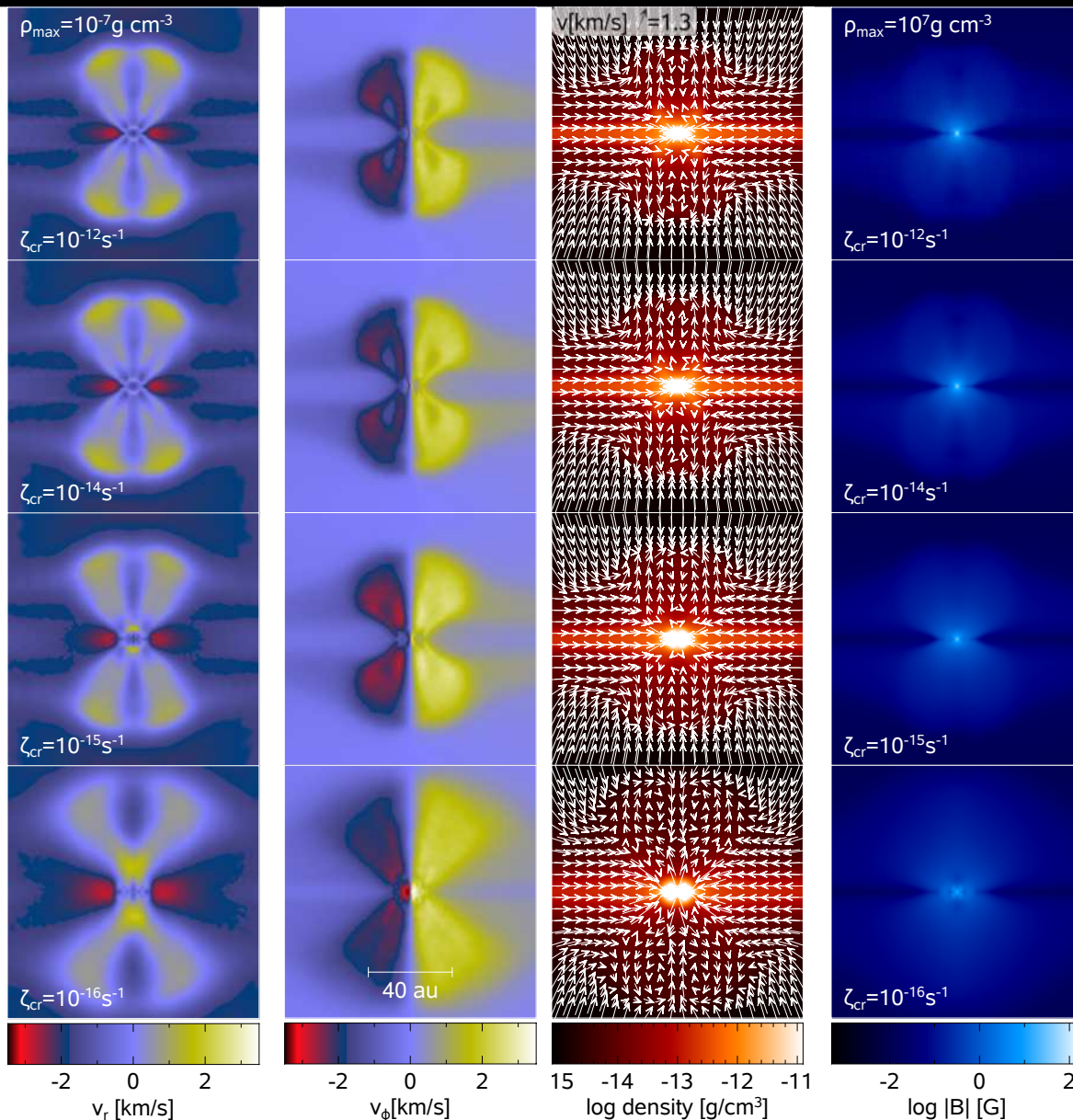
$$\left. \frac{dB}{dt} \right|_{AD} = \nabla \times \eta_{AD} \left\{ [(\nabla \times B) \times \hat{B}] \times \hat{B} \right\}.$$



