

# Protostars and discs: Low-mass star formation in a magnetised medium




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# *Importance of stars: The big picture*



**Stars as energetic events:**  
SN 1994D near NGC 4526  
(apod.nasa.gov)




**Stars as light sources:**  
Whirlpool Galaxy (M51; nasa.gov)



**Stars as energetic events:** Wolf-Rayet Star 124 (apod.nasa.gov)



**Stars hosting planetary systems:**  
HL Tau dust disc (ALMA Partnership, 2015)

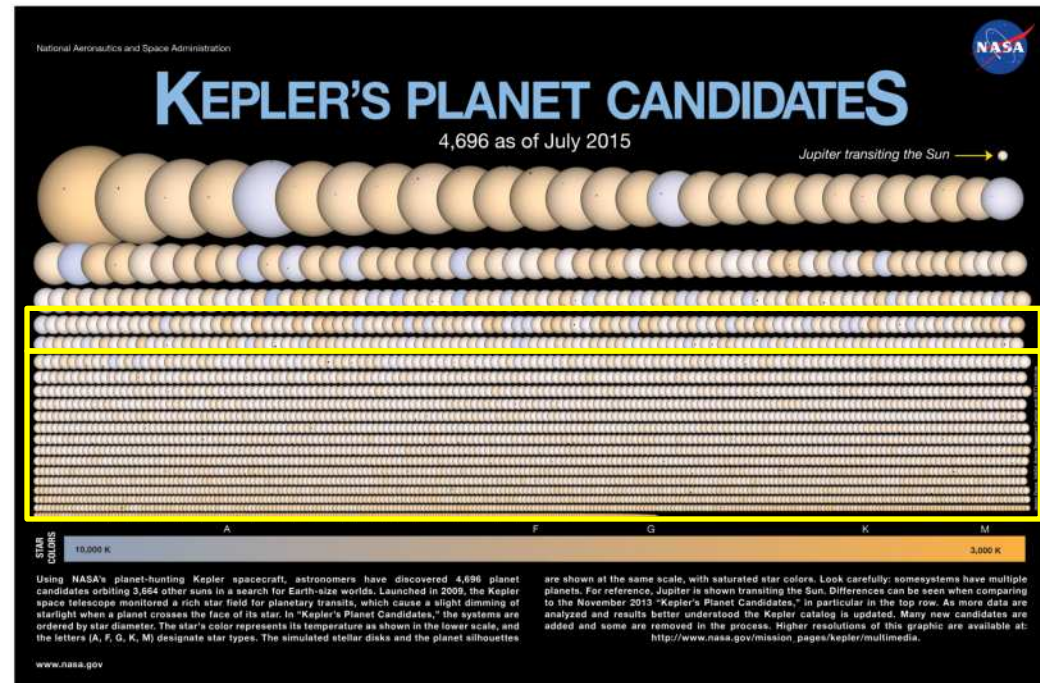
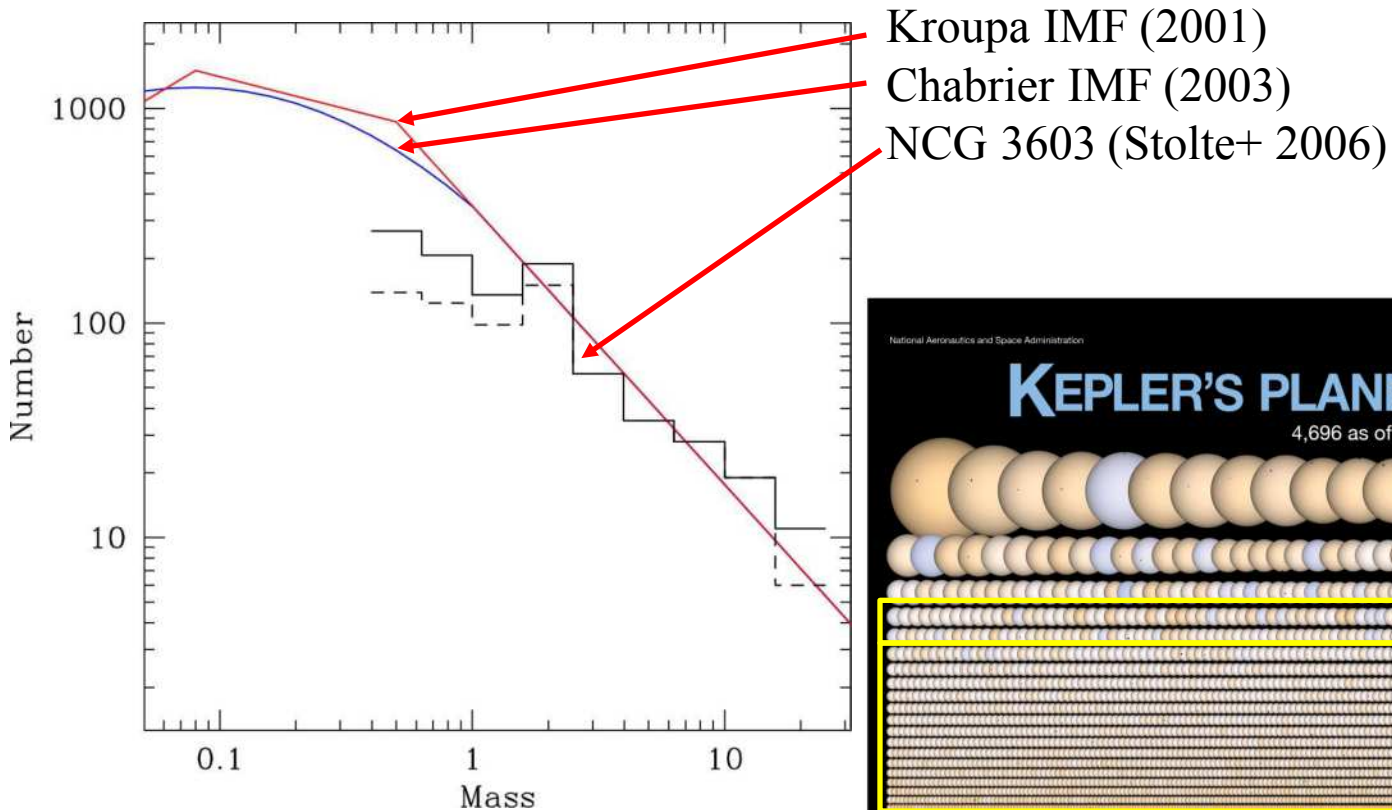


**Stars launching jets:** Large scale HH jet driven by a protobrown dwarf (Riaz et. al., 2017)

**Stars as light sources:** Hubble Ultra Deep Field (nasa.gov)

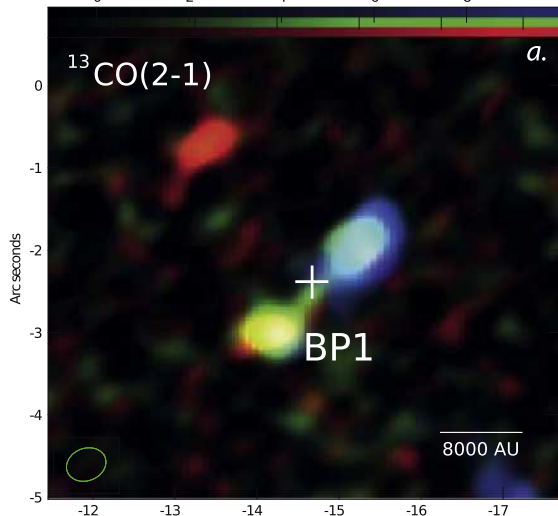
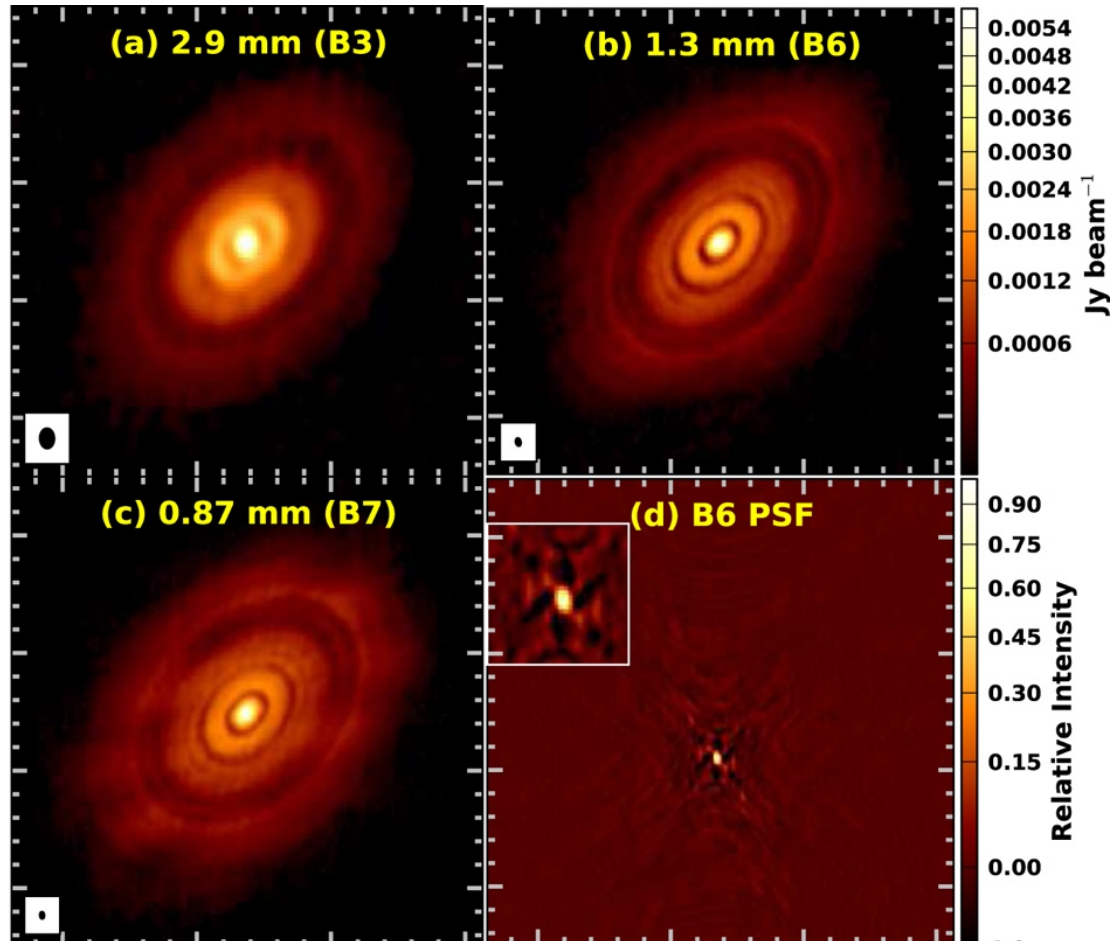
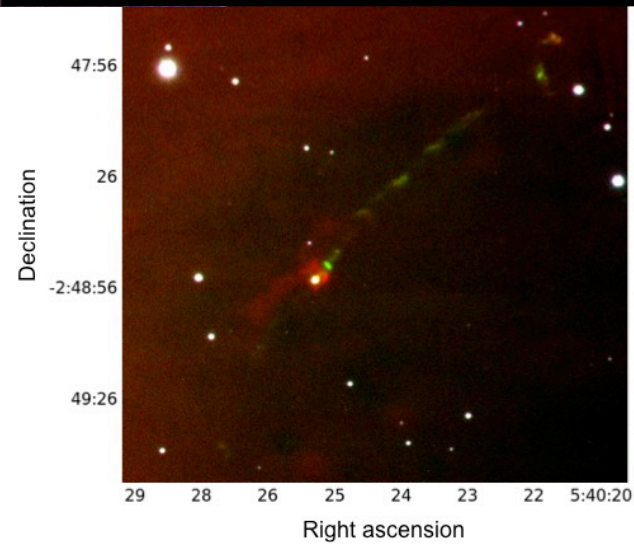
# Importance of stars: Masses

## ➤ Initial mass function (IMF) of NCG 3603



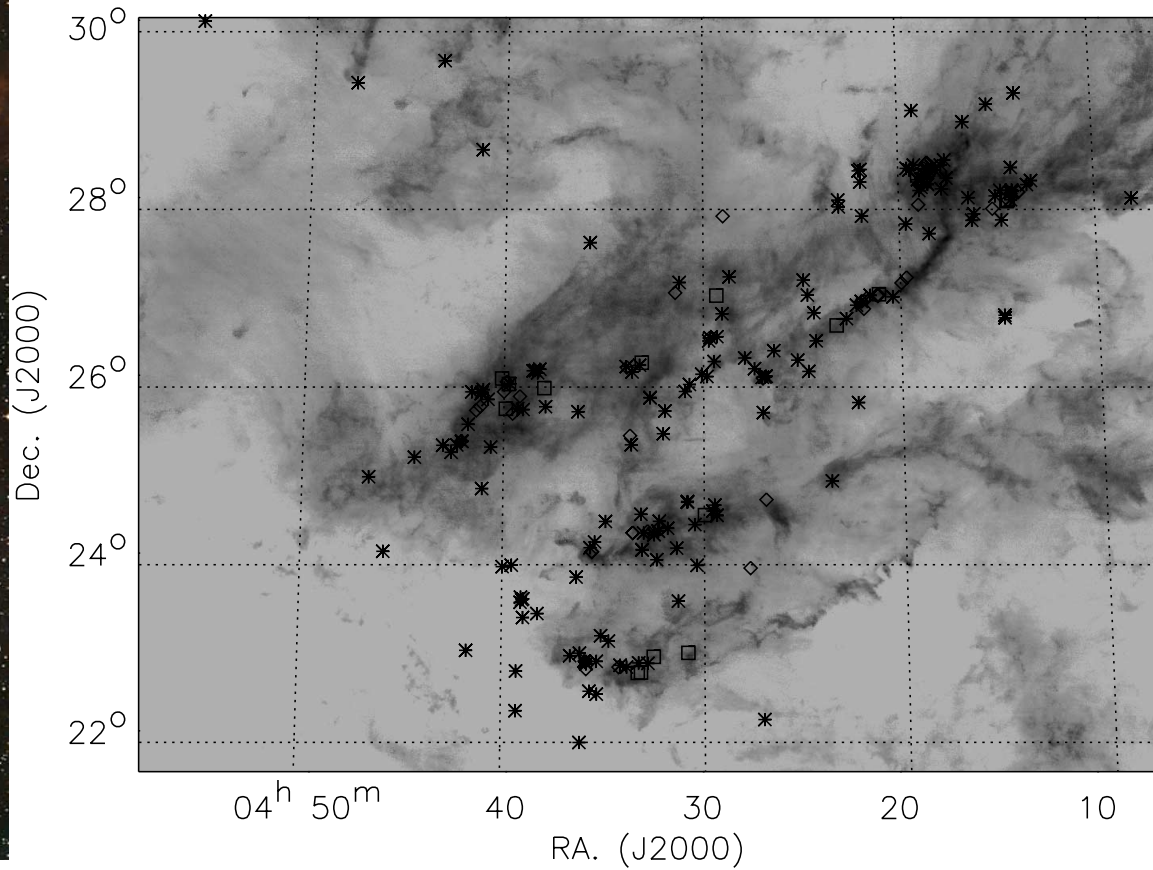
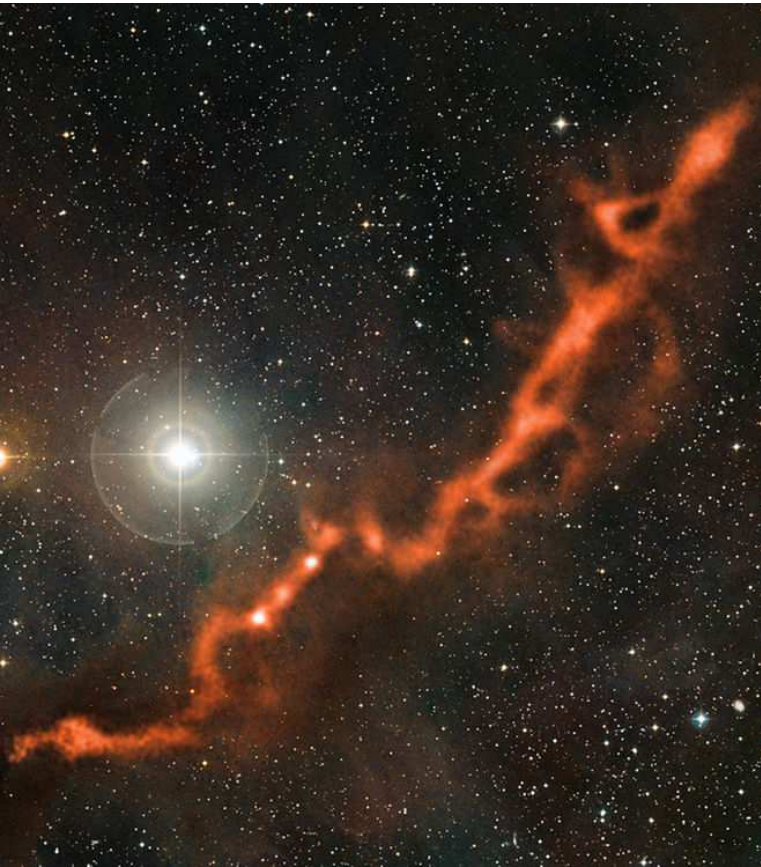


# Importance of Low-stars: Outflows & Discs



Top left: Large scale Herbig-Haro jet driven by a proto-brown dwarf (Riaz et. al., 2017)  
Bottom left: CO outflows from low-mass stars with 1pc of Sgr A\* (Yusef-Zadeh et. al., 2017)  
Right: HL Tau dust disc (ALMA Partnership, 2015)

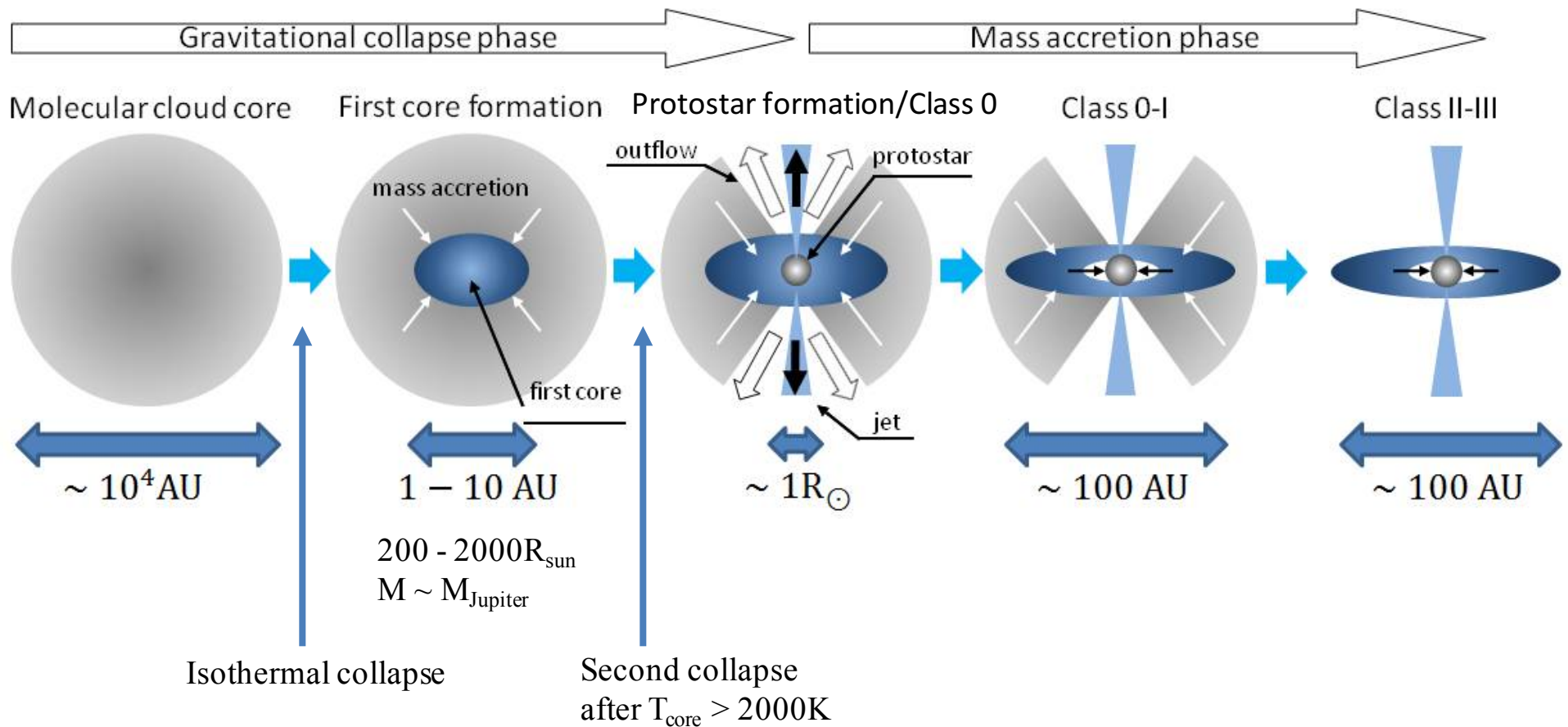
# *Importance of stars: Stellar nurseries*



