

Protostars and discs: Low-mass star formation in a magnetised medium



James Wurster

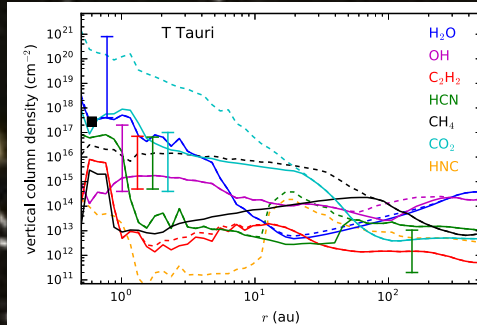
Collaborators: Matthew Bate & Daniel Price

Chalmers University of Technology

July 2, 2019

Importance of stars: The big picture

Stars as energetic events:
SN 1994D near NGC 4526
(apod.nasa.gov)



Chemical Evolution
(Agundez + 2018)



Stars as light sources:
Whirlpool Galaxy (M51; nasa.gov)



Stars as energetic events: Wolf-Rayet Star 124 (apod.nasa.gov)



Stars hosting planetary systems:
HL Tau dust disc (ALMA Partnership, 2015)

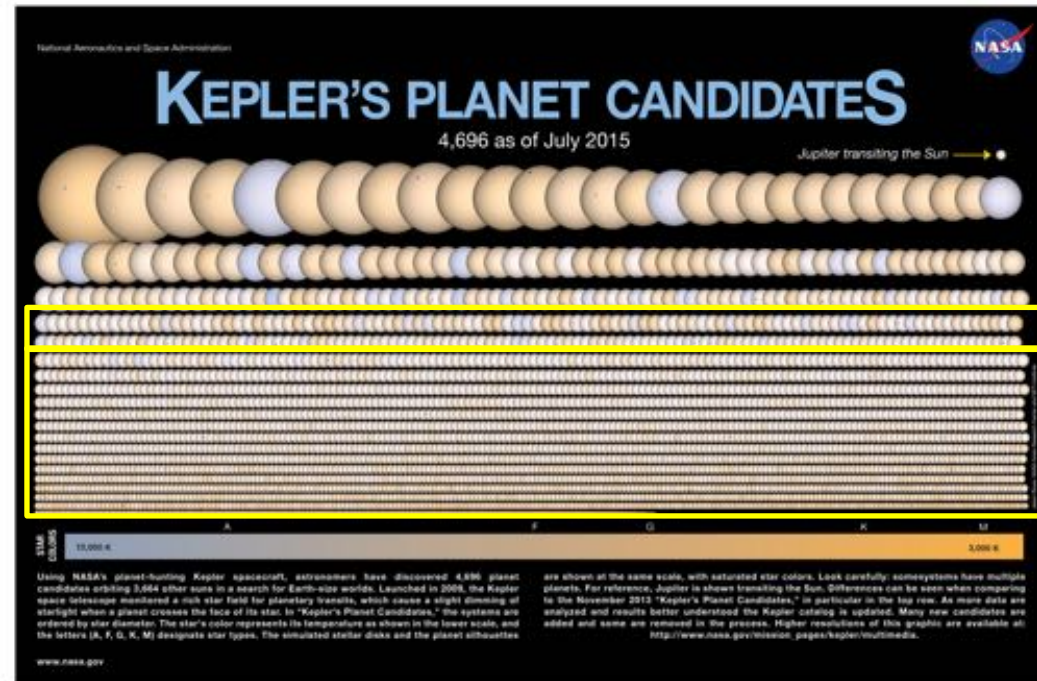
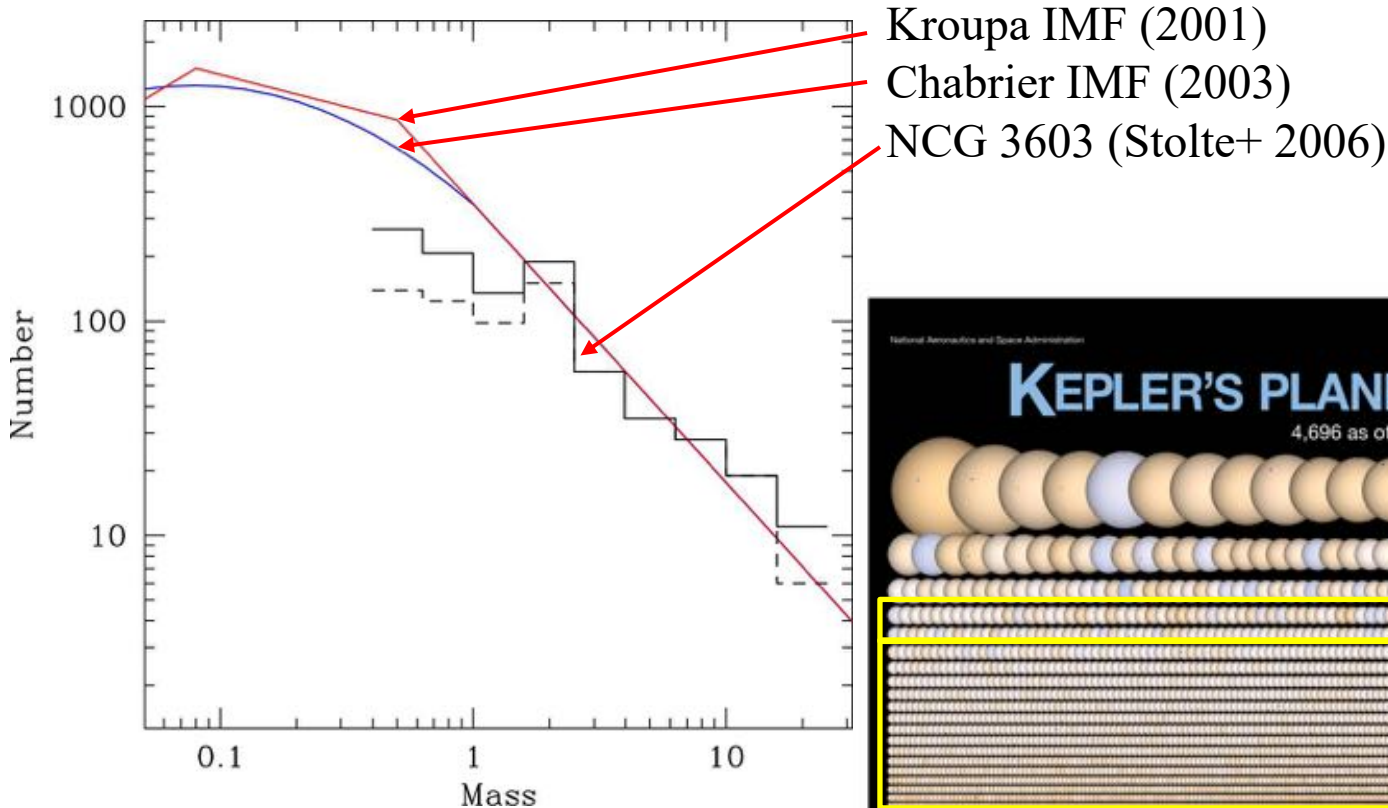