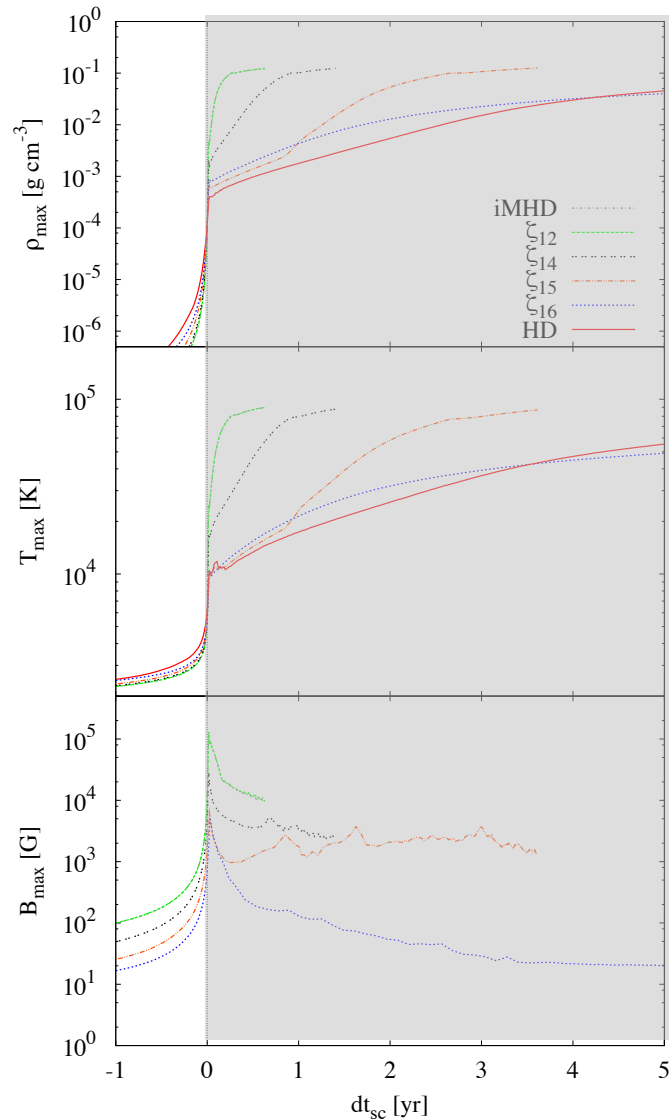
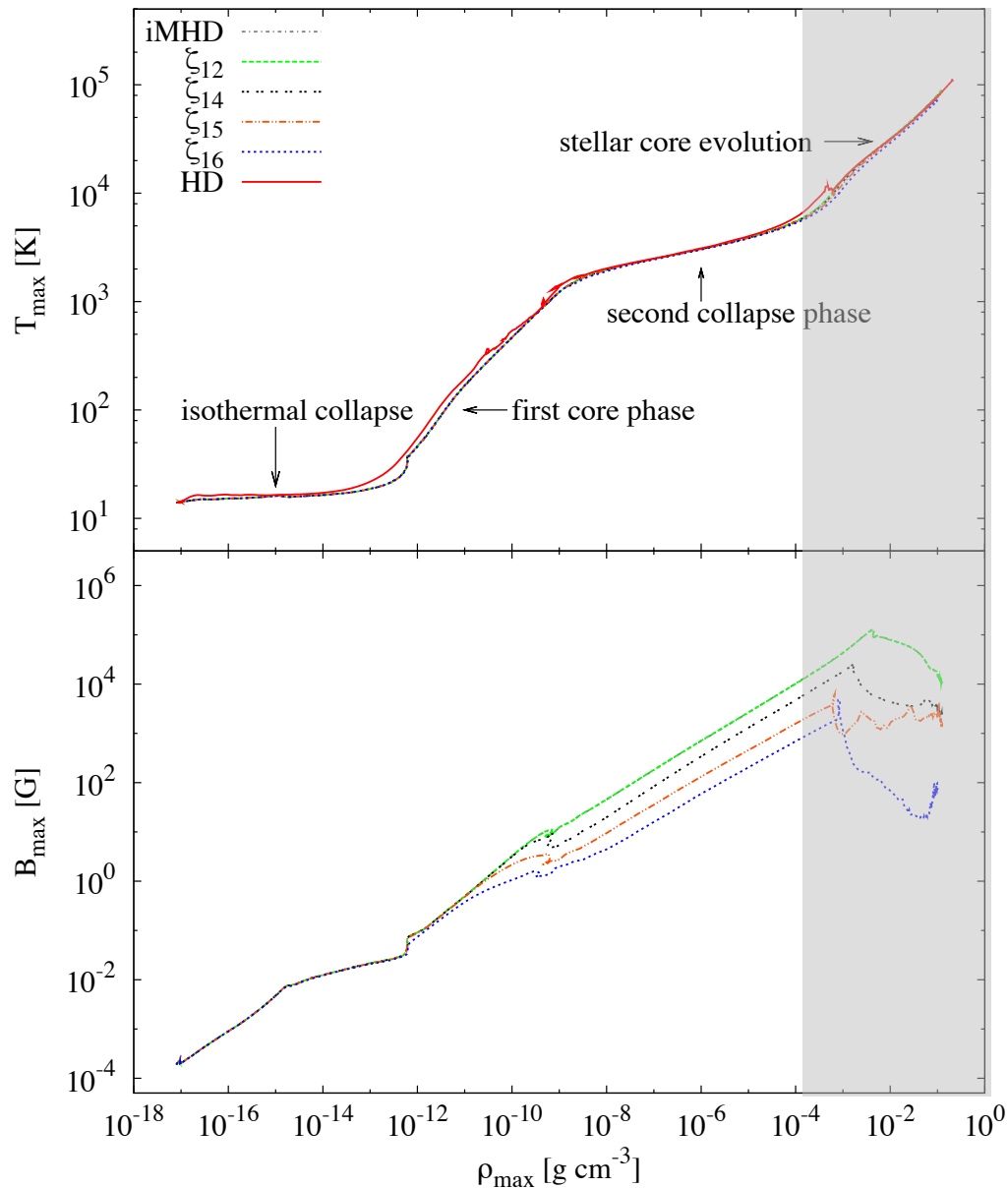
# *Collapse to stellar densities: First Hydrostatic Core*