Taurus Molecular Cloud  
(Credit: ESO/APEX (MPIfR/ESO/OSO)/A. Hacar  
et al./Digitized Sky Survey 2.  
Acknowledgment: Davide De Martin)

Taurus Molecular Cloud: H<sub>2</sub> column density map with  
positions of young stars (Goldsmith et. al., 2008)

# Star formation: from the beginning



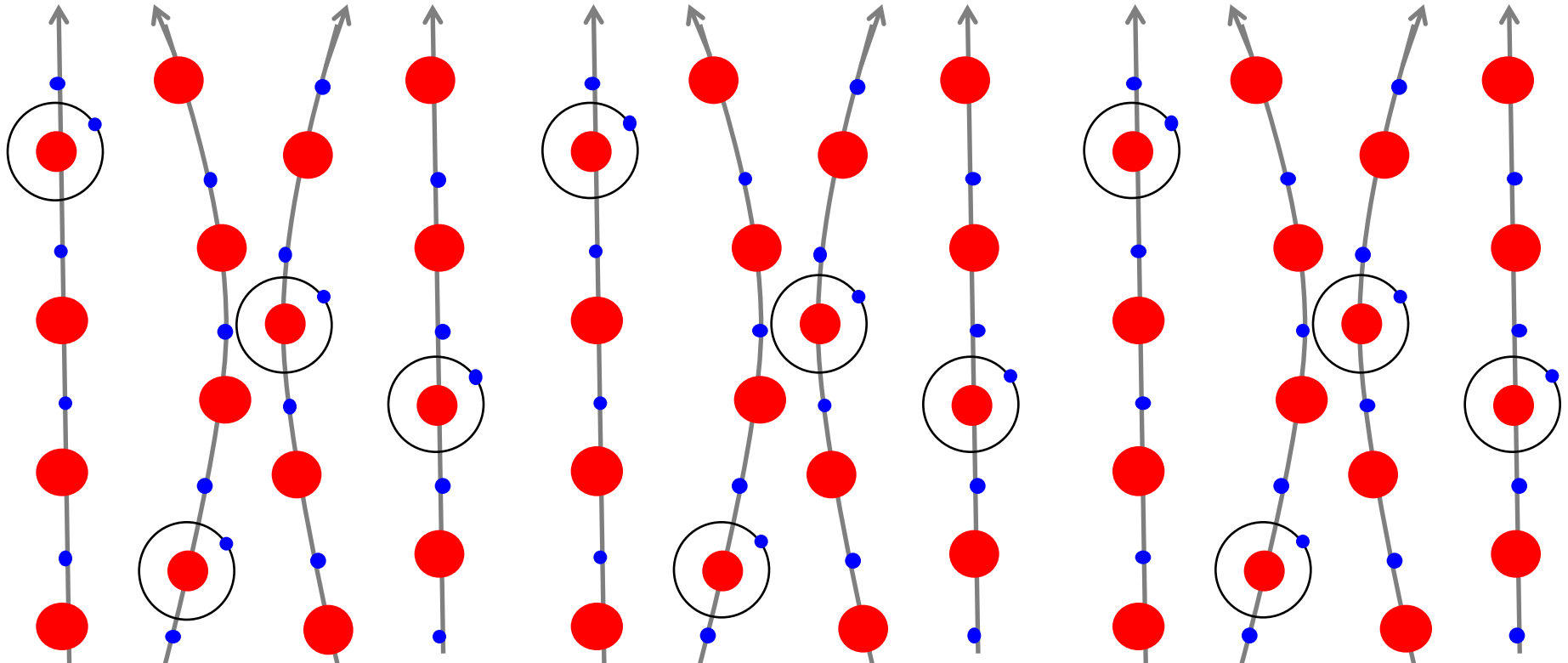
# *Ideal magnetic fields*

➤ Highly ionised plasma: ● + ●

➤ Zero resistivity & infinite conductivity

➤ Ions & electrons are tied to the magnetic field

➤ Neutral particles are tied to the magnetic field due to interactions with the ions & electrons



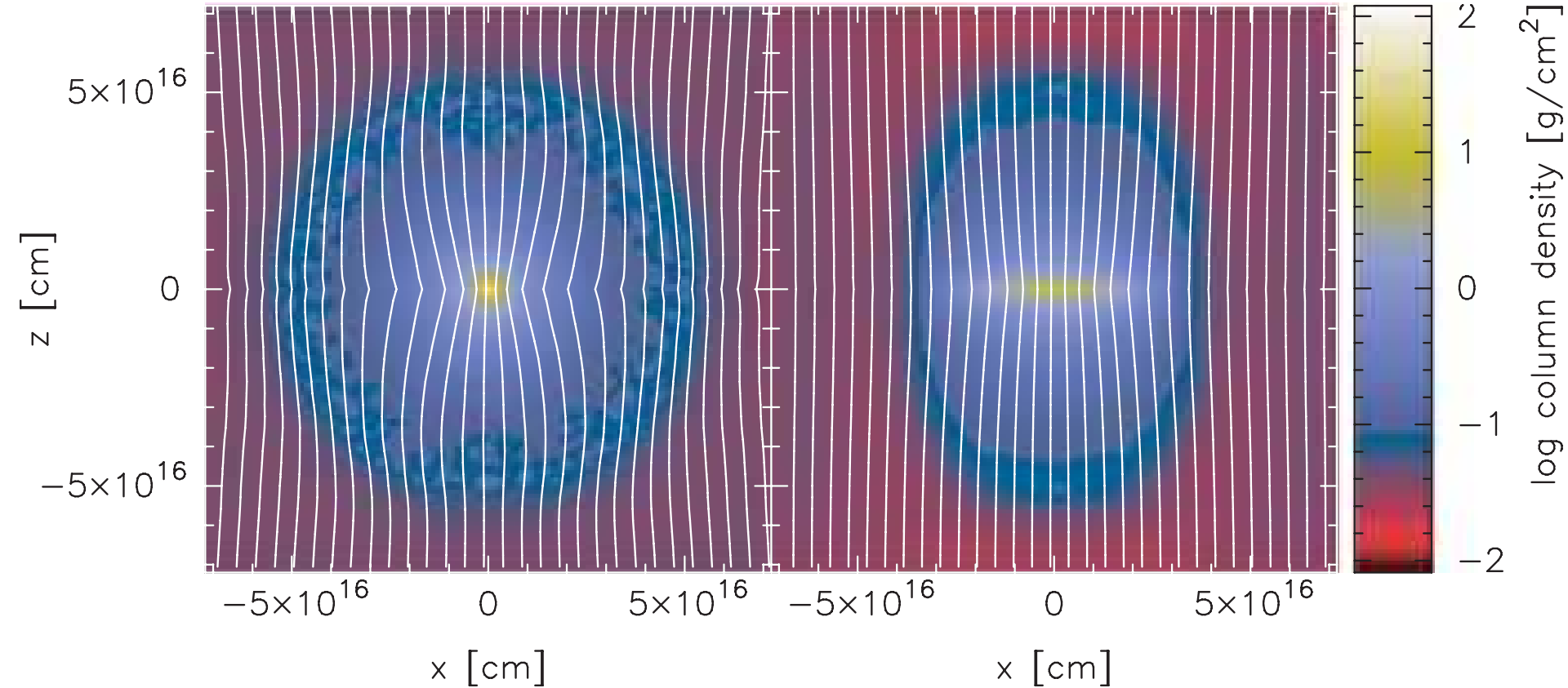


# *Star formation: with magnetic fields*



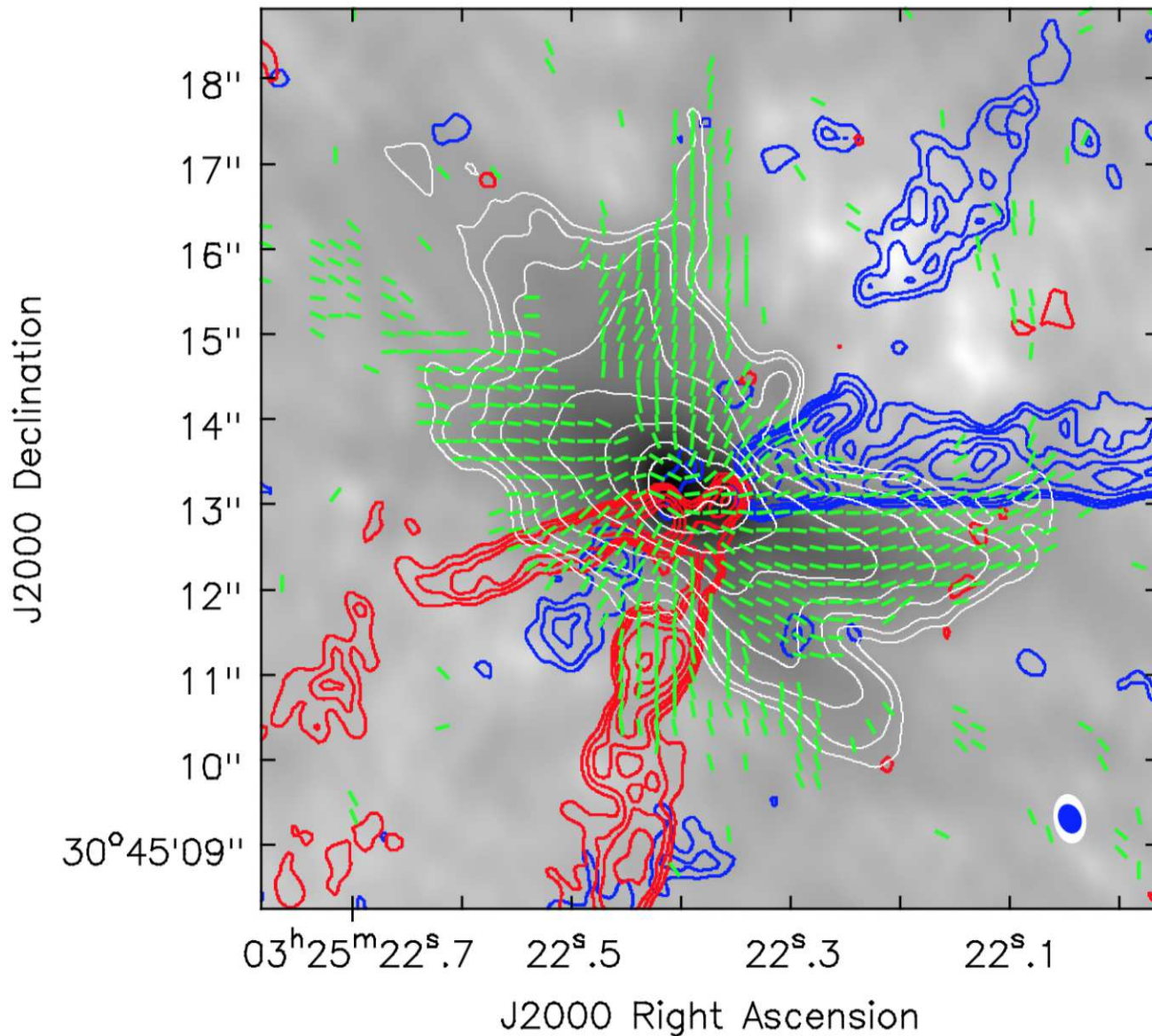
$\mu_0 = 100$  (weak field)

$\mu_0 = 3$  (strong field)



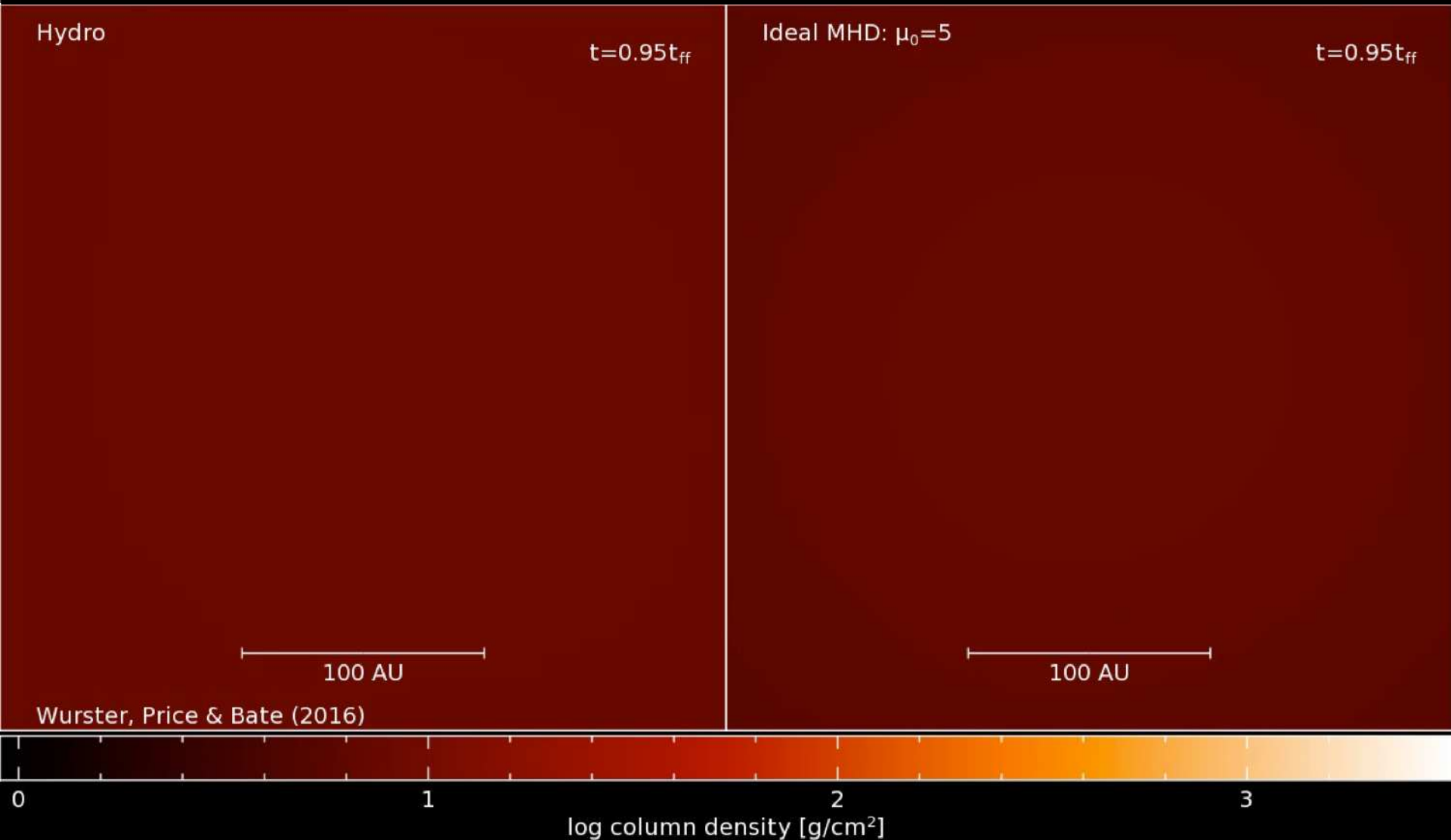


# *Star formation: with magnetic fields*




# *Disc formation:*

# *Hydrodynamics vs Magnetohydrodynamics*



Video Available at:

<https://youtu.be/WqfqYRUsYuQ?list=PLwI7am9c6sBi3yBP0Yp-8qMK414H5OPph>



*Disc formation:  
Magnetohydrodynamics*

***The Magnetic Braking Catastrophe:***

discs do not form in numerical simulations  
containing strong, ideal magnetic fields

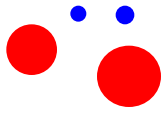


No magnetic field




Strong magnetic field





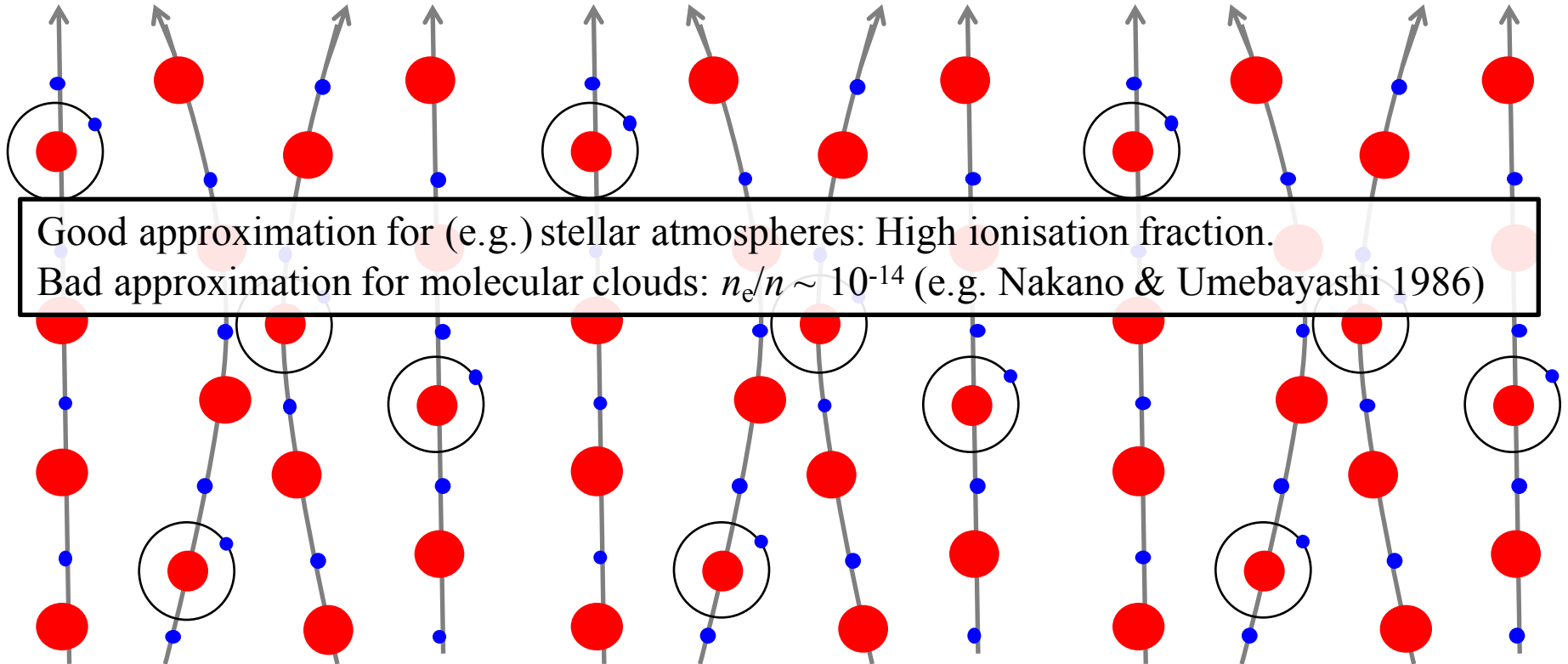
# *Ideal magnetohydrodynamics*

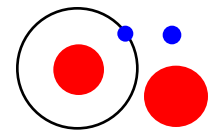
➤ Highly ionised plasma: 

➤ Zero resistivity & infinite conductivity

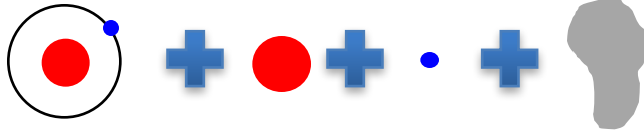
➤ Ions & electrons are tied to the magnetic field