Stars launching jets: Large scale HH jet driven by a proto-brown dwarf (Riaz et. al., 2017)

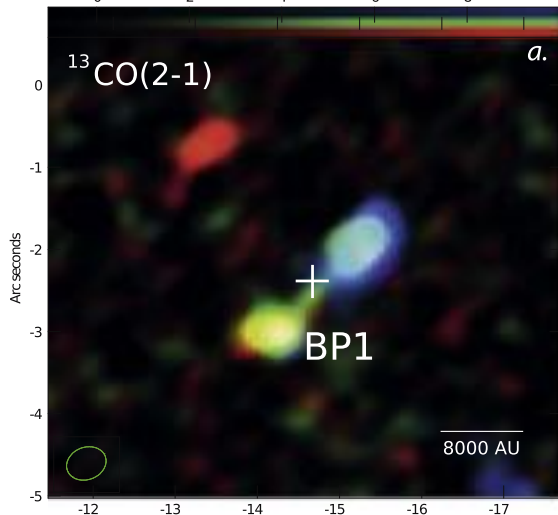
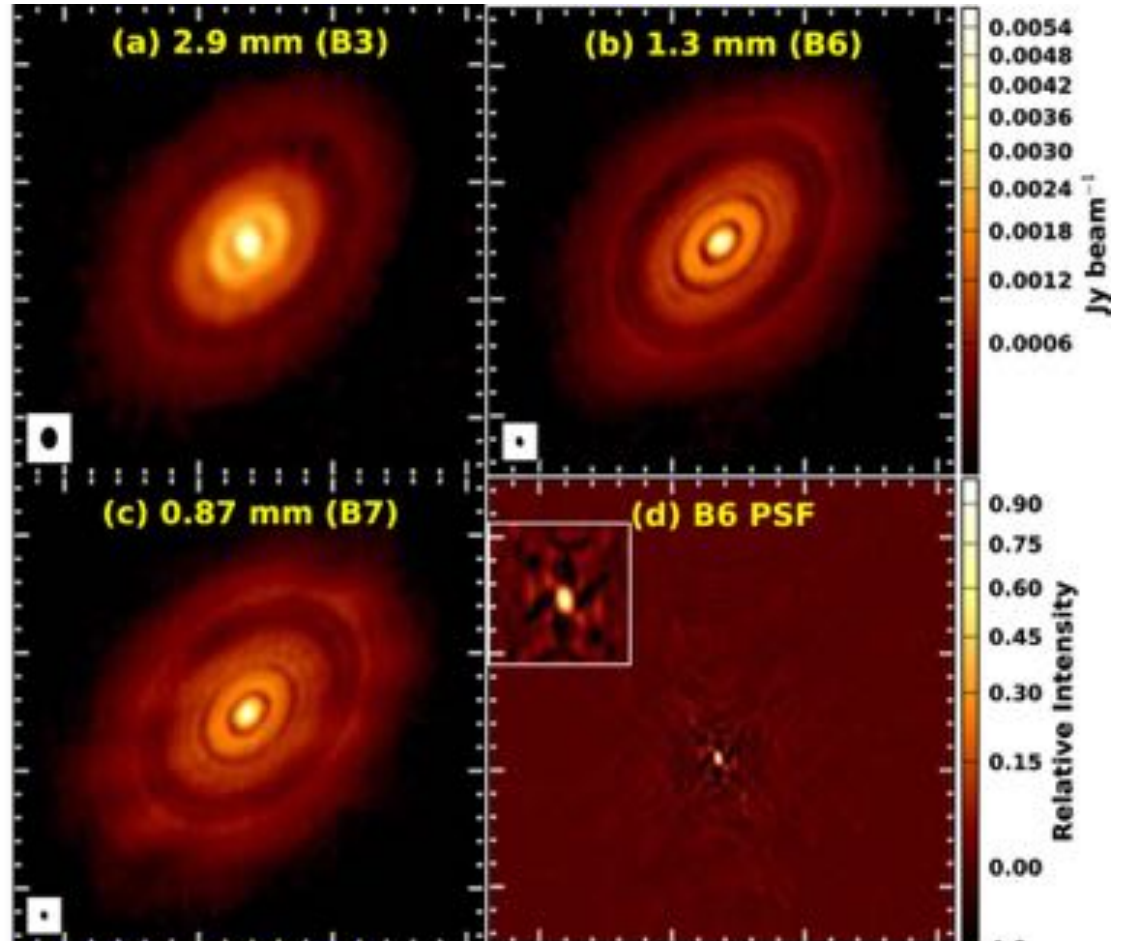
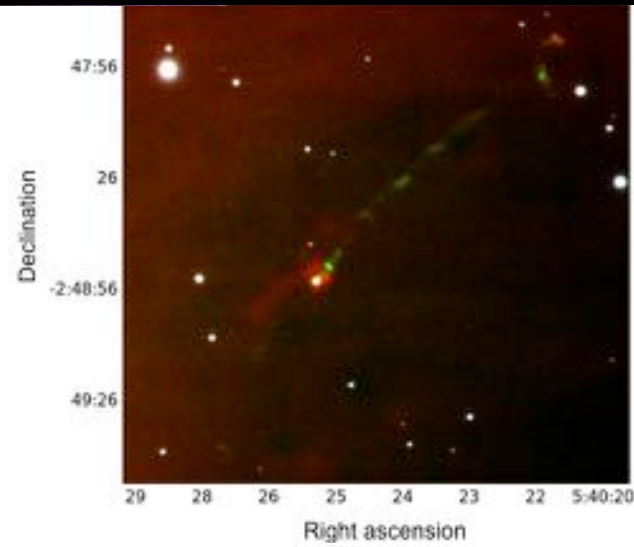
Stars as light sources: Hubble Ultra Deep Field (nasa.gov)