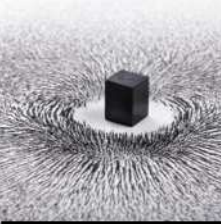


# *Collapse to stellar densities: First Hydrostatic Core*



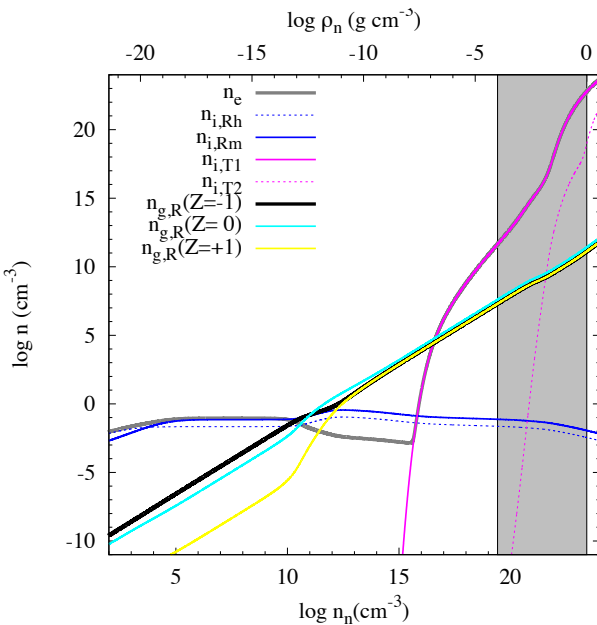
# Collapse to stellar densities: Stellar core