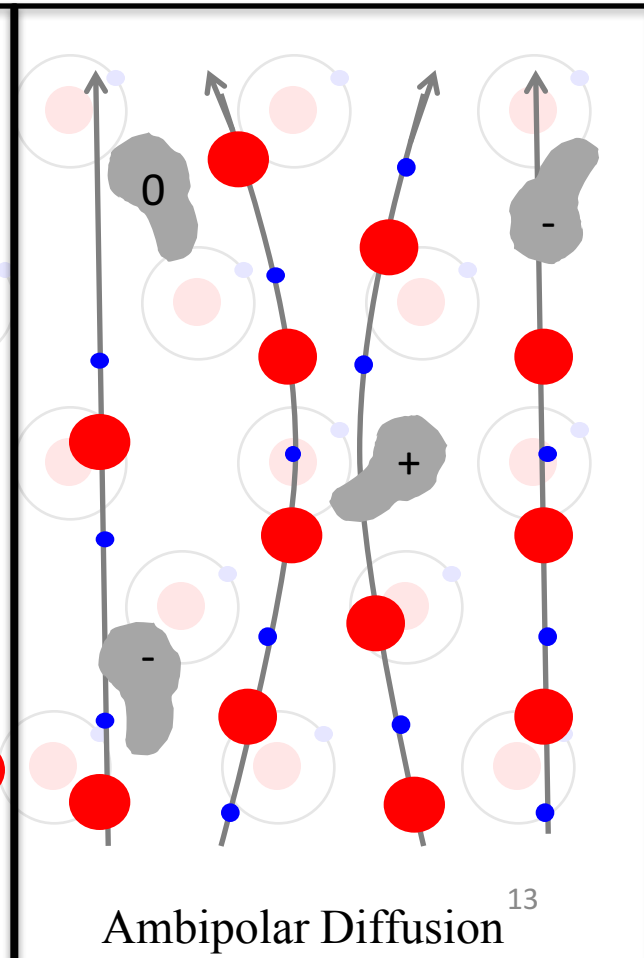
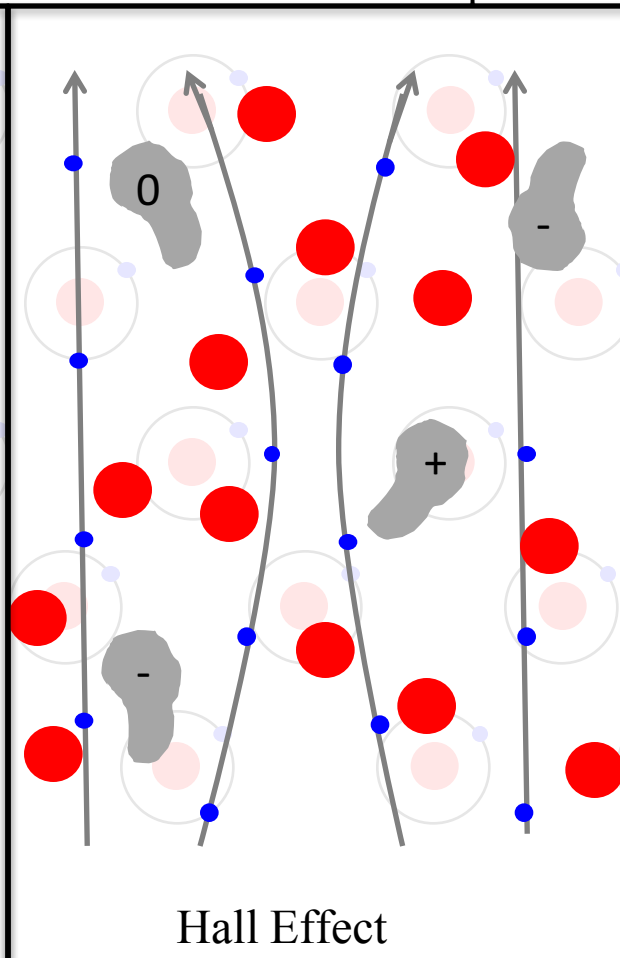
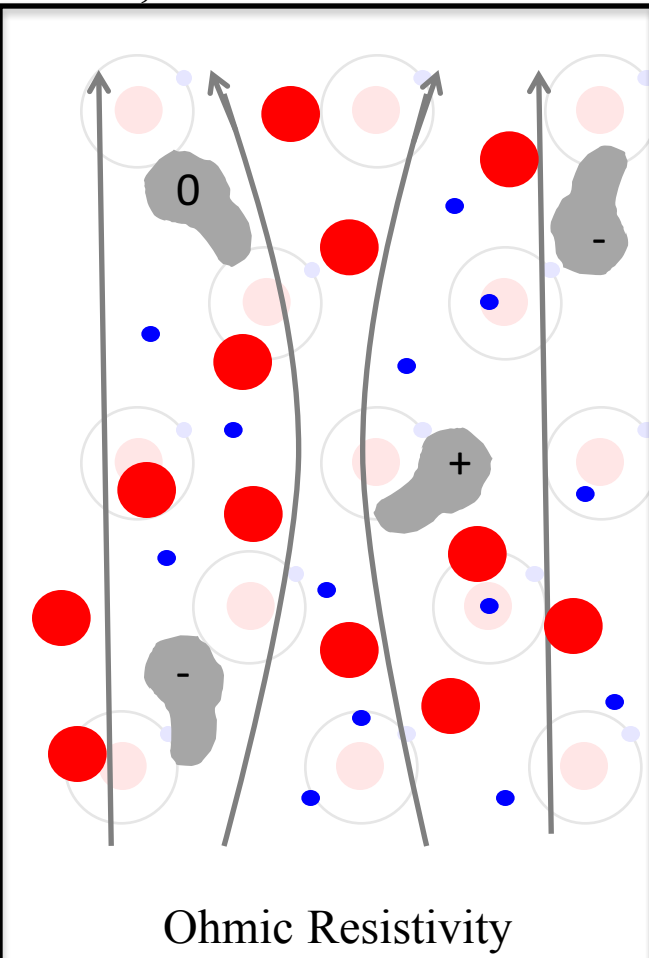
➤ Neutral particles are tied to the magnetic field due to interactions with the ions & electrons

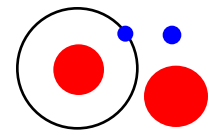




# *Non-ideal magnetohydrodynamics*

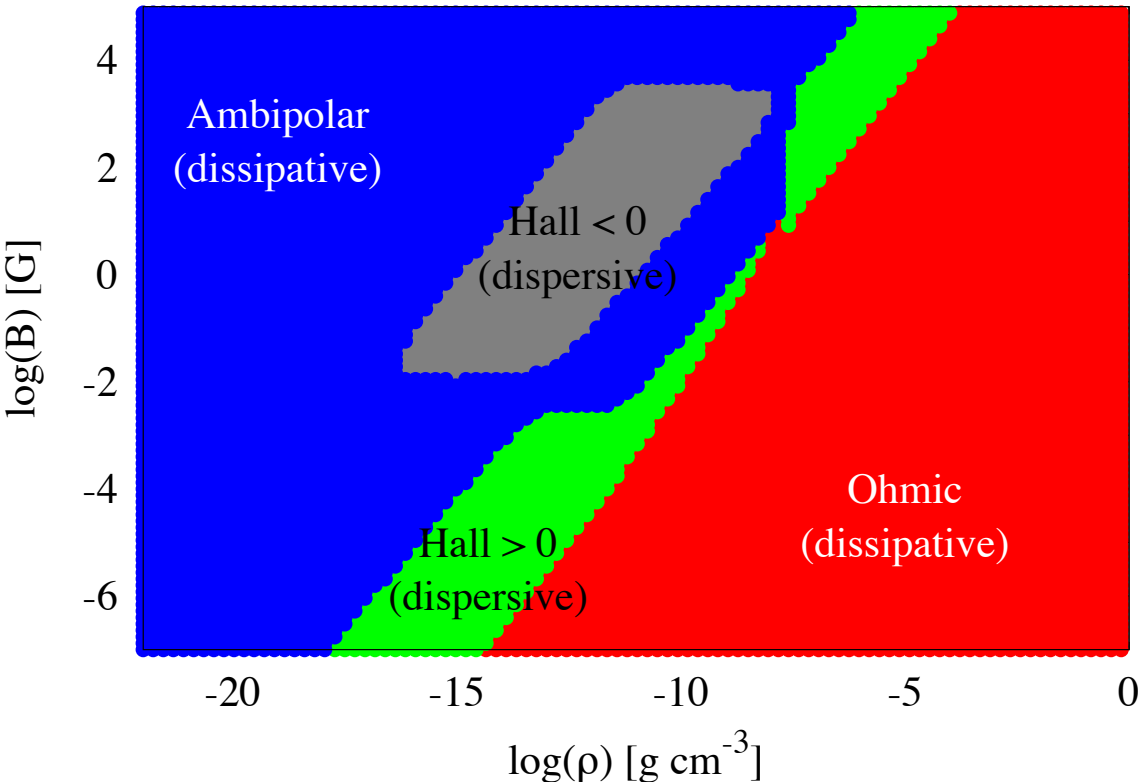
- Partially ionised plasma and dust: 
  - Non-zero resistivity & conductivity
  - Ions, electrons & neutrals behaviour is environment-dependent
- $\xrightarrow{B}$   
 $\rho$   
 $\xleftarrow{\quad}$



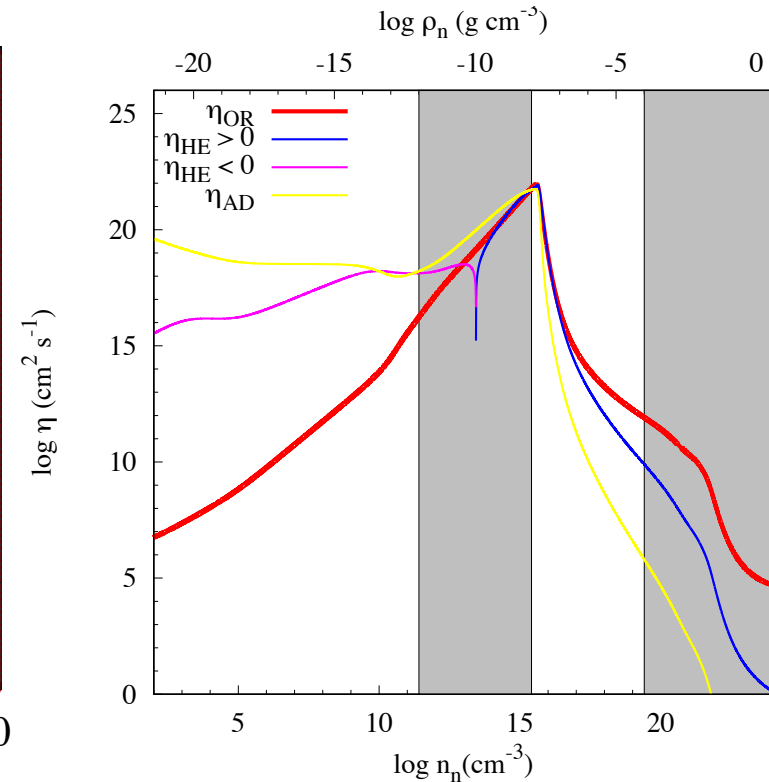


# Non-ideal magnetohydrodynamics

Phase space diagram



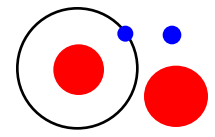
Coefficients  
(for a star-forming model)



➤ Values dependent on microphysics:

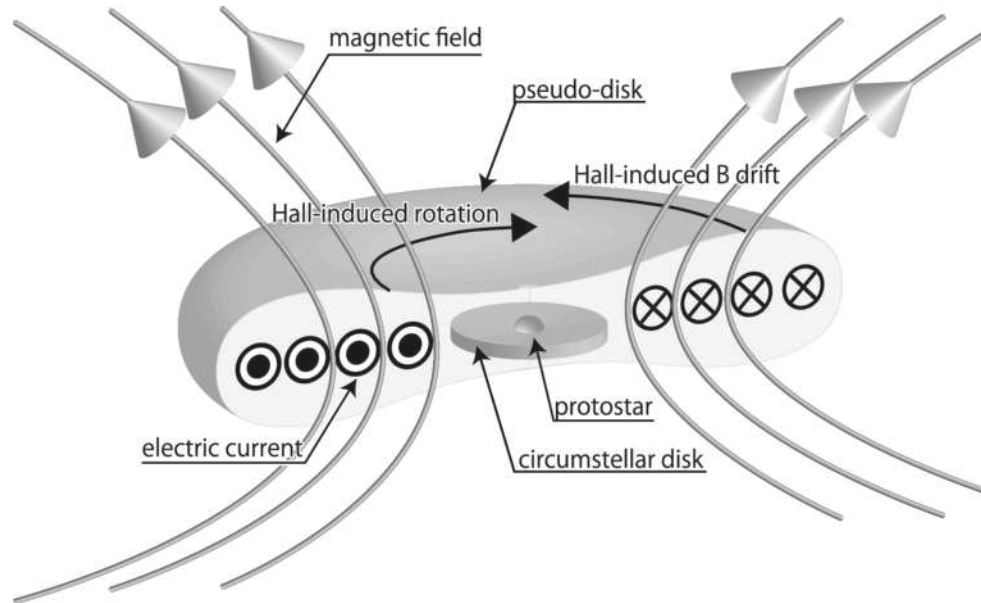
➤ Grain size, ionised species, cosmic ray ionisation rate





# Non-ideal magnetohydrodynamics: The Hall effect

➤ Image assumes  $\eta_{\text{HE}} < 0$  (reasonable for star formation; Wurster 2016; Marchand + 2016)



$$\left. \frac{d\mathbf{B}}{dt} \right|_{\text{OR}} = -\nabla \times [\eta_{\text{OR}} (\nabla \times \mathbf{B})]$$

$$\left. \frac{d\mathbf{B}}{dt} \right|_{\text{HE}} = -\nabla \times [\eta_{\text{HE}} (\nabla \times \mathbf{B}) \times \hat{\mathbf{B}}]$$

$$\left. \frac{d\mathbf{B}}{dt} \right|_{\text{AD}} = \nabla \times \left\{ \eta_{\text{AD}} [(\nabla \times \mathbf{B}) \times \hat{\mathbf{B}}] \times \hat{\mathbf{B}} \right\}$$

For magnetic field reversal, substitute  $\mathbf{B} \rightarrow -\mathbf{B}$ :

$$\left. \frac{d(-\mathbf{B})}{dt} \right|_{\text{OR}} = -\nabla \times \{ \eta_{\text{OR}} [\nabla \times (-\mathbf{B})] \}$$

$$\left. \frac{d(-\mathbf{B})}{dt} \right|_{\text{HE}} = -\nabla \times \left\{ \eta_{\text{HE}} [\nabla \times (-\mathbf{B})] \times (-\hat{\mathbf{B}}) \right\}$$

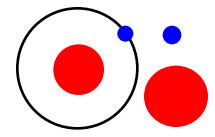
$$\left. \frac{d(-\mathbf{B})}{dt} \right|_{\text{AD}} = \nabla \times \left\{ \eta_{\text{AD}} \left[ [\nabla \times (-\mathbf{B})] \times (-\hat{\mathbf{B}}) \right] \times (-\hat{\mathbf{B}}) \right\}$$

Simplify:

$$\left. \frac{d\mathbf{B}}{dt} \right|_{\text{OR}} = -\nabla \times [\eta_{\text{OR}} (\nabla \times \mathbf{B})]$$

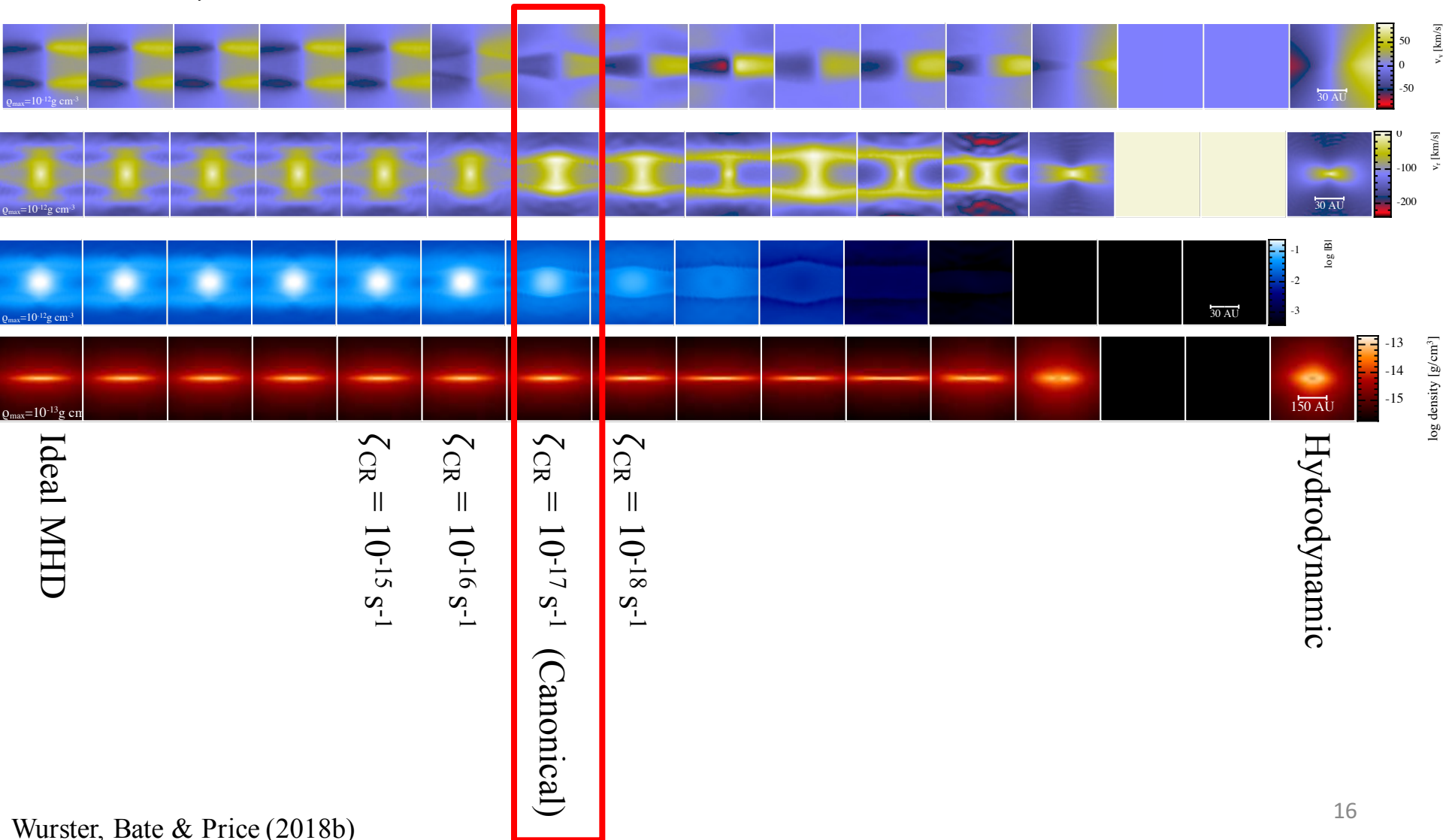
$$\left. \frac{d\mathbf{B}}{dt} \right|_{\text{HE}} = \nabla \times [\eta_{\text{HE}} (\nabla \times \mathbf{B}) \times \hat{\mathbf{B}}]$$

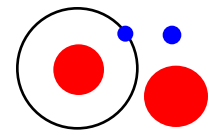
$$\left. \frac{d\mathbf{B}}{dt} \right|_{\text{AD}} = \nabla \times \left\{ \eta_{\text{AD}} [(\nabla \times \mathbf{B}) \times \hat{\mathbf{B}}] \times \hat{\mathbf{B}} \right\}$$



# Cosmic ray ionisation rate

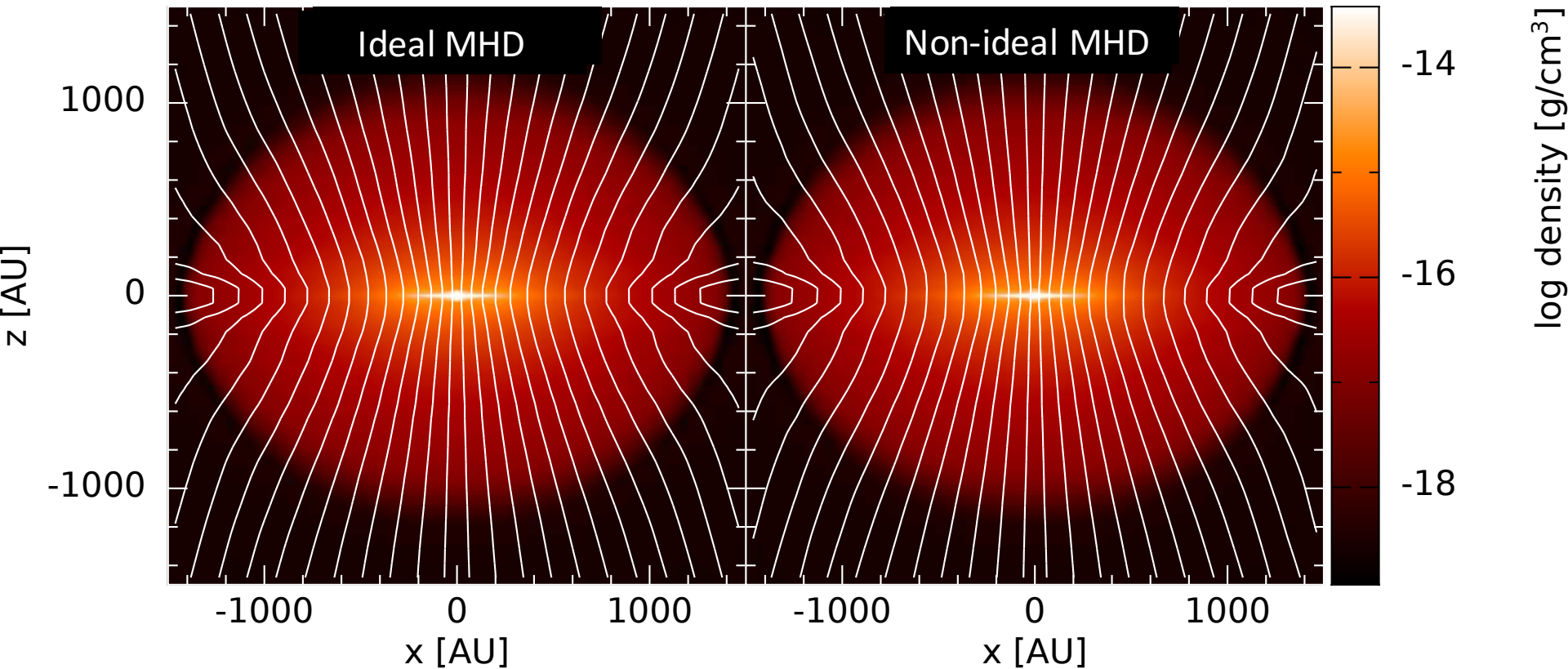
➤ Images:  $v_y$ ,  $v_r$ ,  $\log(B)$ ,  $\log(\rho)$  at  $\rho_{\max} = 10^{-12} \text{ g cm}^{-3}$