Importance of stars: Masses

➤ Initial mass function (IMF) of NCG 3603

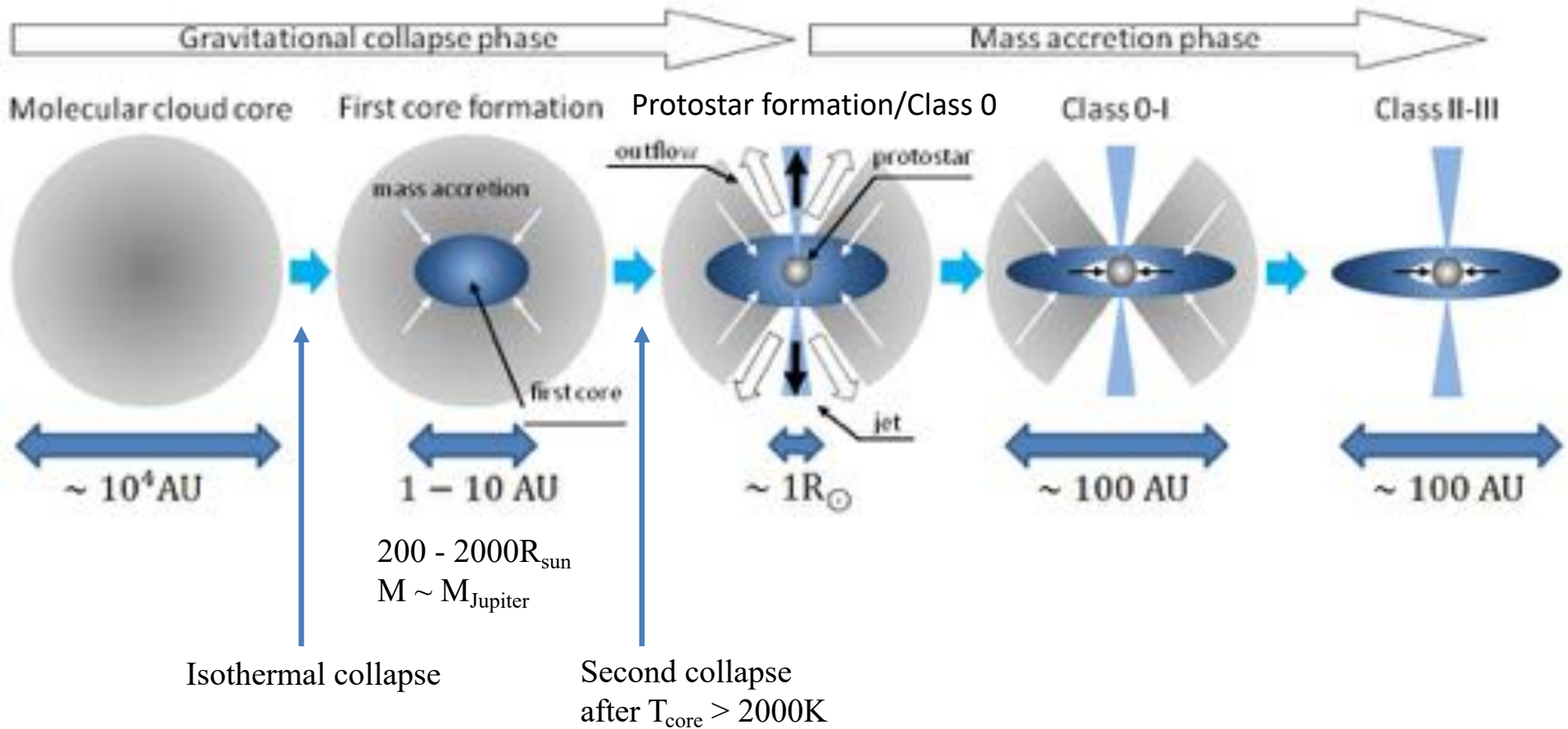


Importance of Low-stars: Outflows & Discs



Top left: Large scale Herbig-Haro jet driven by a proto-brown dwarf (Riaz et. al., 2017)
Bottom left: CO outflows from low-mass stars with 1pc of Sgr A* (Yusef-Zadeh et. al., 2017)
Right: HL Tau dust disc (ALMA Partnership, 2015)

Star formation: from the beginning





*Disc formation:
Magnetohydrodynamics*

The Magnetic Braking Catastrophe:

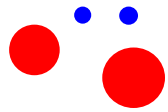
discs do not form in numerical simulations containing strong, ideal magnetic fields