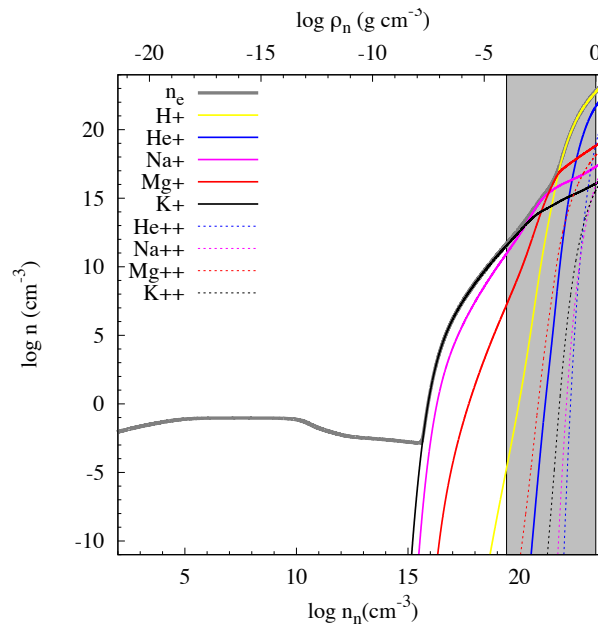


# Collapse to stellar densities: SHC: Non-ideal Magnetohydrodynamics

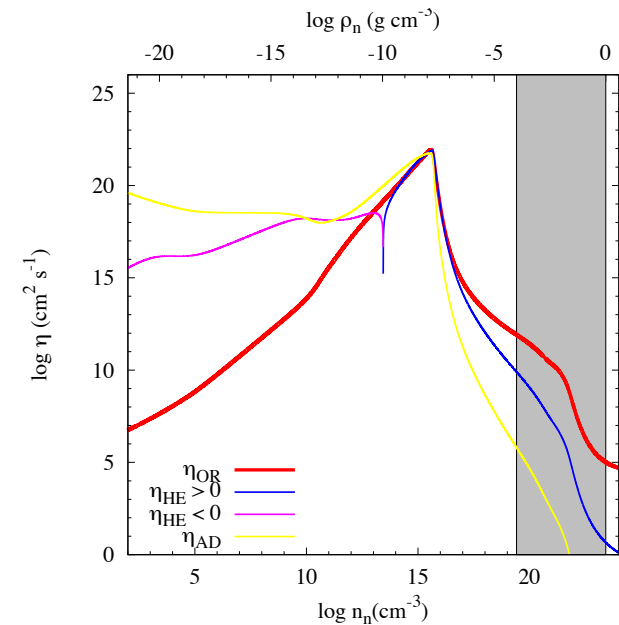
Cosmic ray ionisation:



Thermal ionisation:



Coefficients:



- Includes
  - Heavy & light ions
  - grains

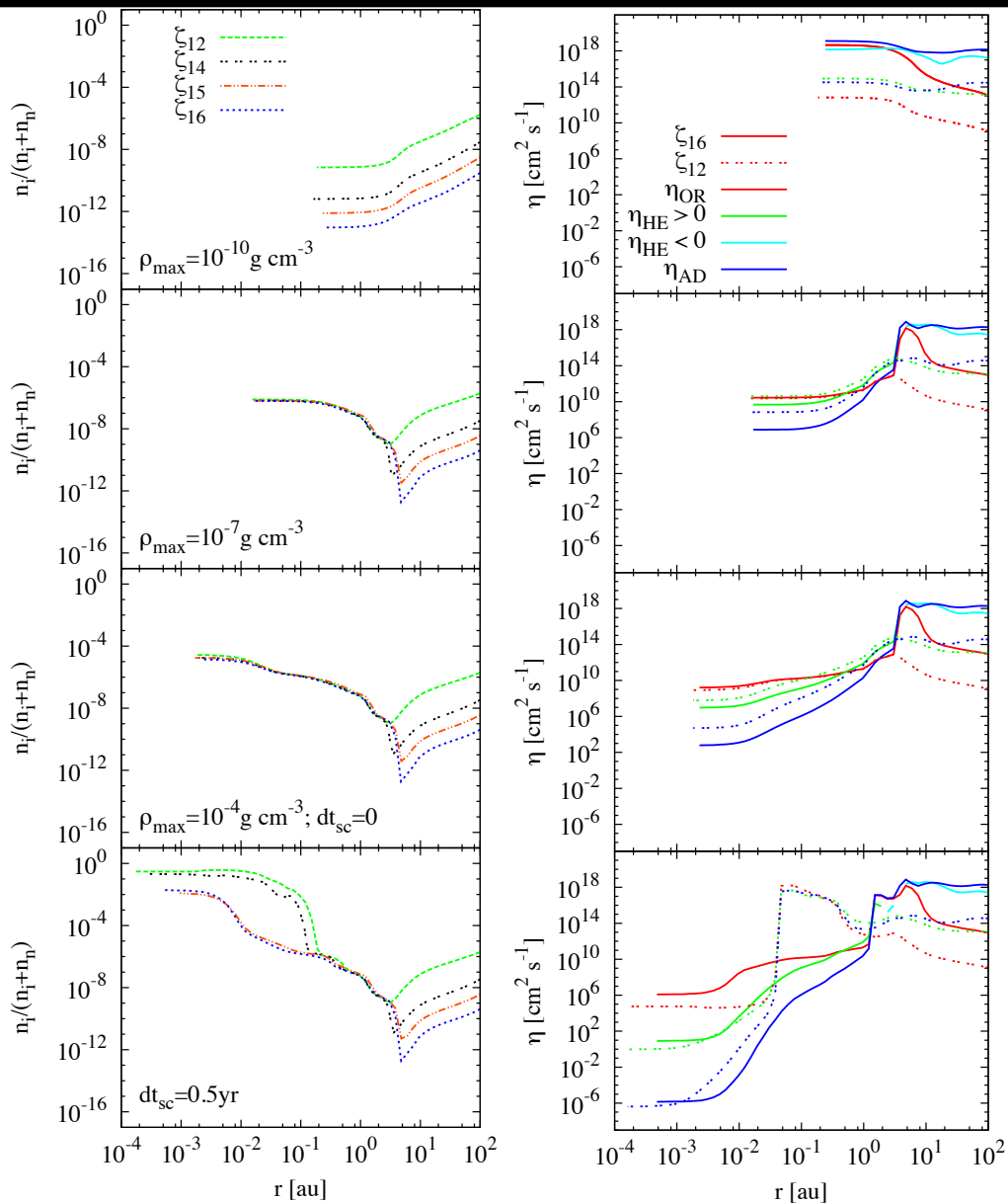
- Includes
  - 5 singly ionised elements
  - 4 doubly ionised elements

$$\left. \frac{dB}{dt} \right|_{OR} = -\nabla \times \eta_{OR} (\nabla \times B),$$