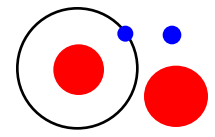


# *Non-ideal magnetohydrodynamics*

- Strong field; large scale structure

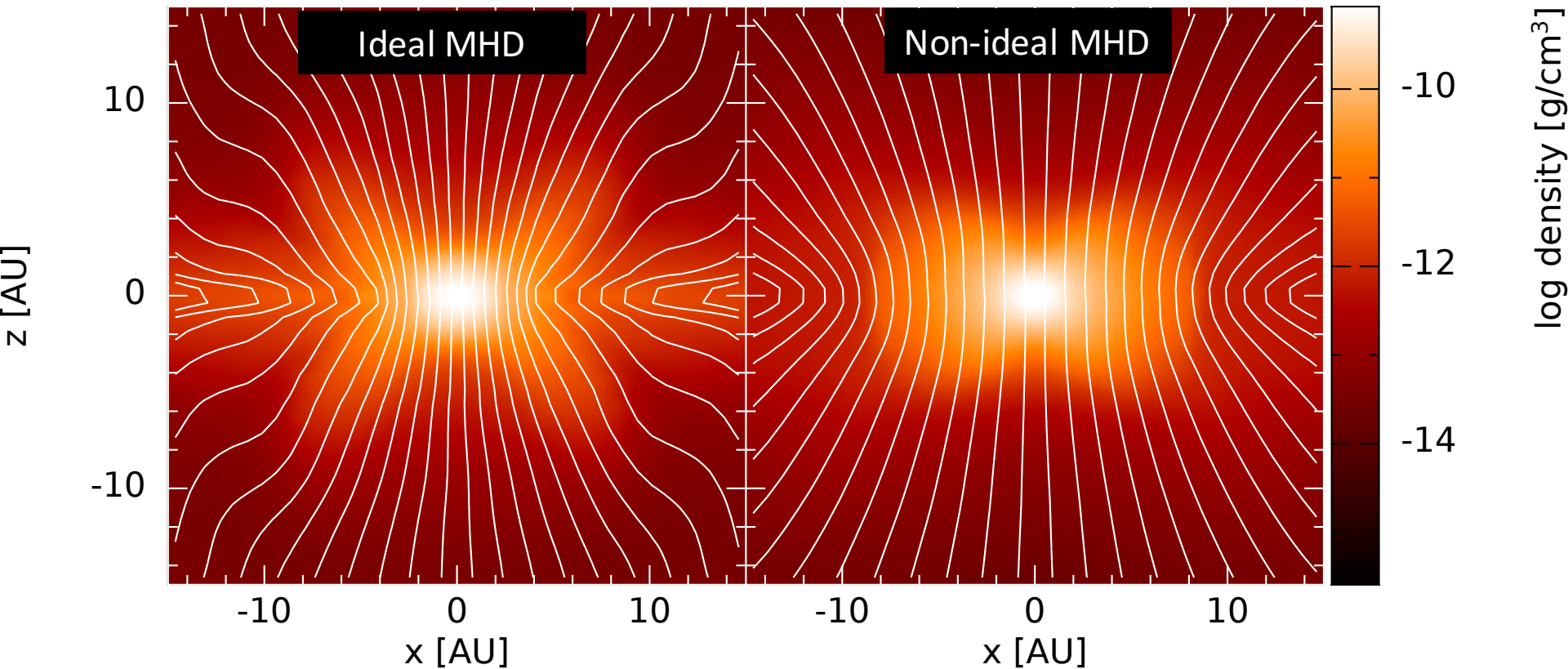


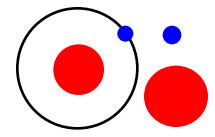




# *Non-ideal magnetohydrodynamics*

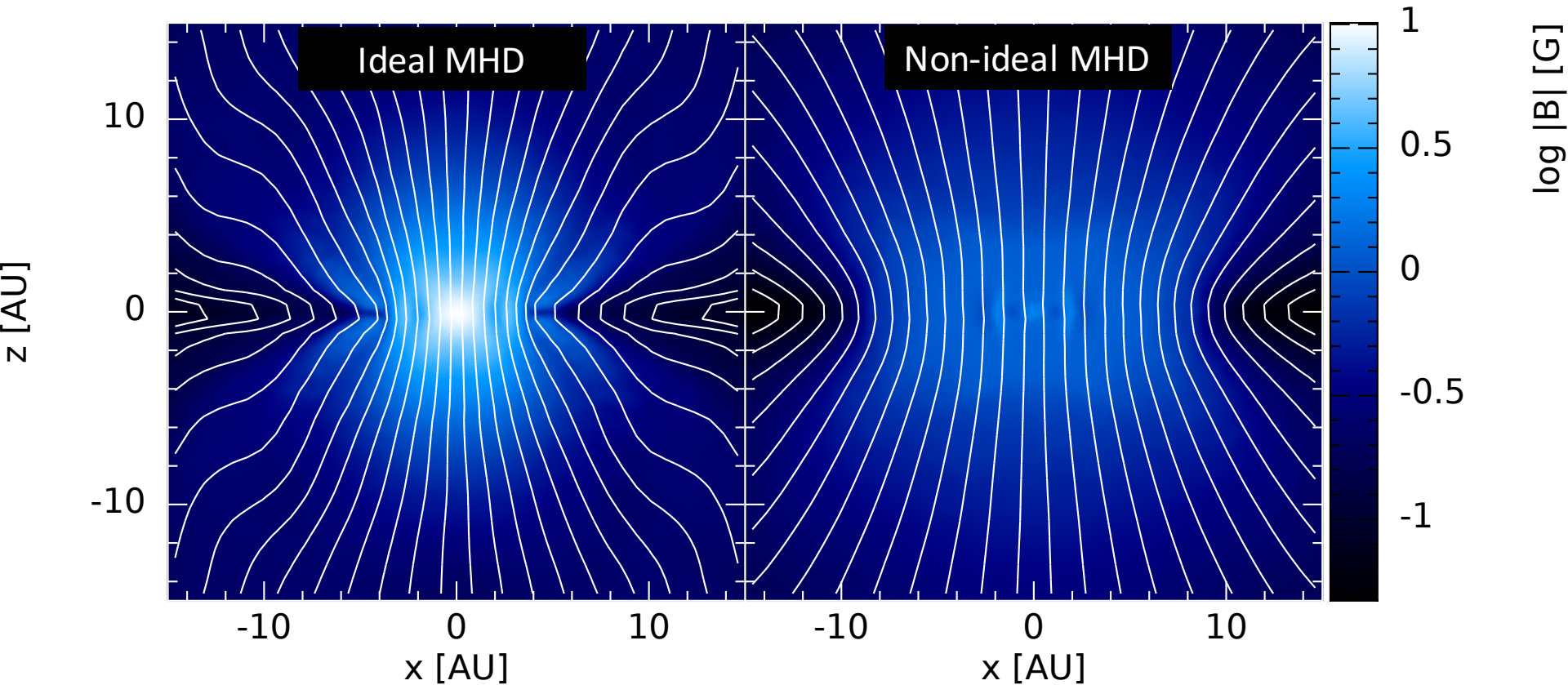
- Strong field; small scale structure



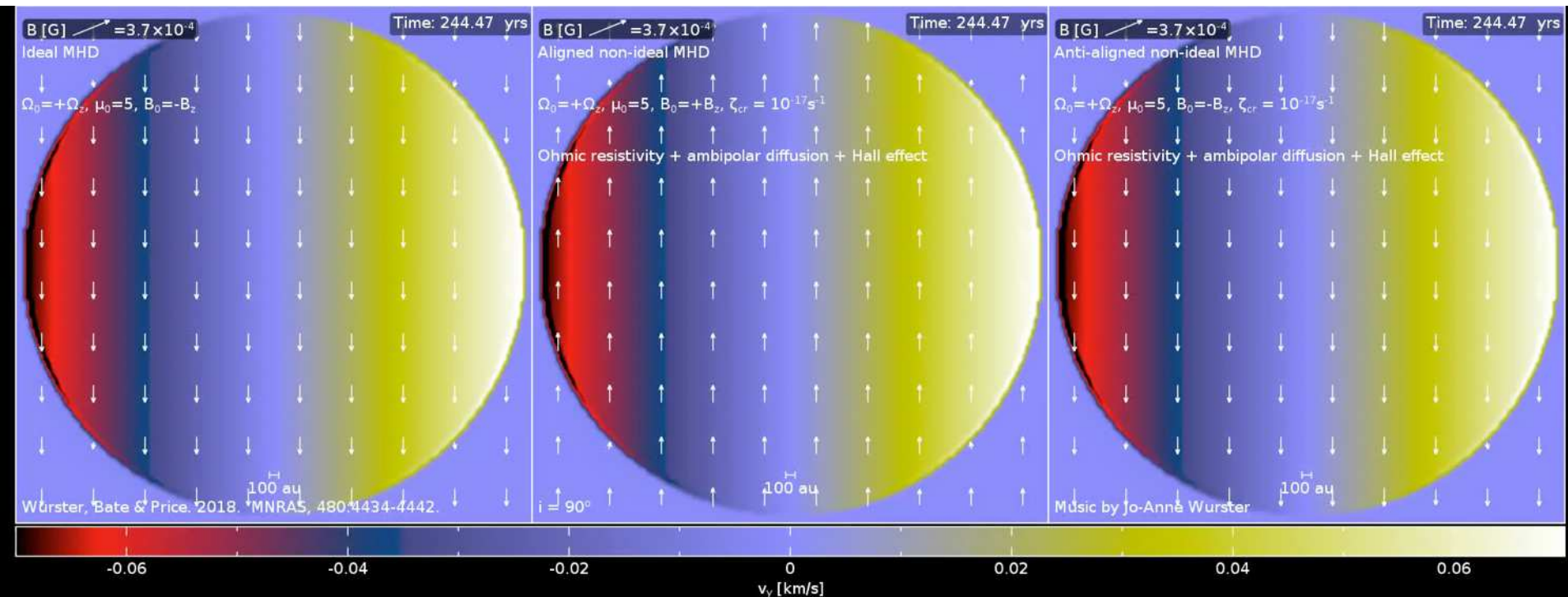


# *Non-ideal magnetohydrodynamics*

- Strong field; small scale structure



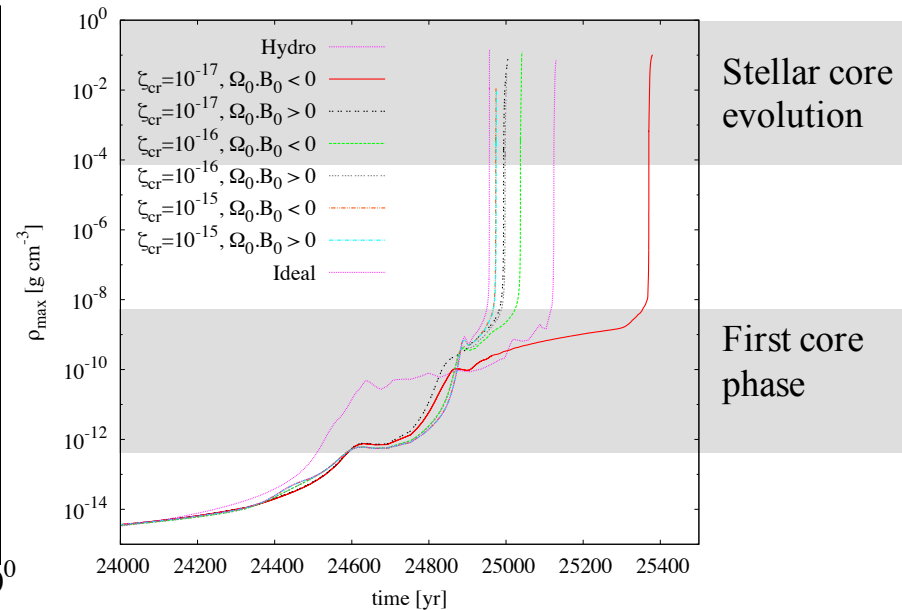
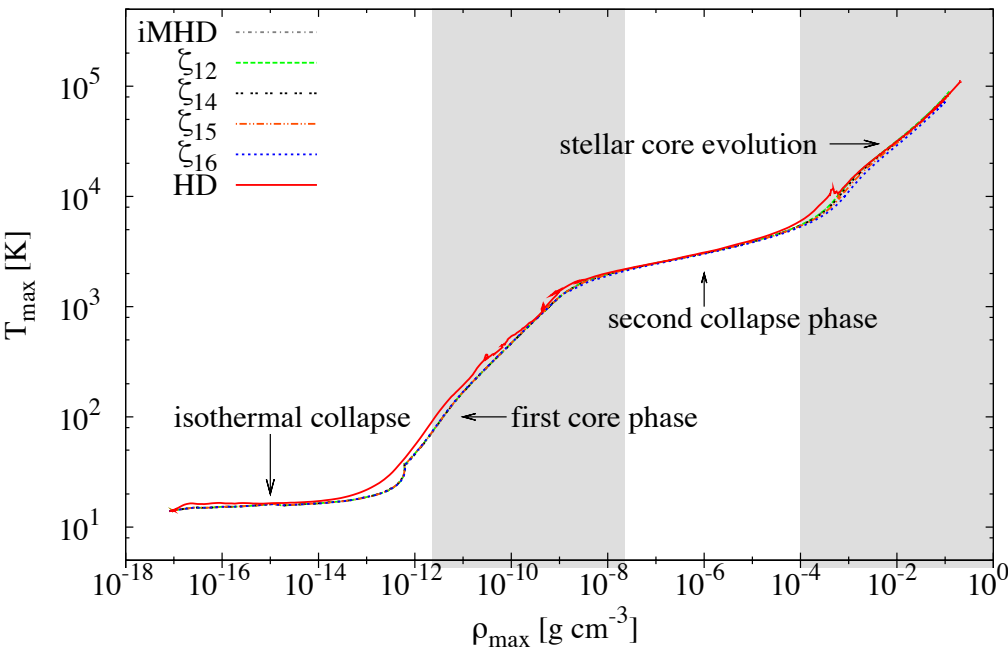
# Formation of a low-mass star



➤ Video available at  
<https://youtu.be/2SQxgXbdJyg?list=PLwI7am9c6sBhhofuWPomUvqu9asfkKwCf>

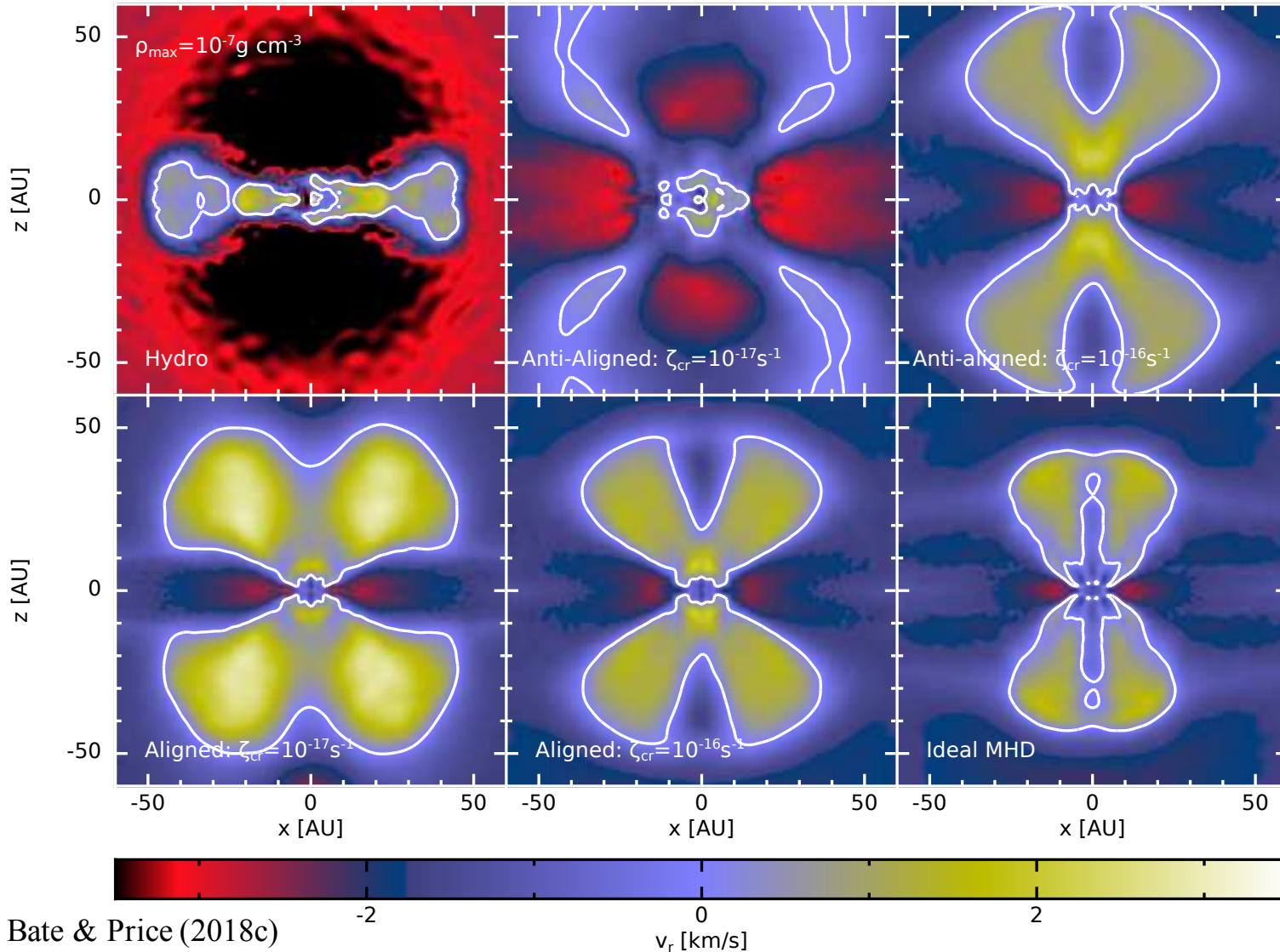
# Collapse to stellar densities: Evolution

- Temperature evolution is independent of ionisation rates
- Time evolution is dependent on ionisation rates & magnetic field orientation



# First core outflows

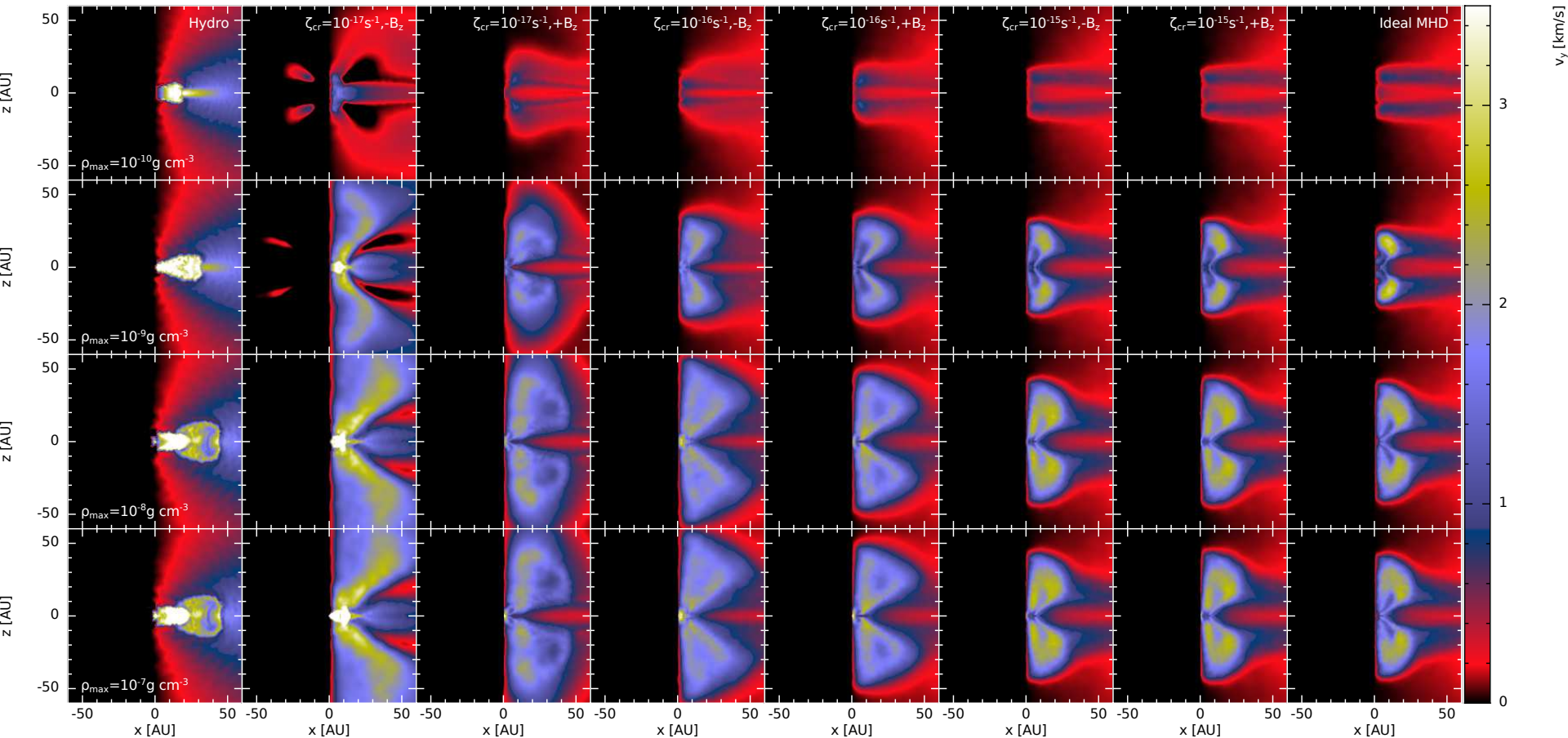
- Aligned magnetic fields enhance outflows; Anti-aligned magnetic fields suppress outflows