No magnetic field



Strong magnetic field



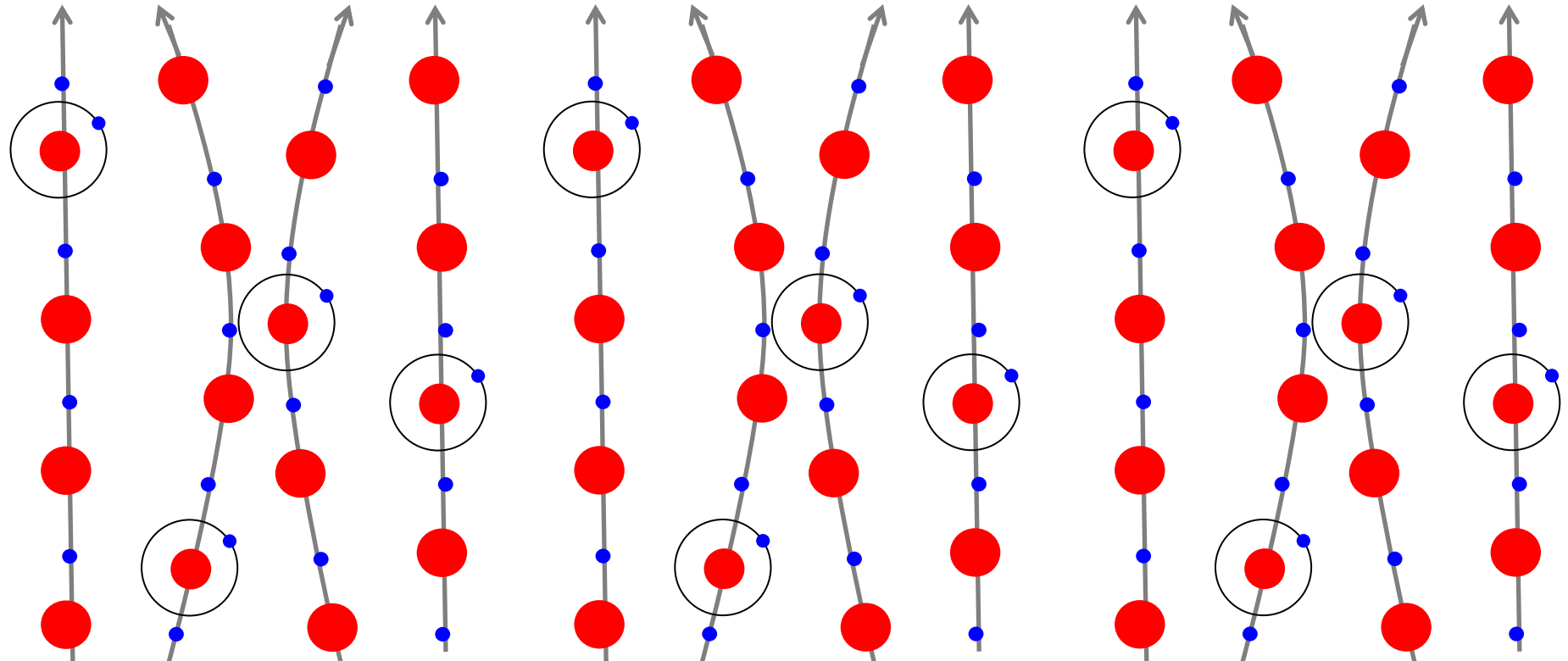
Ideal magnetohydrodynamics