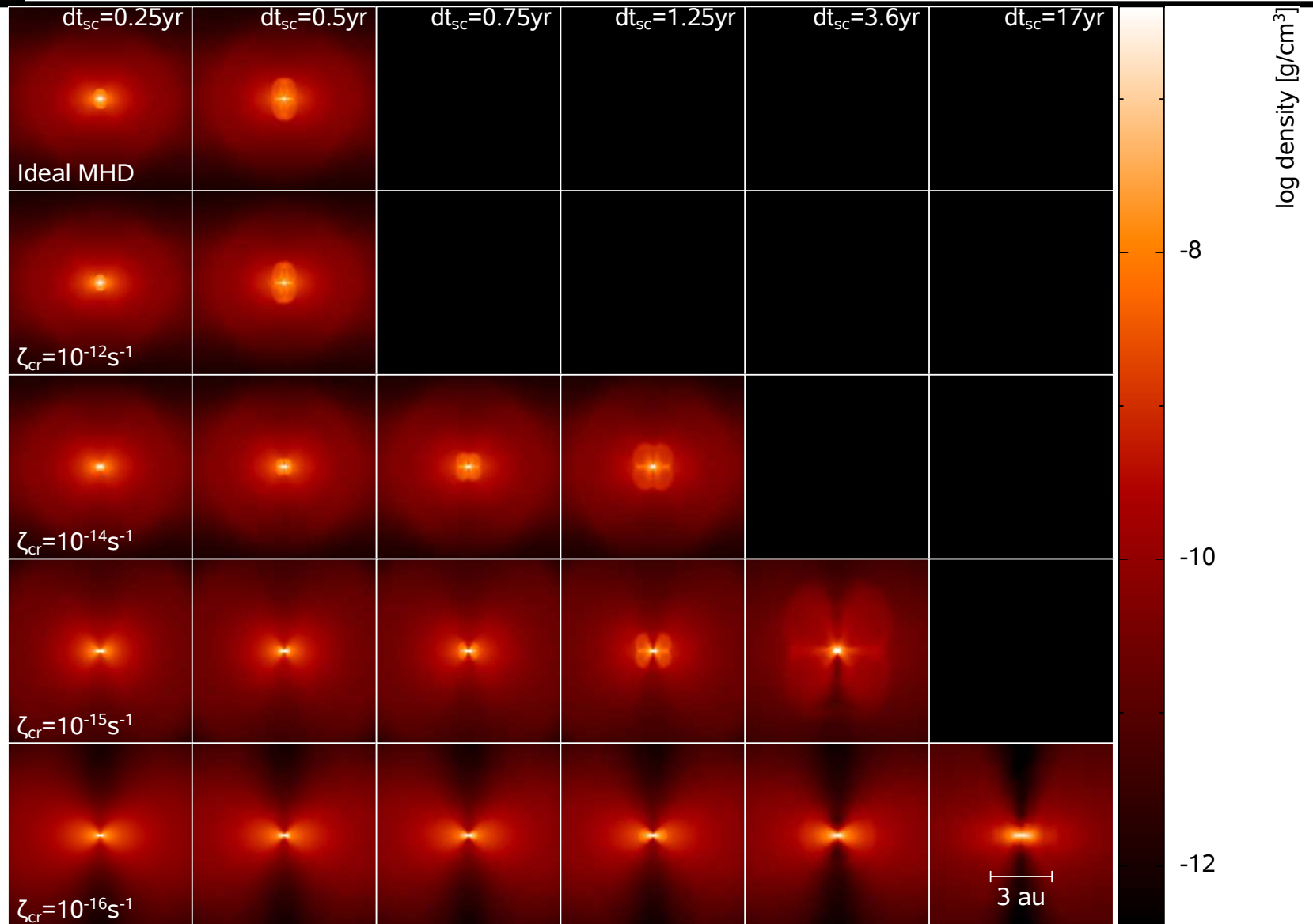
$$\left. \frac{dB}{dt} \right|_{HE} = -\nabla \times \eta_{HE} [(\nabla \times B) \times \hat{B}],$$

$$\left. \frac{dB}{dt} \right|_{AD} = \nabla \times \eta_{AD} \left\{ [(\nabla \times B) \times \hat{B}] \times \hat{B} \right\}.$$