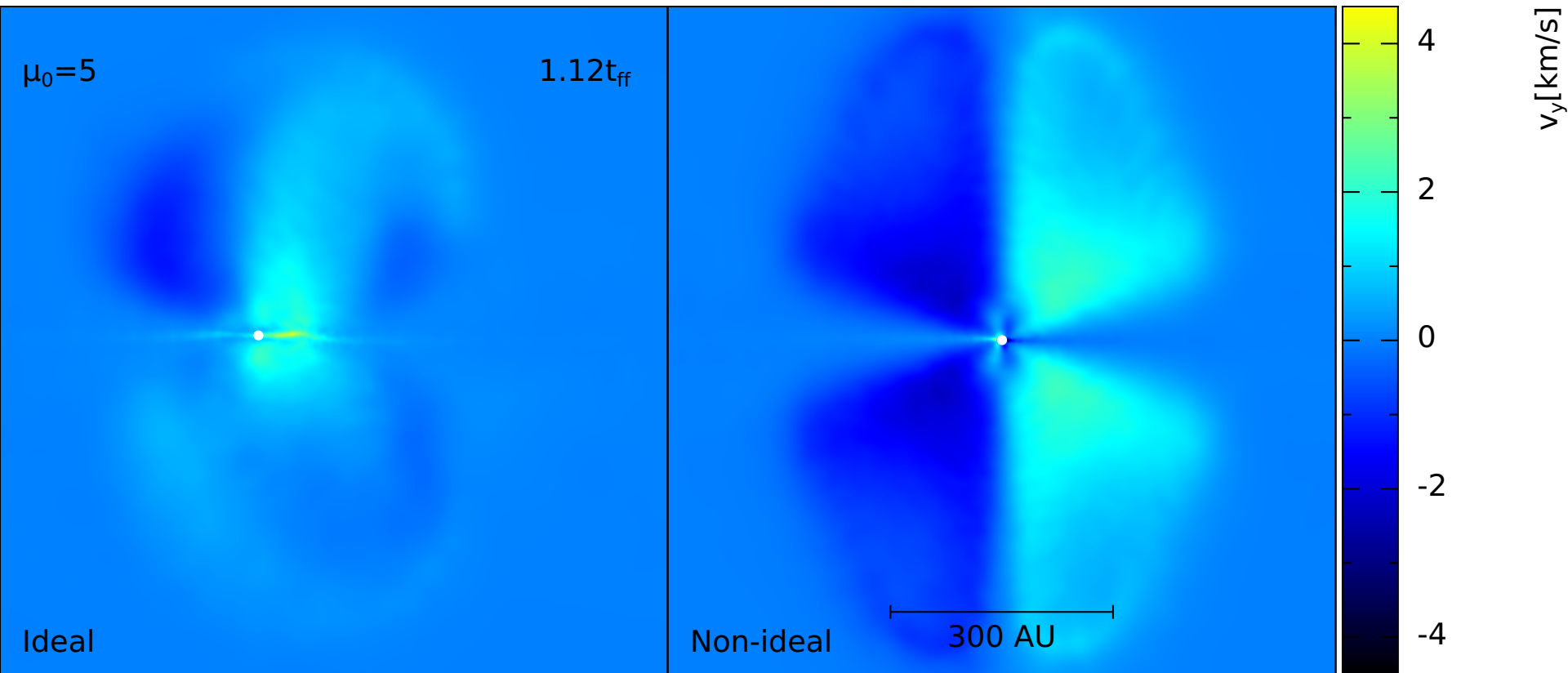
# Large scale rotational velocity

- Rotational speed increases as ionisation rate decreases
- Counter-rotating envelopes are a transient feature in the model with  $\zeta_{\text{cr}} = 10^{-17} \text{ s}^{-1}$  with  $-B_z$



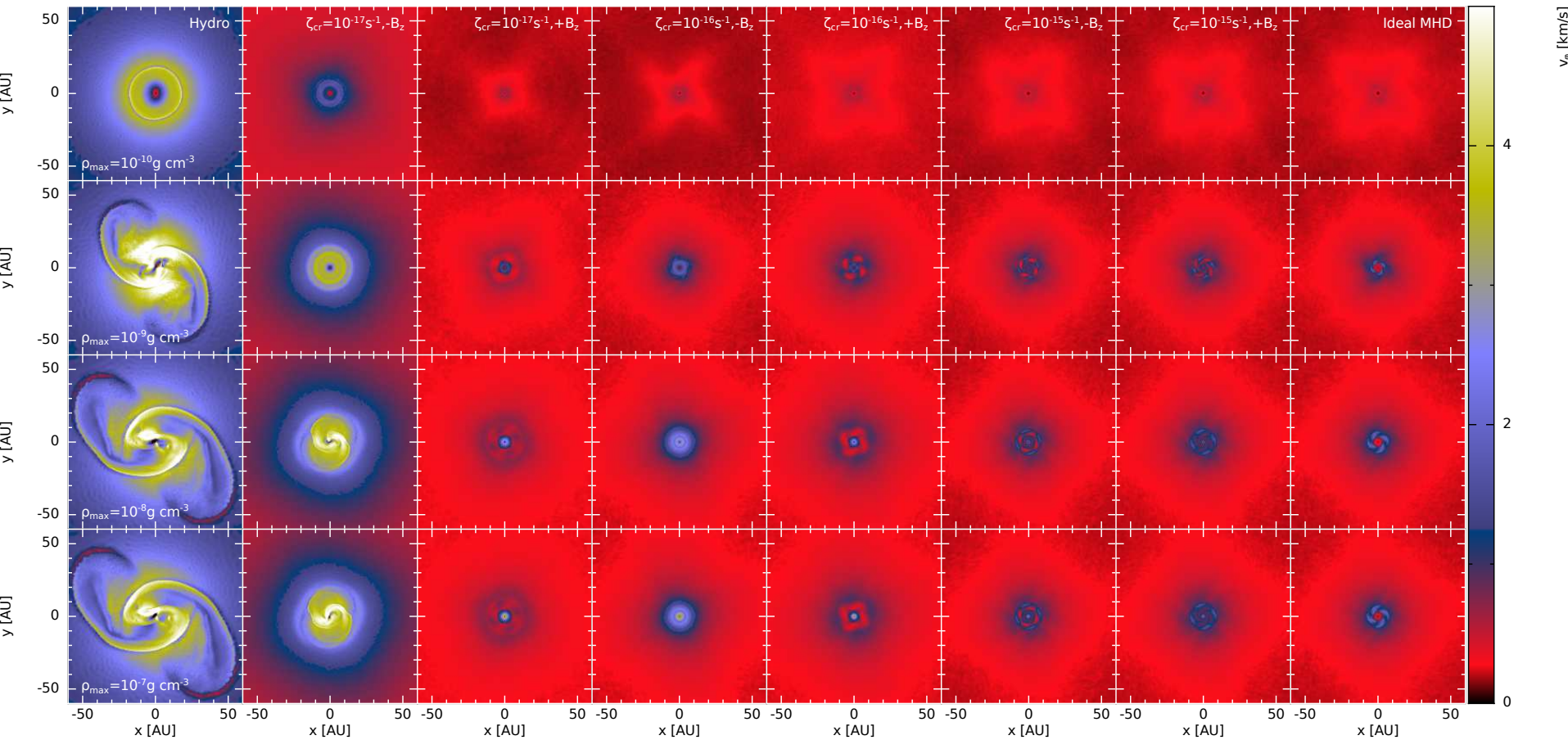
# Envelopes: Induced rotation

- Hall effect can induce coherent rotation from a zero-angular momentum initial condition



# Rotationally supported discs

➤ Discs form in the hydrodynamics model and the non-ideal model with  $\zeta_{\text{cr}} = 10^{-17} \text{ s}^{-1}$  with  $-B_z$



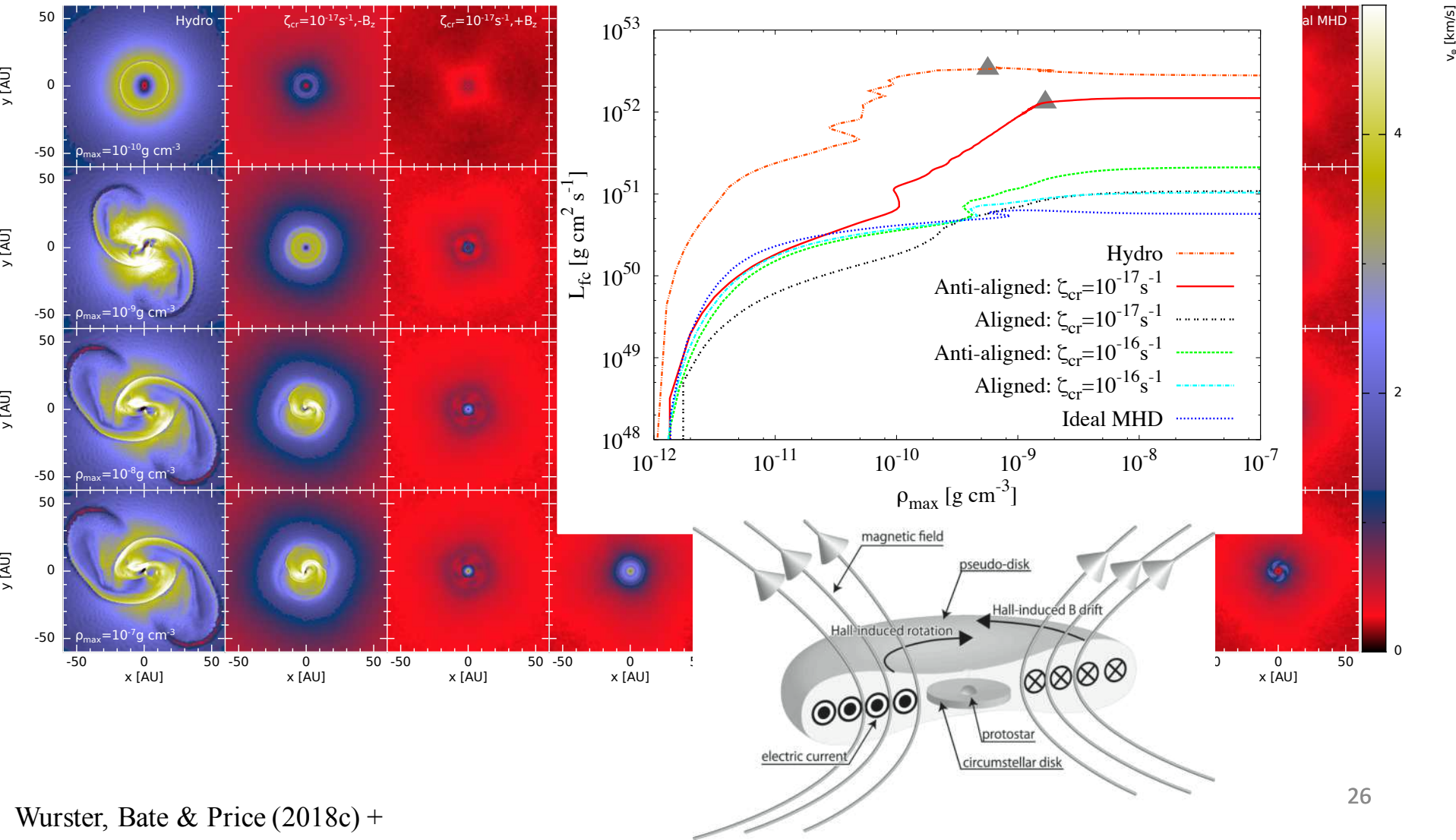
➤ Discs form during the first hydrostatic core phase

➤ Similar disc structure obtained by Tsukamoto+ (2015a) for  $\zeta_{\text{cr}} = 10^{-17} \text{ s}^{-1}$  with  $\pm B_z$

Wurster, Bate & Price (2018c) +

# Rotationally supported discs

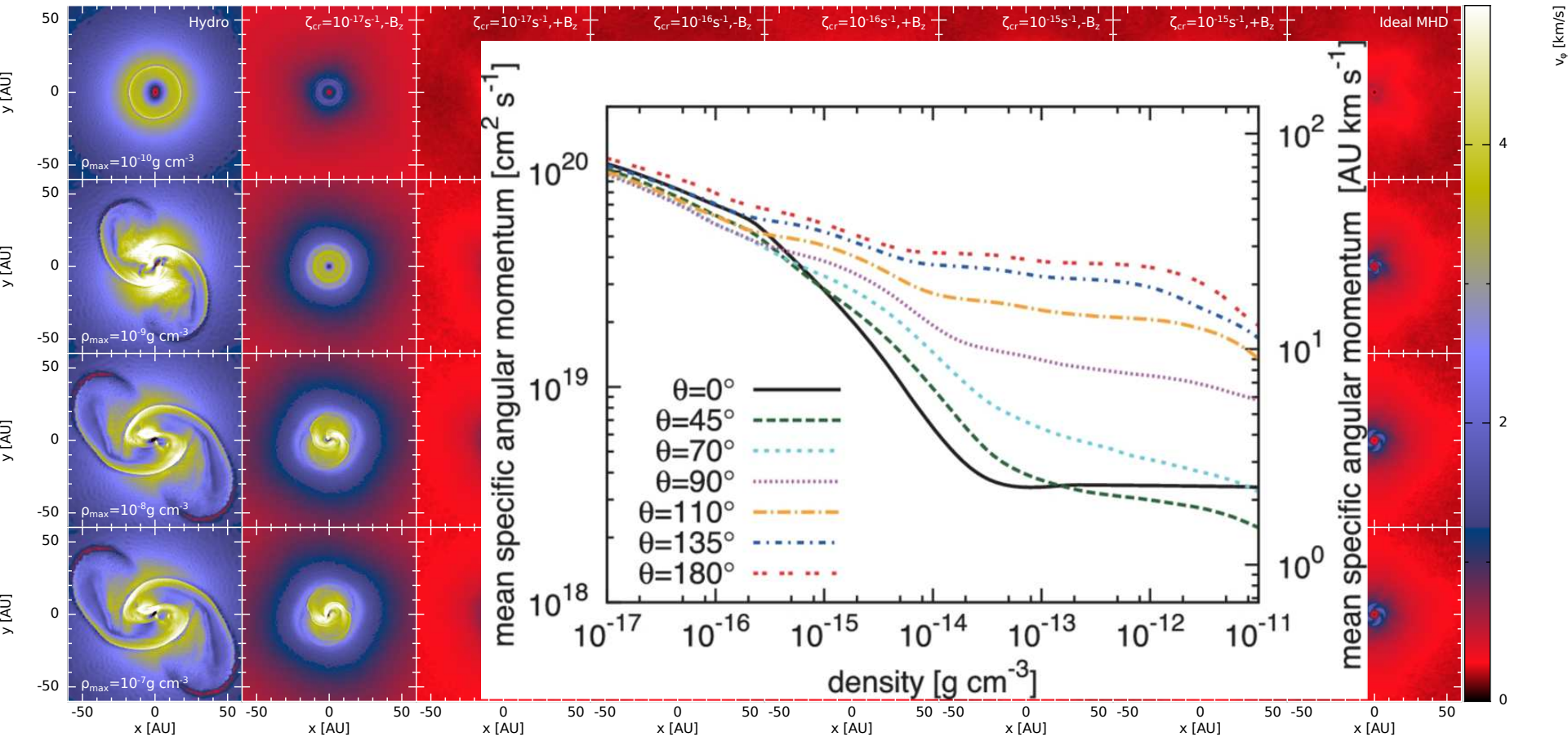
➤ Discs form in the hydrodynamics model and the non-ideal model with  $\zeta_{\text{cr}} = 10^{-17} \text{ s}^{-1}$  with  $-B_z$





# Rotationally supported discs

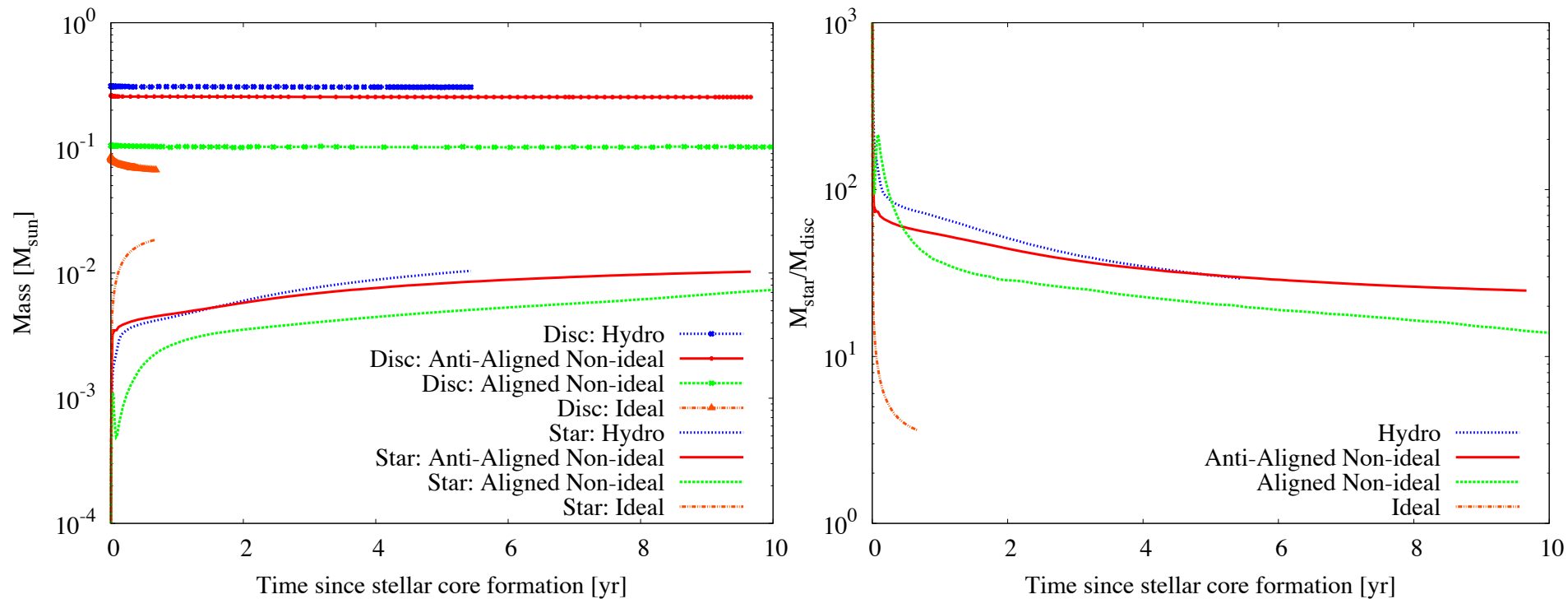
➤ Discs form in the hydrodynamics model and the non-ideal model with  $\zeta_{\text{cr}} = 10^{-17} \text{ s}^{-1}$  with  $-B_z$