➤ Highly ionised plasma: ● + ●

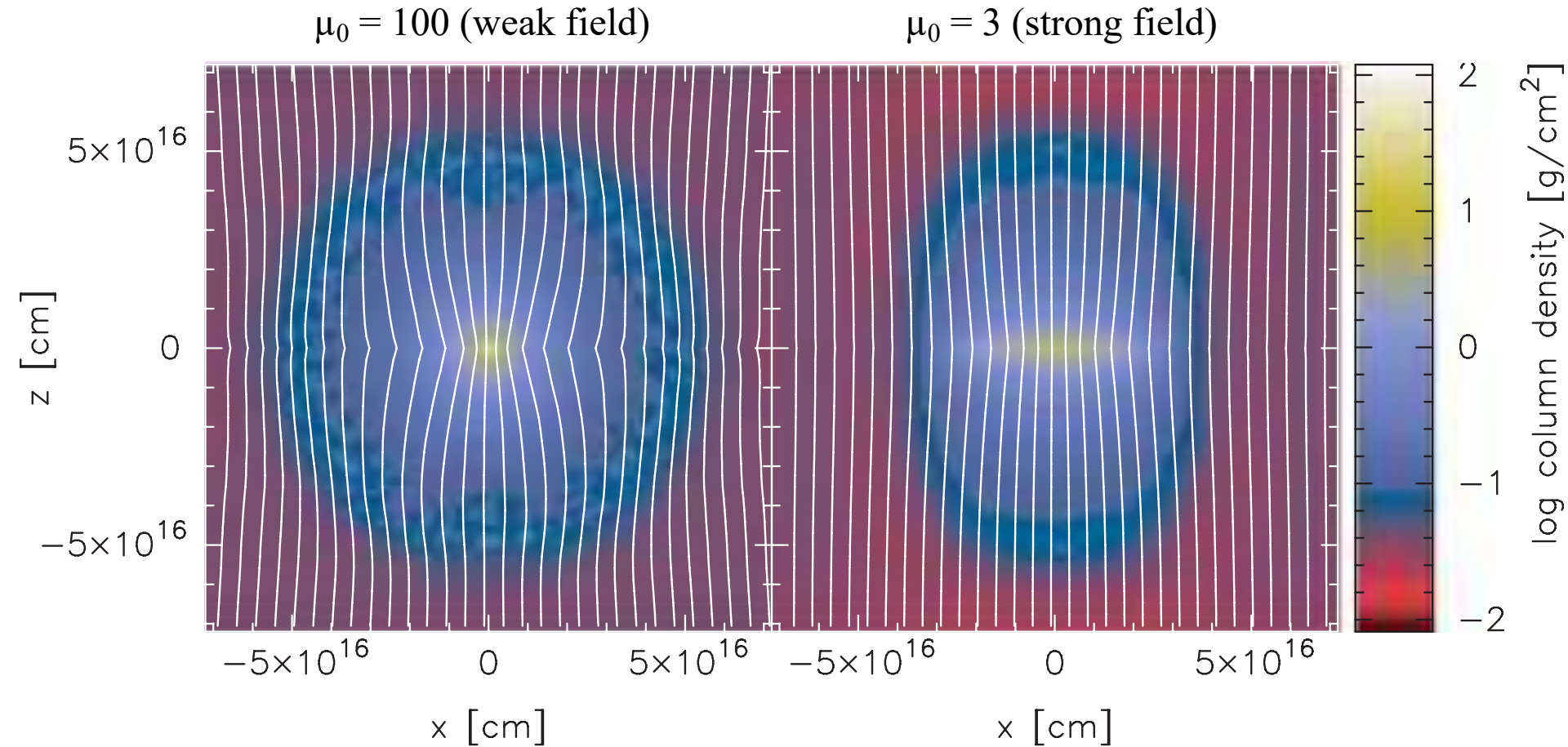
➤ Zero resistivity & infinite conductivity