# Collapse to stellar densities

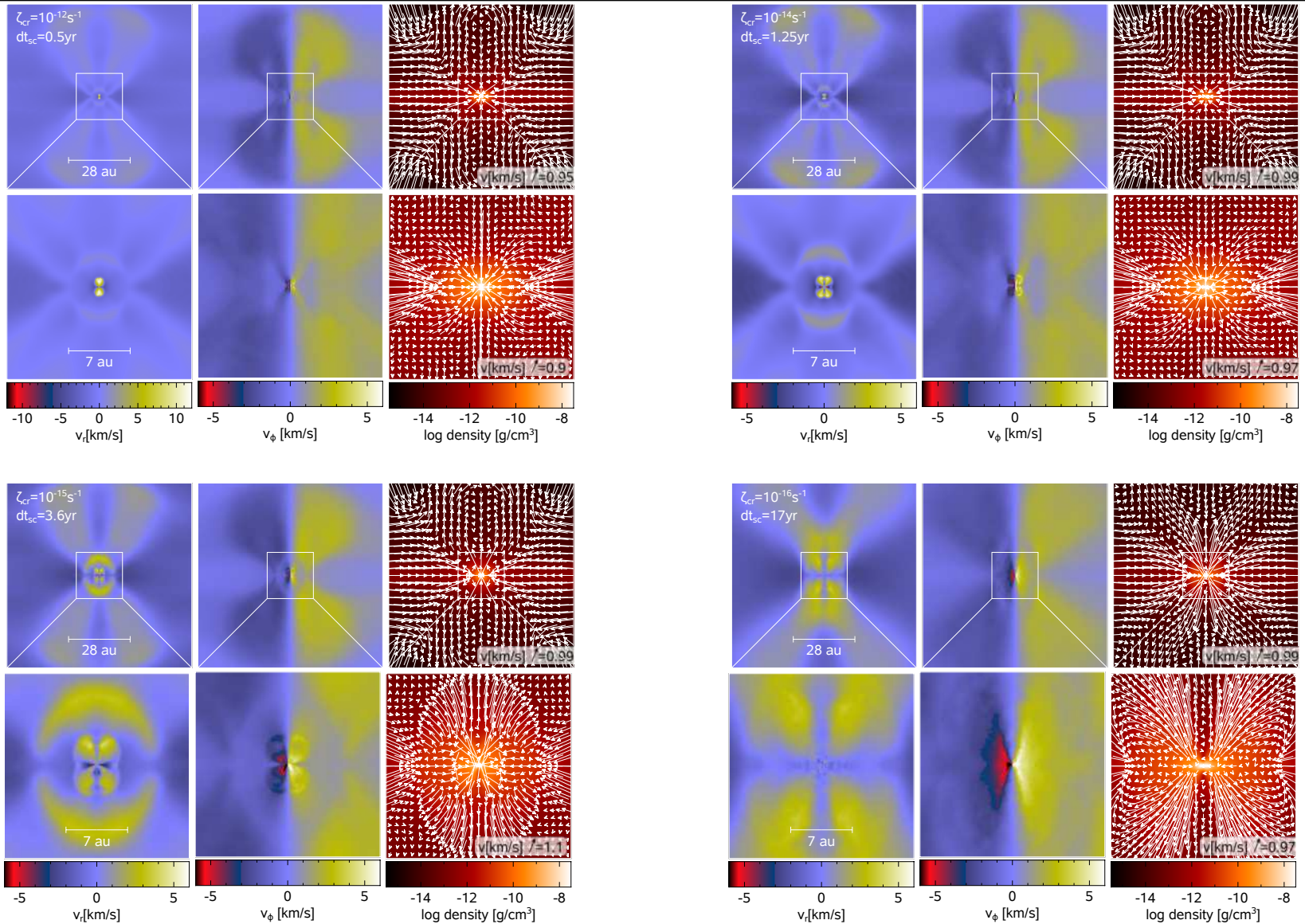


# *Collapse to stellar densities: Stellar core*





# Collapse to stellar densities: Stellar core







# Conclusions

- Large disc forms with no magnetic fields
- No disc forms with strong, ideal magnetic fields
  - Large discs with strong magnetic fields are observed
- Decreasing  $M/\Phi$  decreases mass and size of resulting disc
- Formation of discs and outflows is anti-correlated
- Changing initial magnetic field direction + Hall effect is strongest affect
- Larger discs form with lower ionisation rate
- Hall Effect causes the formation of a counter-rotating envelope
- Non-ideal MHD suppresses first and second core outflows
- This is just the beginning!