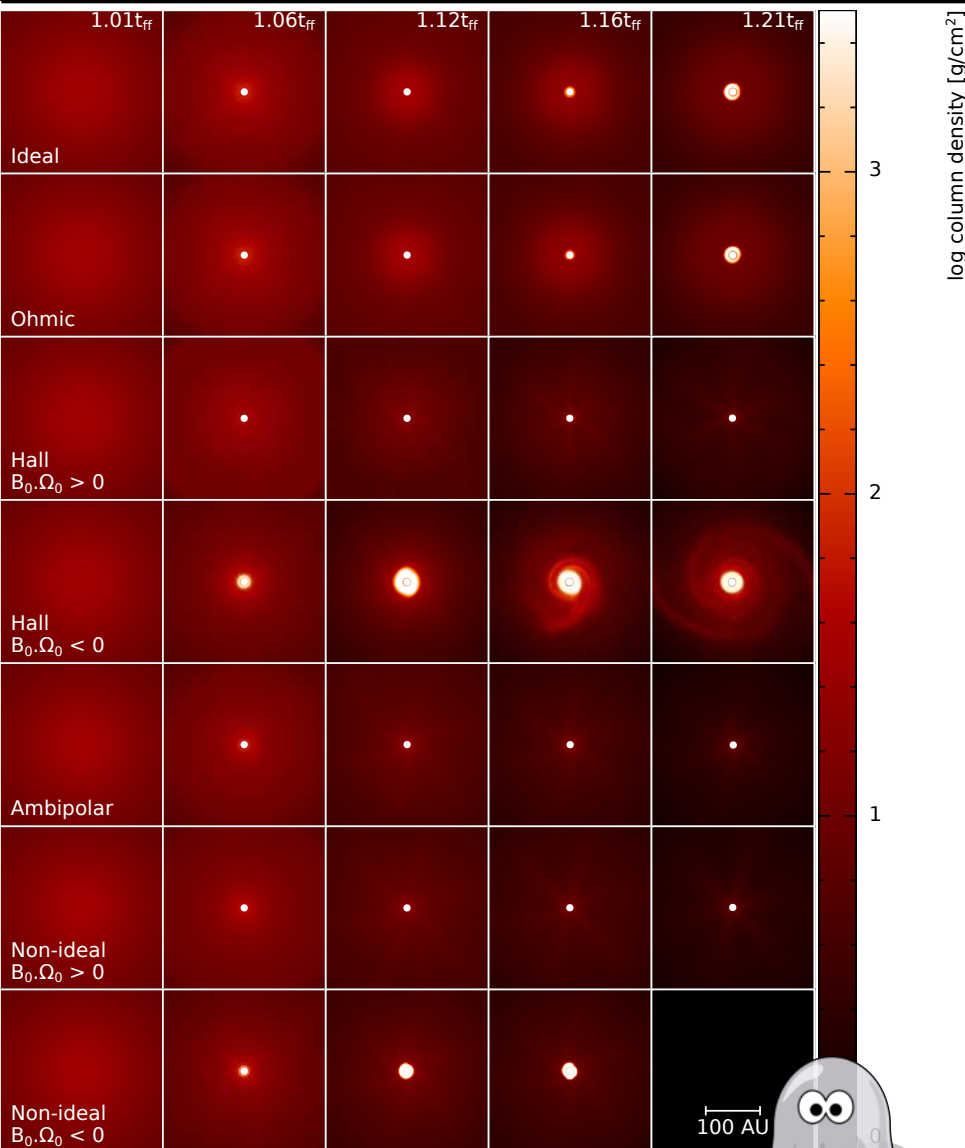


# Disc Masses

- Disc mass: sum of the gas with  $10^{-13} \text{ g cm}^{-3} < \rho < 10^{-4} \text{ g cm}^{-3}$
- Stellar mass: sum of the gas with  $\rho > 10^{-4} \text{ g cm}^{-3}$



# Non-Ideal MHD Components

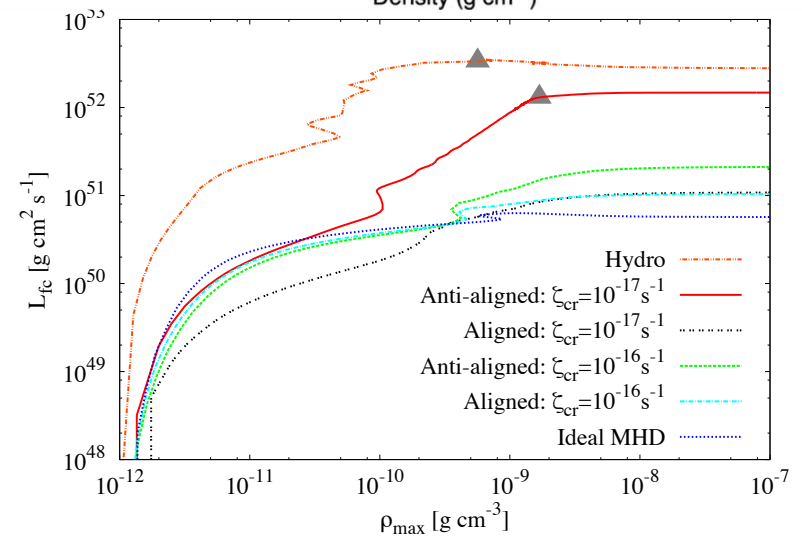
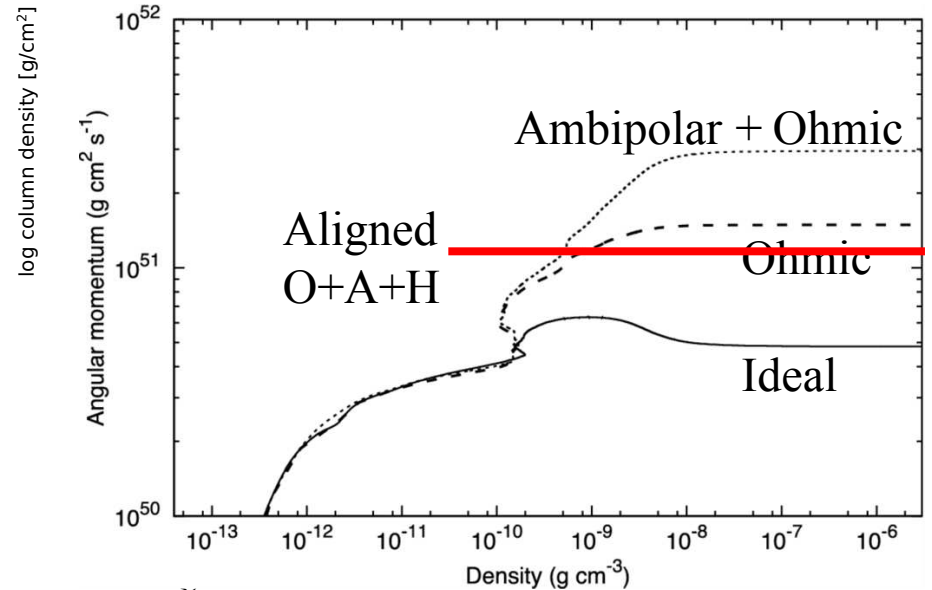
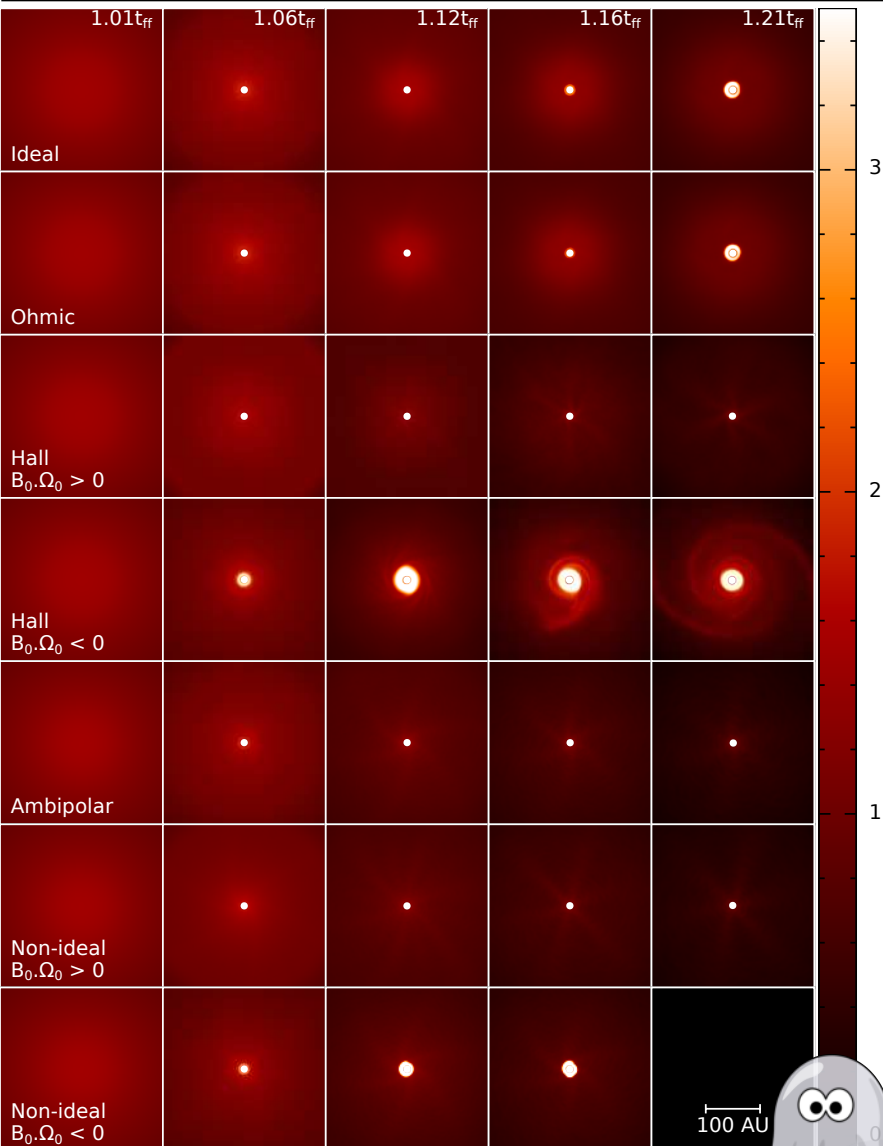


- Multiple conclusions in the literature regarding disc formation with Ohmic resistivity and/or ambipolar diffusion
- Likely possible to form small 1-5au discs in the long term with only Ohmic and/or ambipolar (Dapp and Basu 2010, Machida+ 2011, Dapp+ 2012, Tomida+ 2015, Tsukamoto+ 2015a, Masson+ 2016)
- Hennebelle et al. (2016) predicts 18au discs for ambipolar diffusion only
- Models to the left include a 6.7au sink particle
- Open question: *When do discs form?*



# Non-Ideal MHD Components

Anti-aligned O+A+H

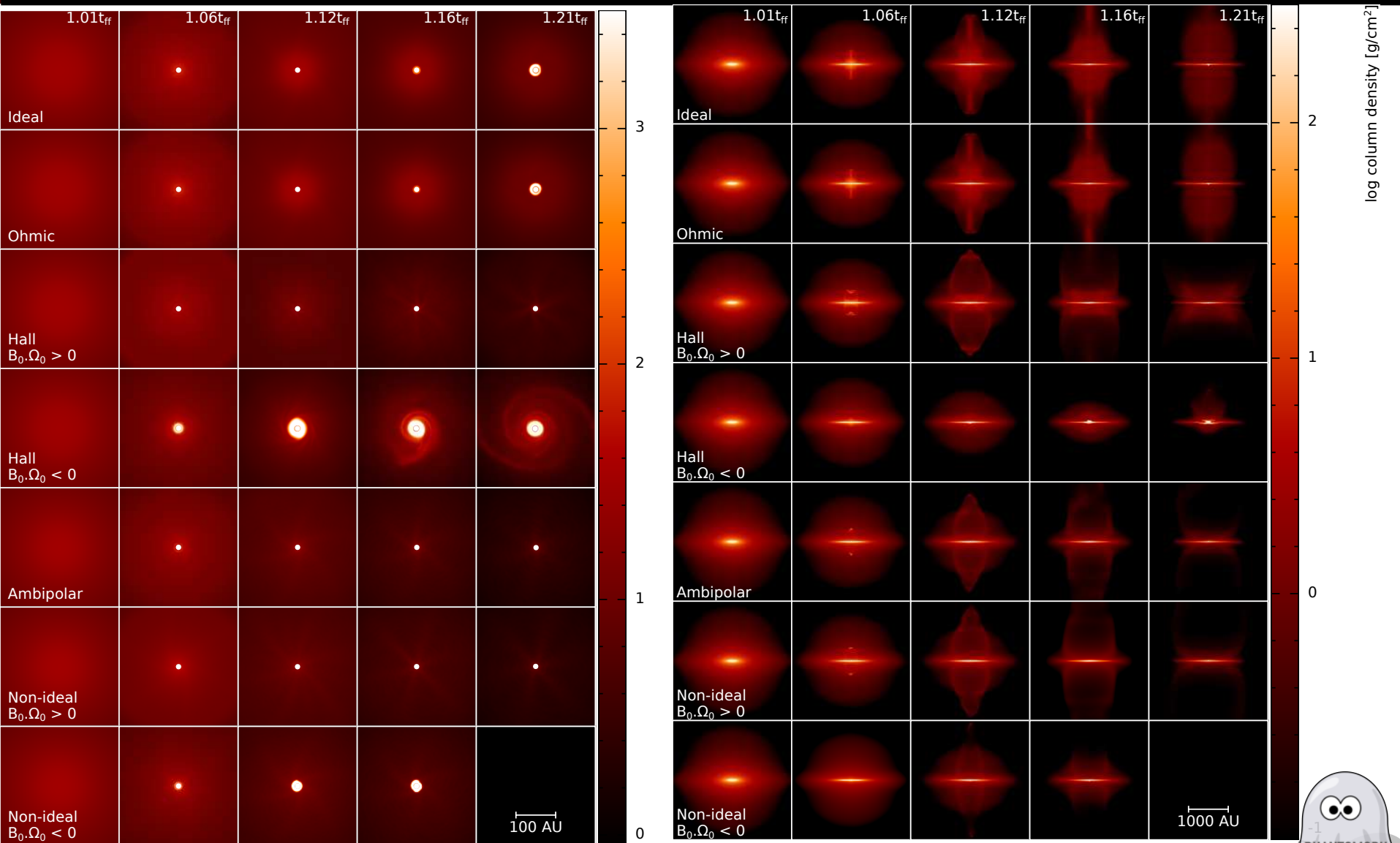


Top: Tsukamoto+ (2015b)

Bottom: Wurster, Bate & Price (2018c)

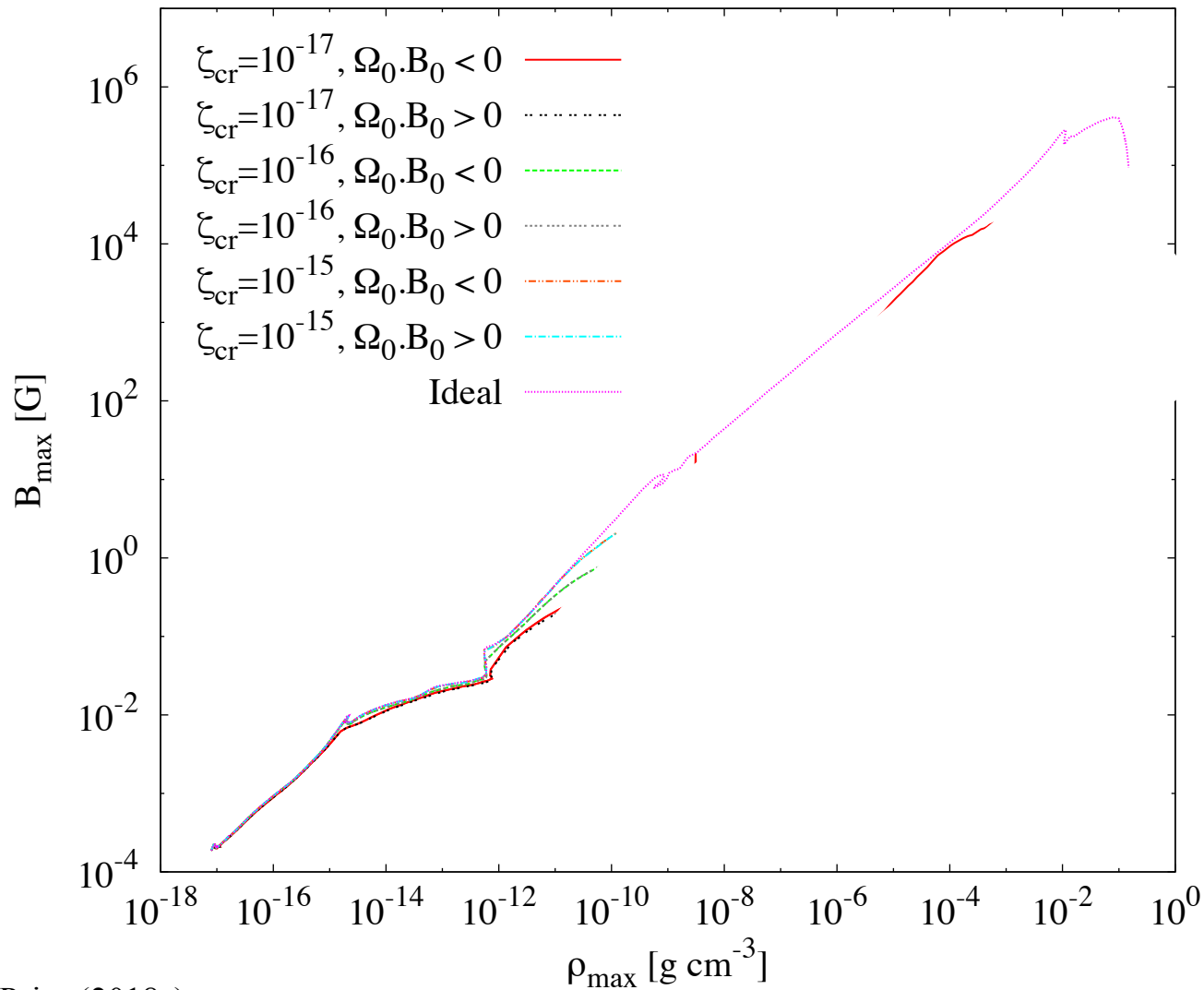


# *Non-Ideal MHD Components*



# Magnetic field evolution

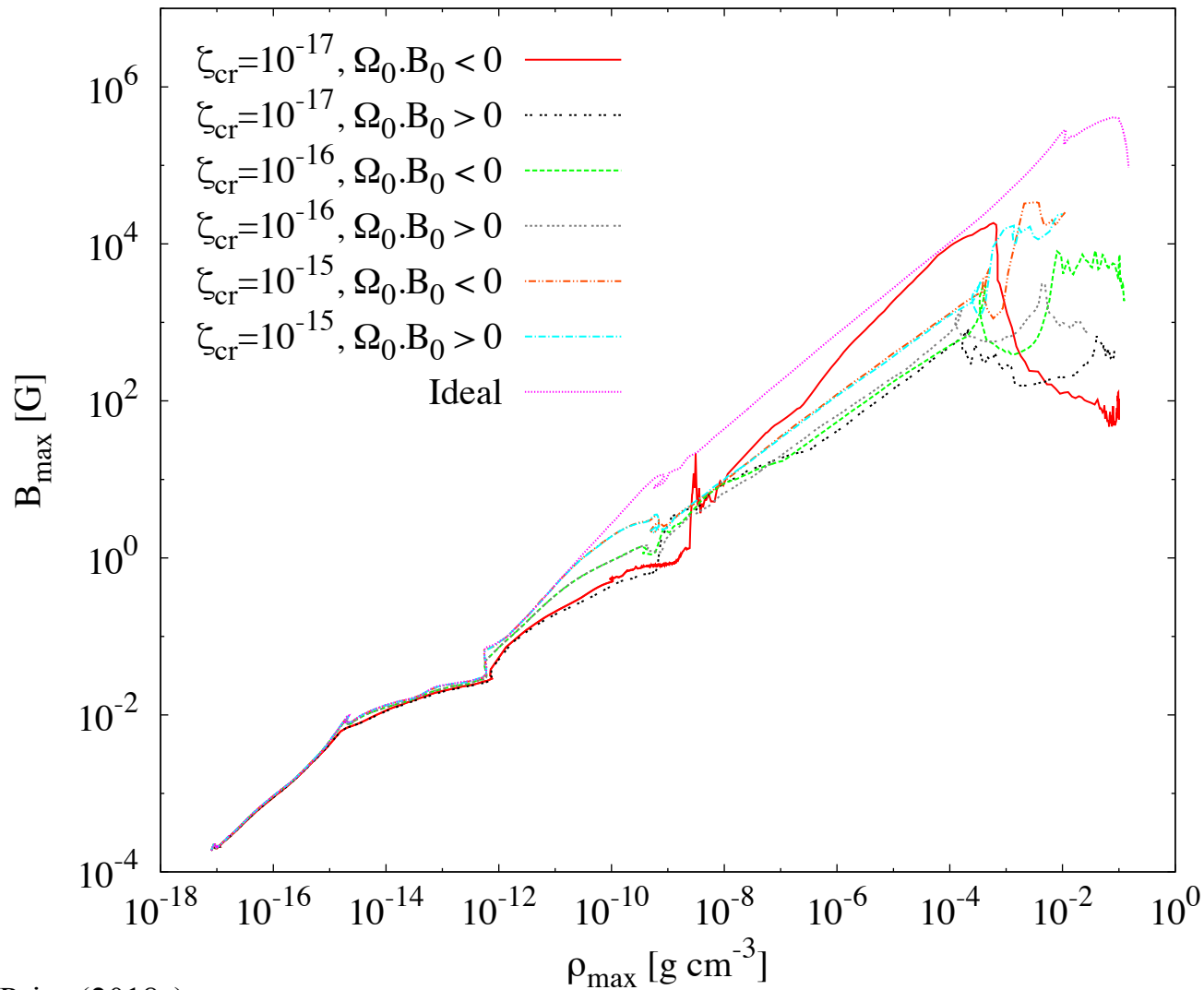
- Ideal MHD: Magnetic fields grow with density; mostly suggests spherical collapse