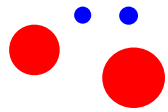
➤ Ions & electrons are tied to the magnetic field

➤ Neutral particles are tied to the magnetic field due to interactions with the ions & electrons



Star formation: with ideal magnetic fields





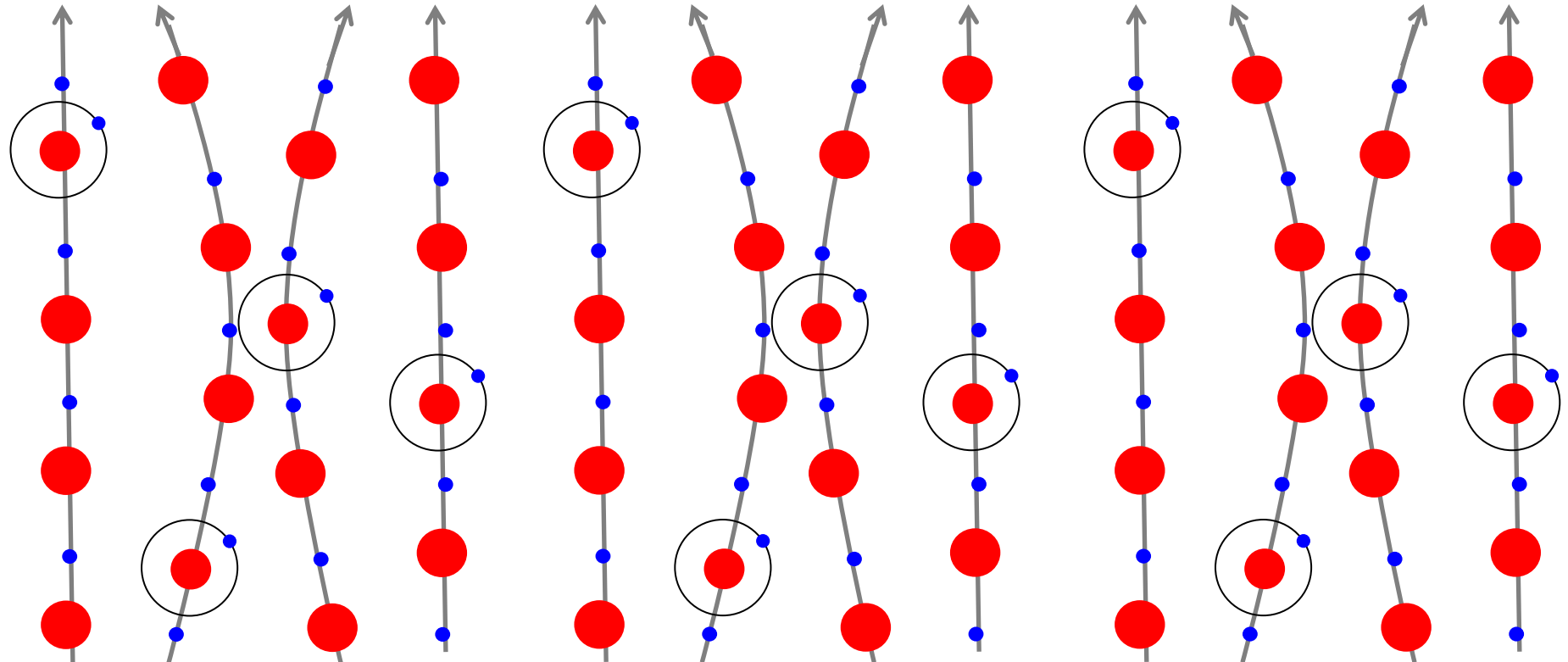
Ideal magnetohydrodynamics

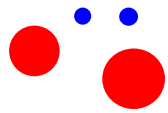
➤ Highly ionised plasma: ● + ●

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➤ Neutral particles are tied to the magnetic field due to interactions with the ions & electrons