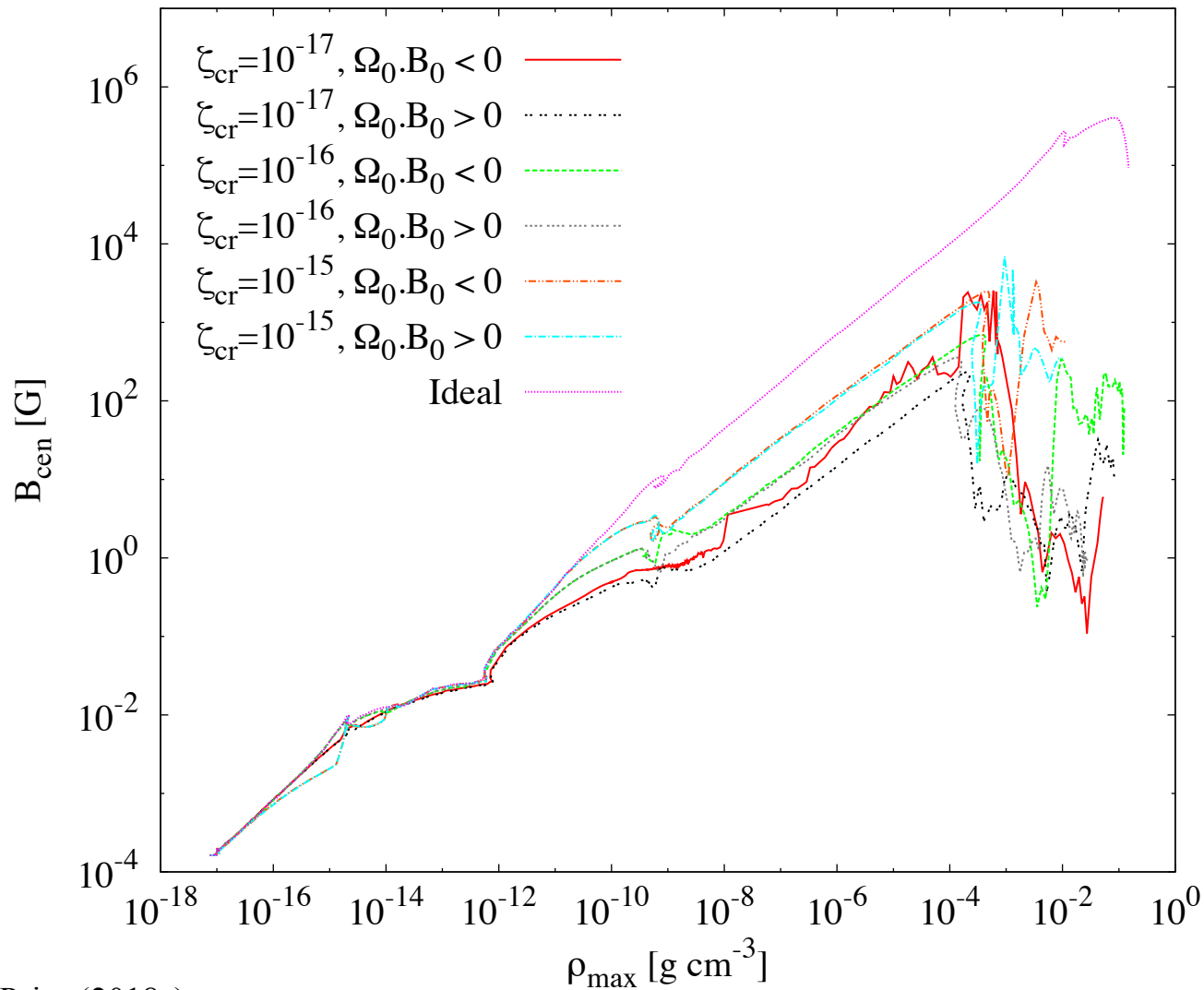
# Magnetic field evolution

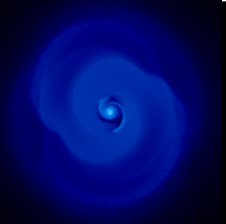
- Non-ideal effects decrease the magnetic field strength, starting in the first core phase



# Magnetic field evolution

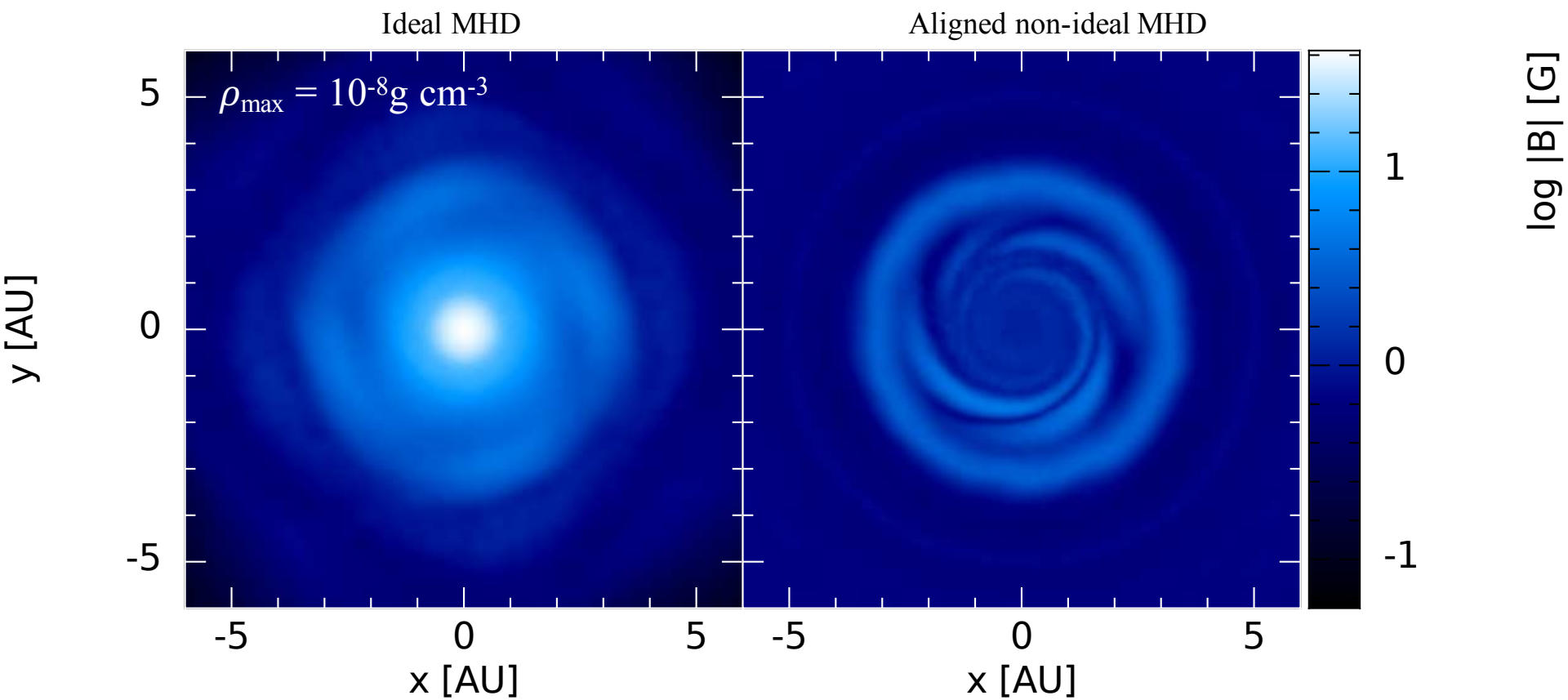
- The maximum magnetic field strength is not at the centre of the core in the non-ideal models





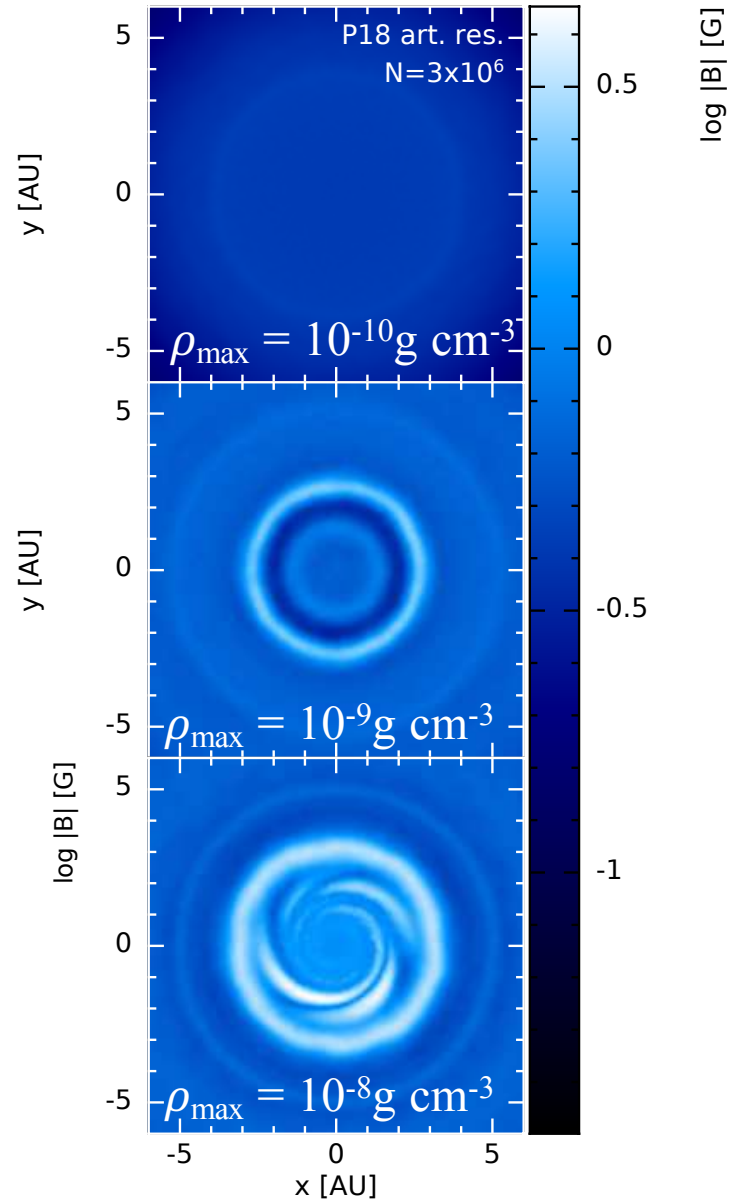
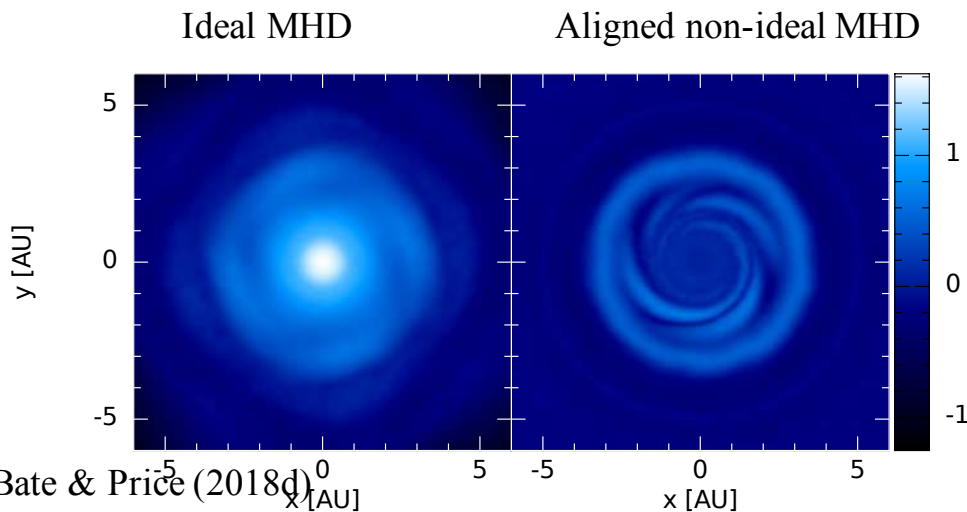
# *Magnetic field evolution*

- Magnetic wall forms in non-ideal MHD models  
(Tassis & Mouschovias, 2005)

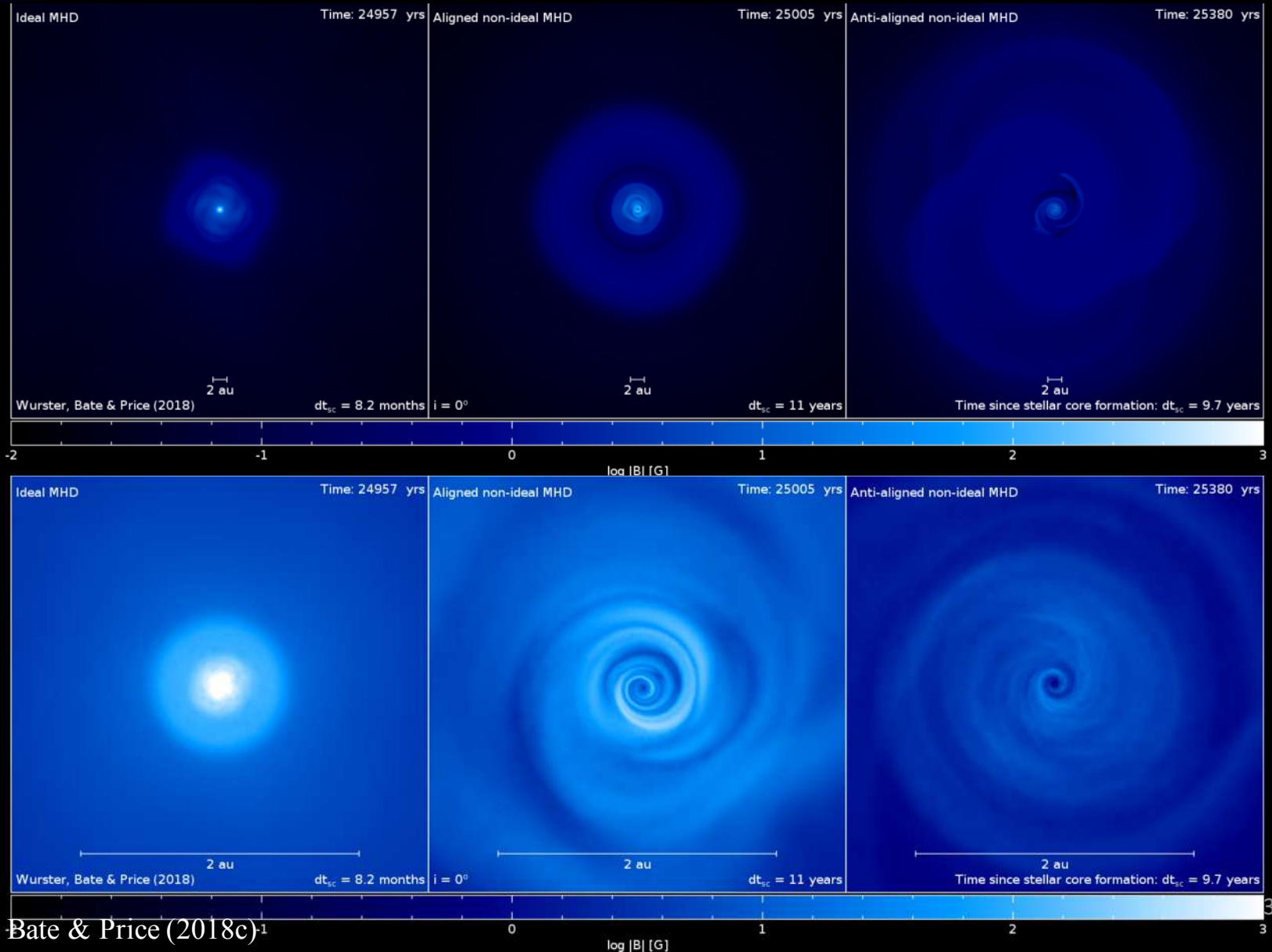


# Magnetic field evolution

- Magnetic wall forms in non-ideal MHD models (Tassis & Mouschovias, 2005)



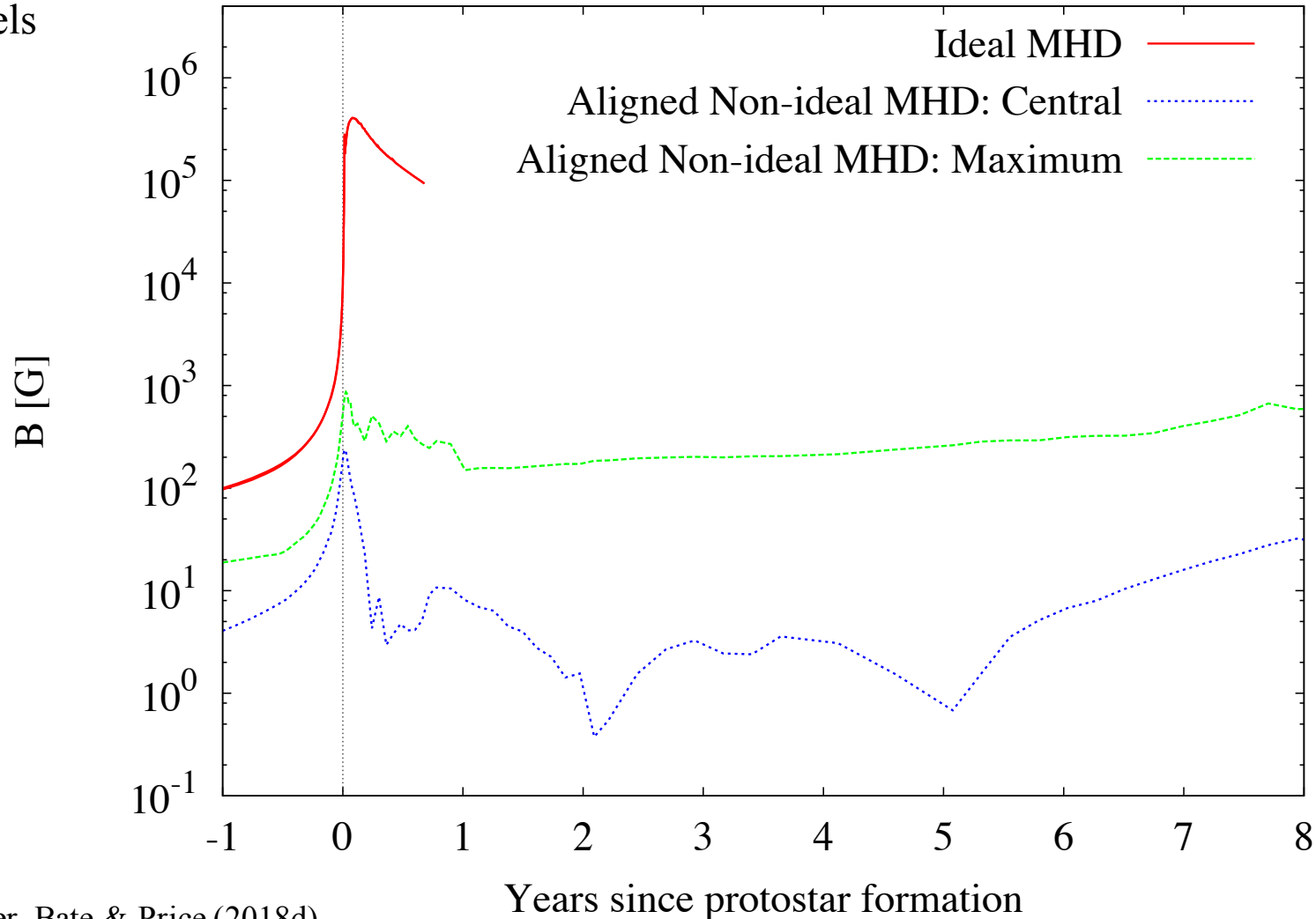
# Magnetic field evolution

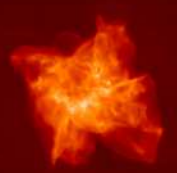




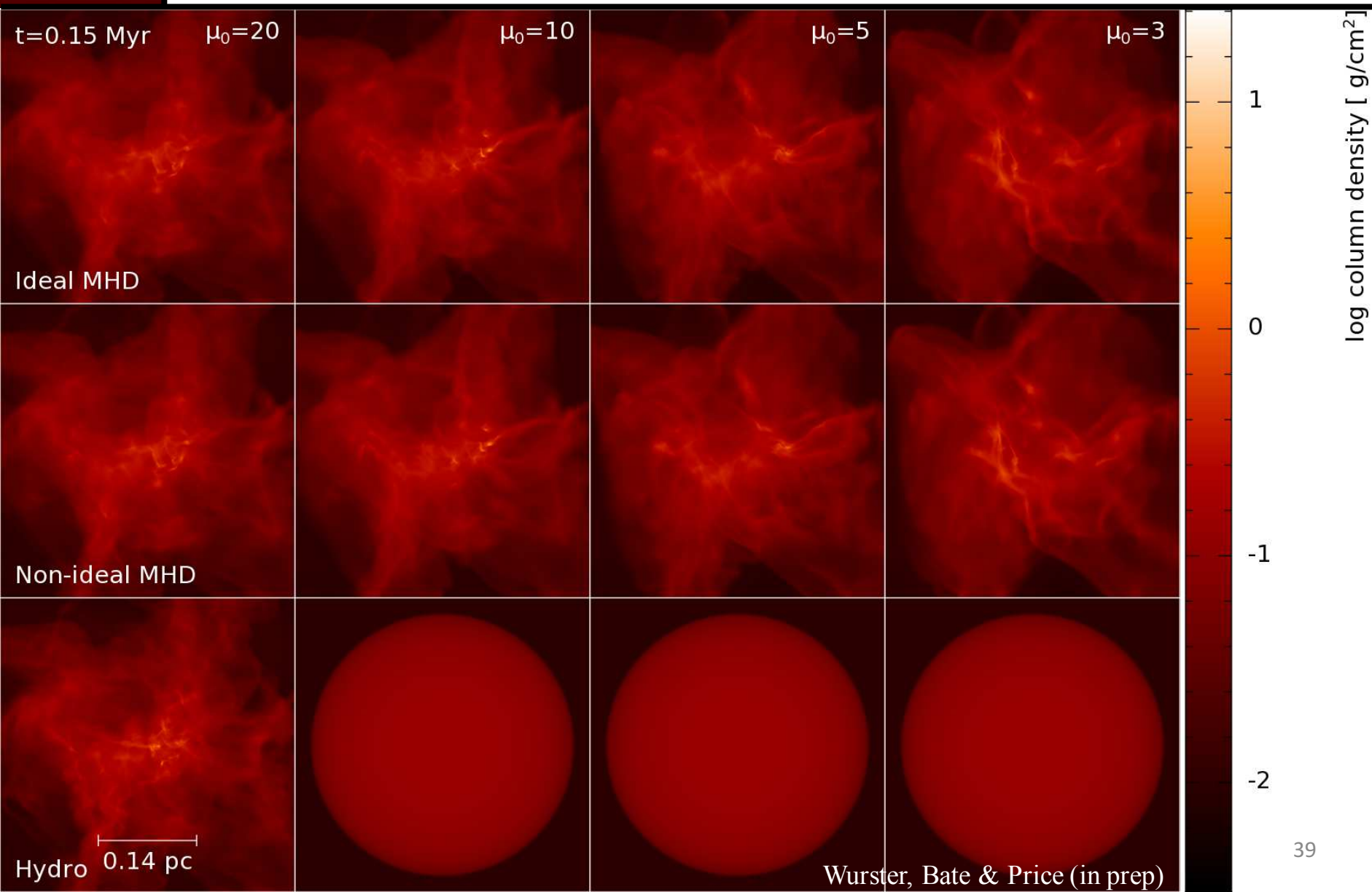
# *Magnetic field evolution*

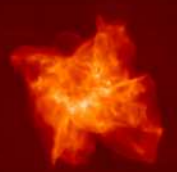
- Strong kG magnetic fields are observed in stars. Are they fossil, or dynamo-generated?
- Most likely dynamo-generated since the fossil magnetic field is  $\ll 1000\text{G}$  in the non-ideal models



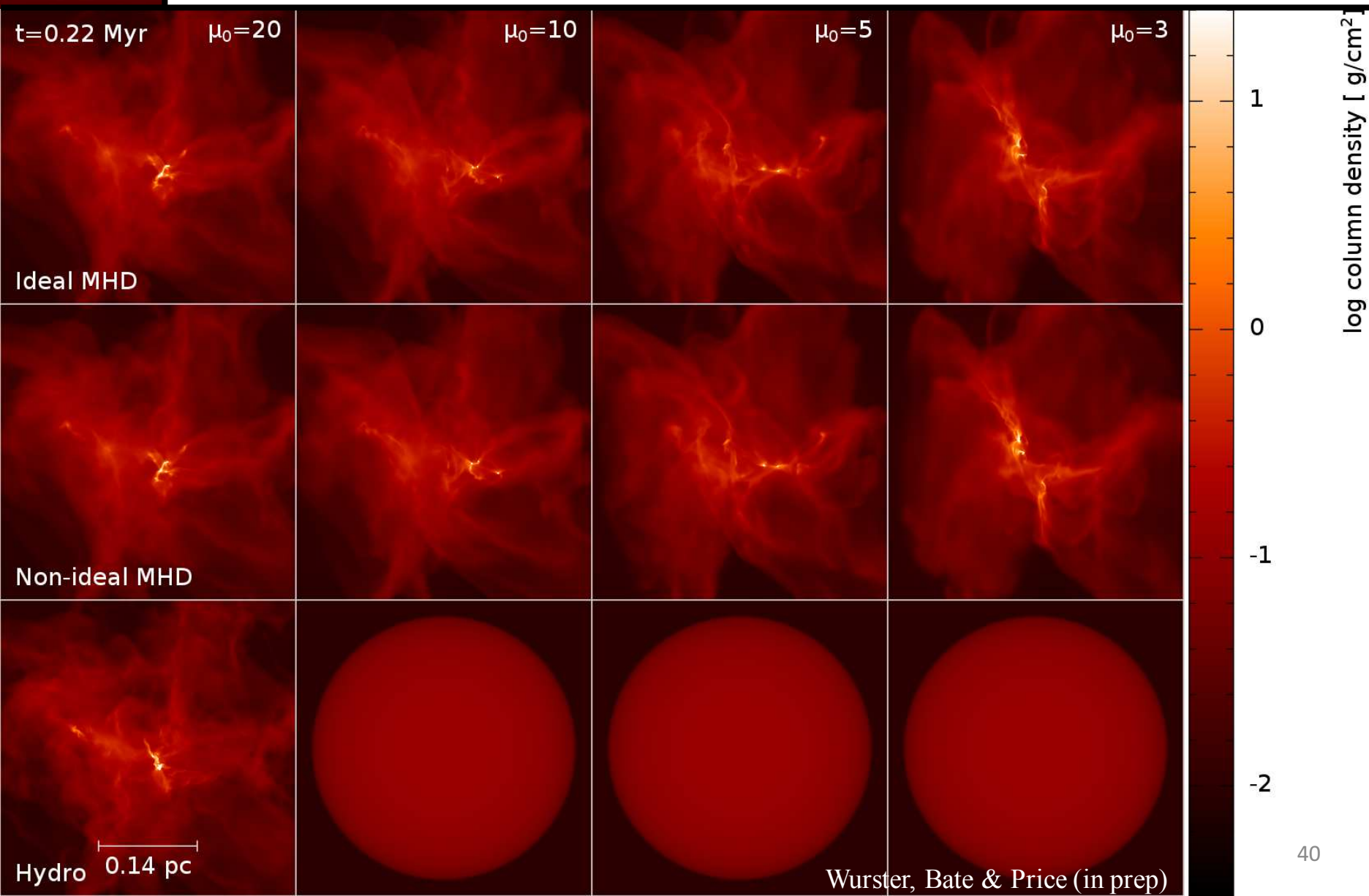


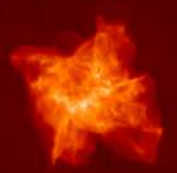
# *Cluster Formation*



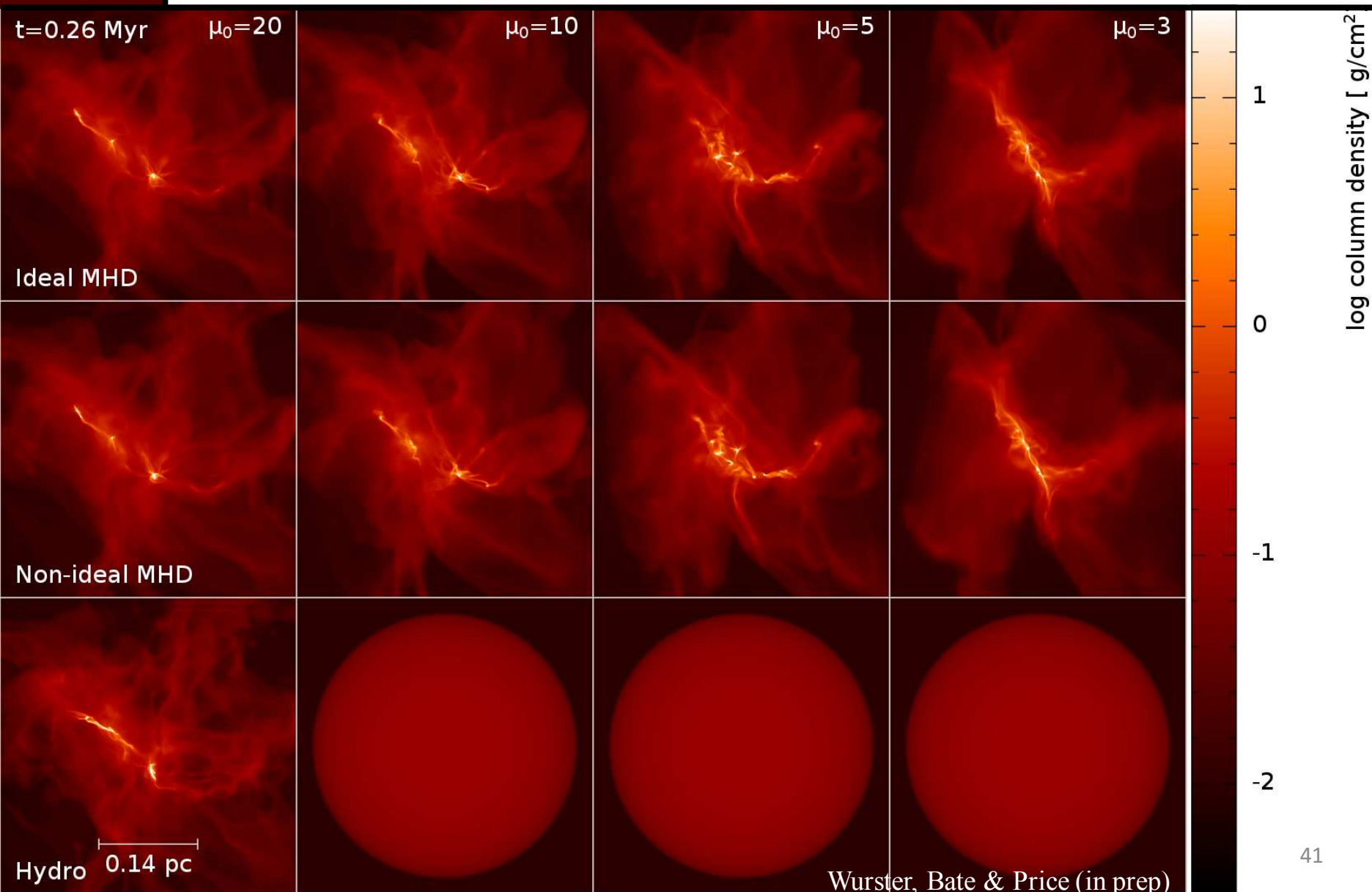


# *Cluster Formation*



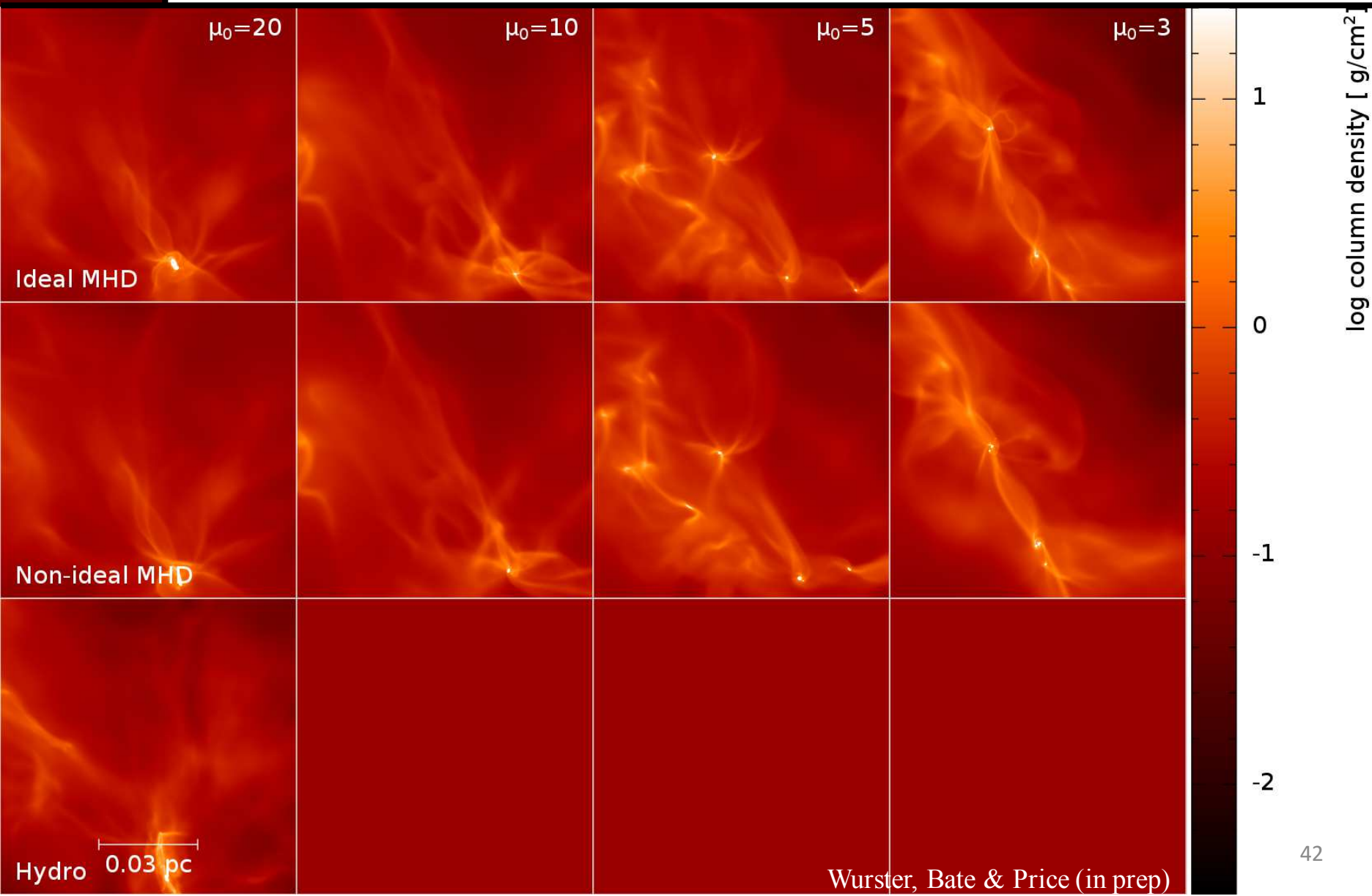


# Cluster Formation



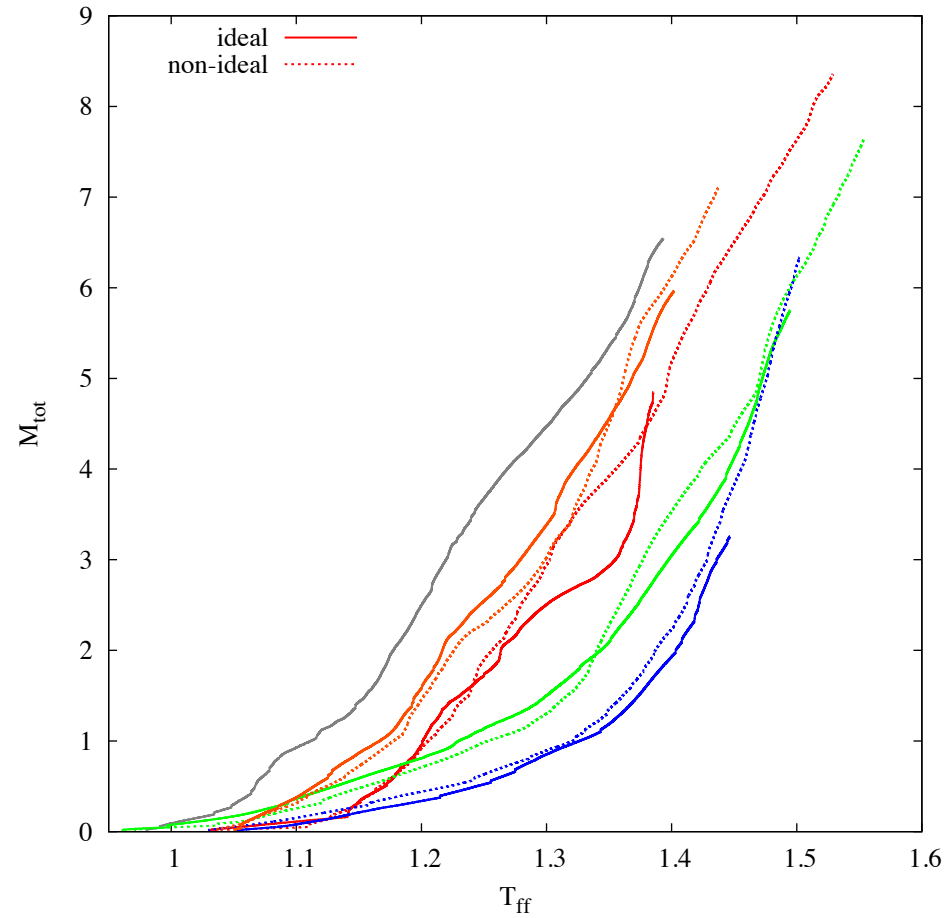
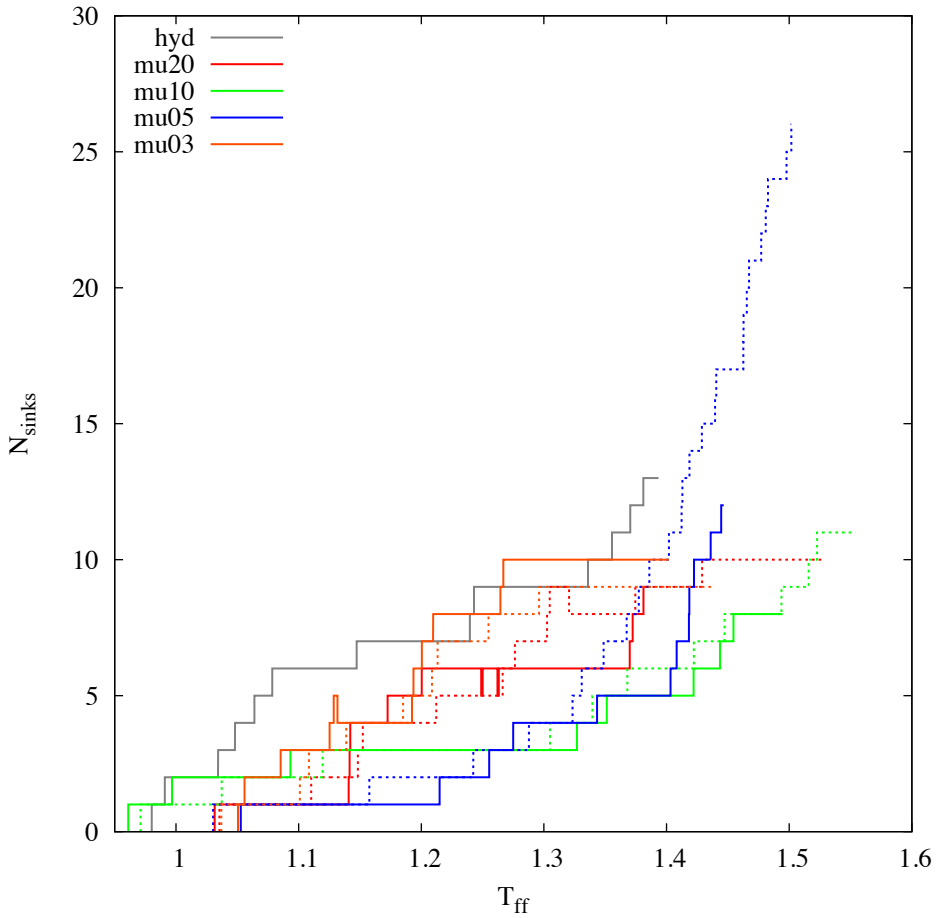
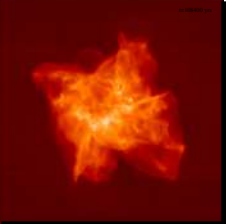


# Cluster Formation





# Cluster Formation





# Conclusions

- Modelled the collapse of a strongly magnetised molecular cloud core through the first core to stellar densities; included Ohmic resistivity, ambipolar diffusion, the Hall effect.
- Large discs only form in the hydrodynamic and  $\zeta_{\text{cr}} = 10^{-17} \text{ s}^{-1}$  with  $-B_z$  models.
- In the  $\zeta_{\text{cr}} = 10^{-17} \text{ s}^{-1}$  with  $-B_z$  model, the maximum magnetic field strength is not coincident with the maximum density.
- First core outflows are suppressed in the hydrodynamic and  $\zeta_{\text{cr}} = 10^{-17} \text{ s}^{-1}$  with  $-B_z$  models.
- A fast first core outflow exists for the  $\zeta_{\text{cr}} = 10^{-17} \text{ s}^{-1}$  with  $+B_z$  model.
- Stellar core outflows exist only when using ideal magnetohydrodynamics
- When using non-ideal MHD, the maximum magnetic field strength is not coincident with the central magnetic field strength
- The magnetic fields in stars must be generated by a dynamo action, rather than being fossil in origin