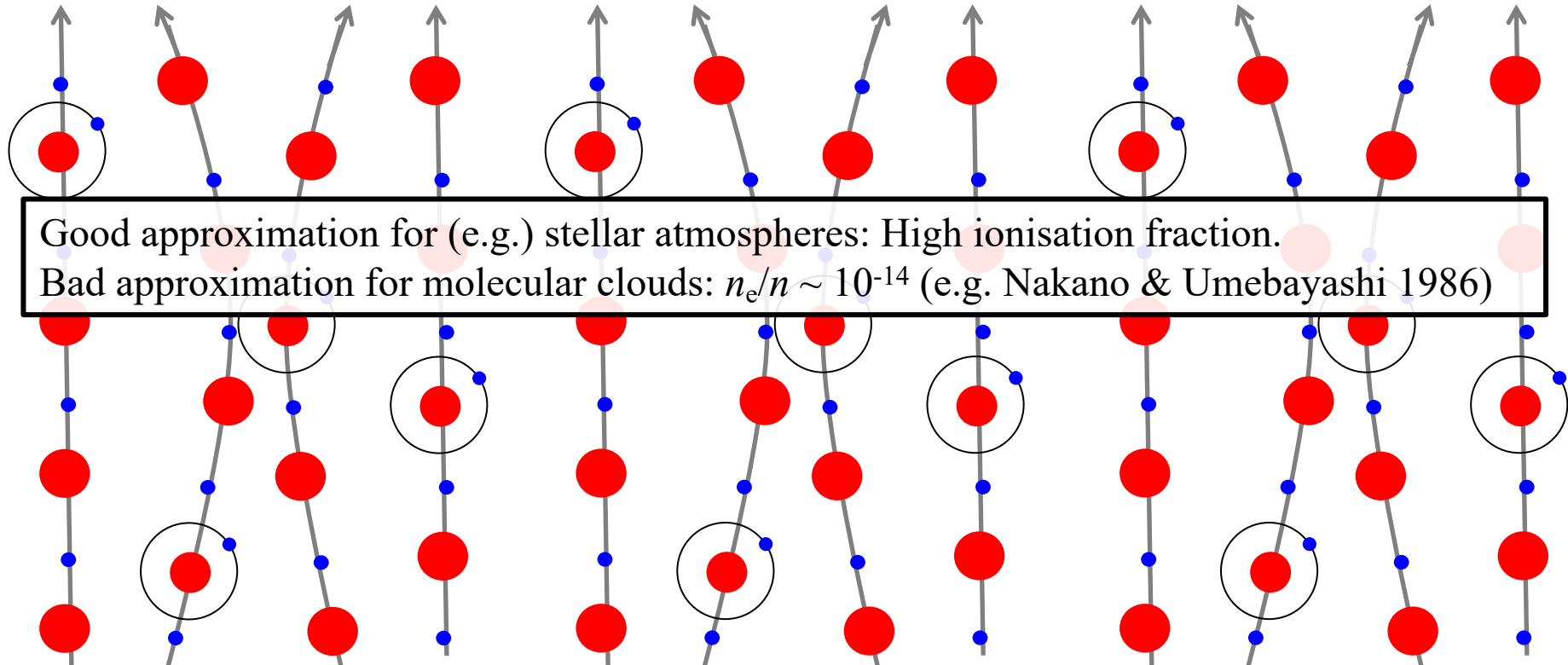
Ideal magnetohydrodynamics

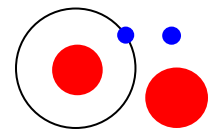
➤ Highly ionised plasma: 

➤ Zero resistivity & infinite conductivity

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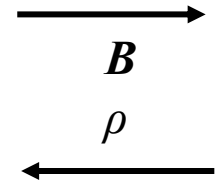
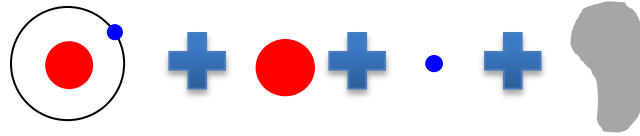
➤ Neutral particles are tied to the magnetic field due to interactions with the ions & electrons





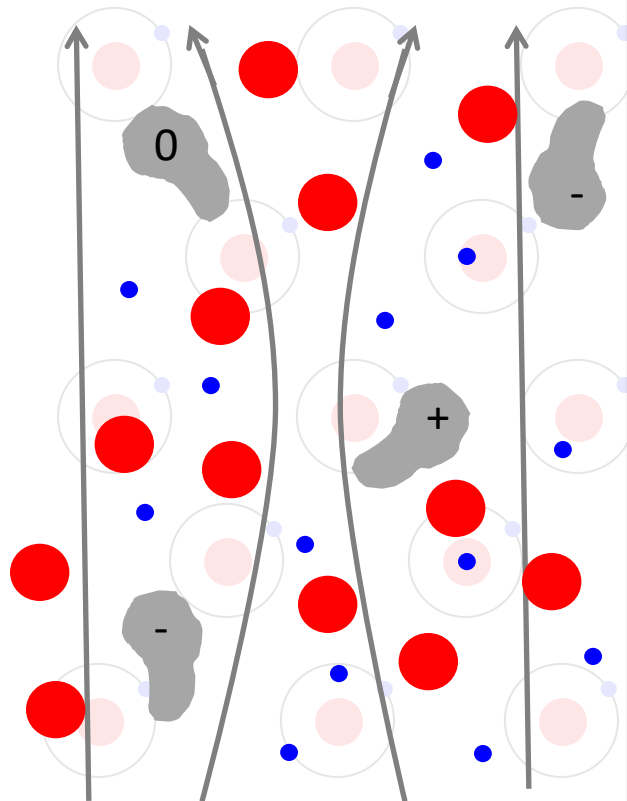
Non-ideal magnetohydrodynamics

➤ Partially ionised plasma and dust:

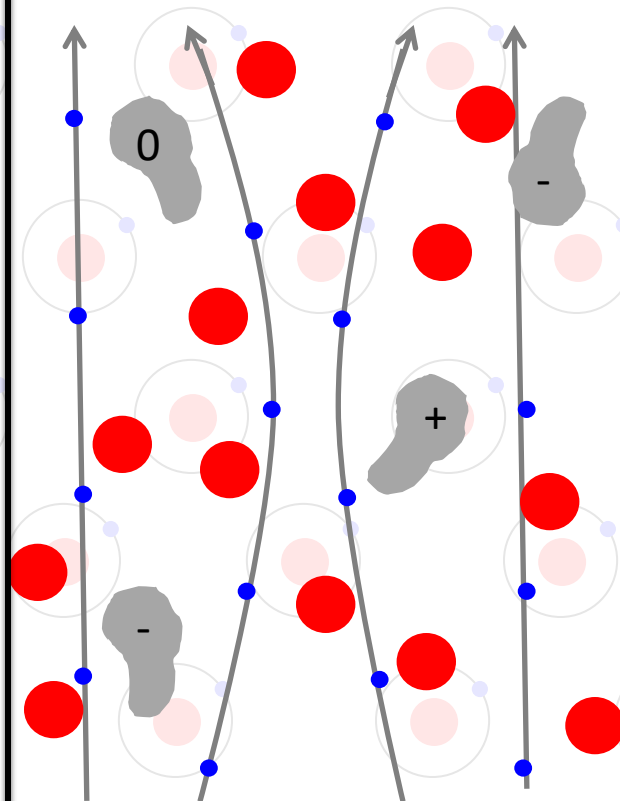


➤ Non-zero resistivity & conductivity

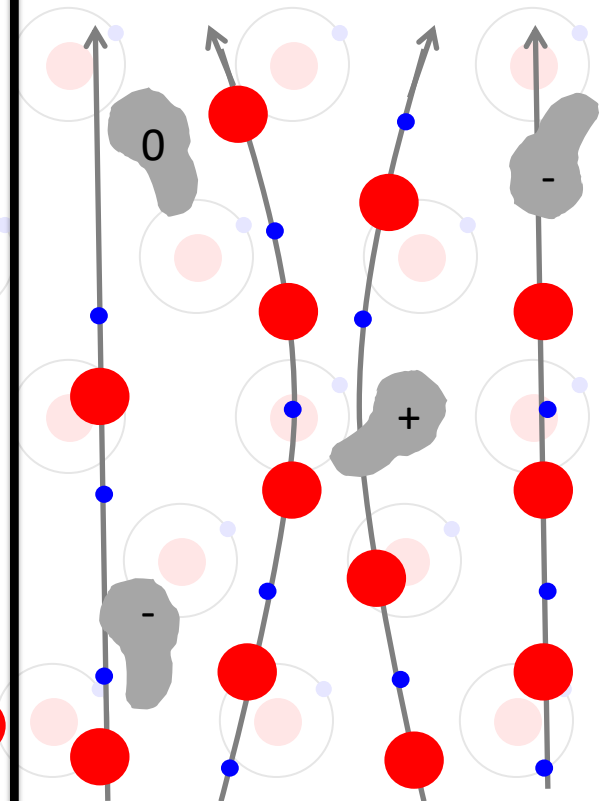
➤ Ions, electrons & neutrals behaviour is environment-dependent



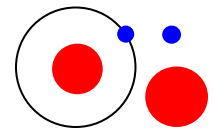
Ohmic Resistivity



Hall Effect

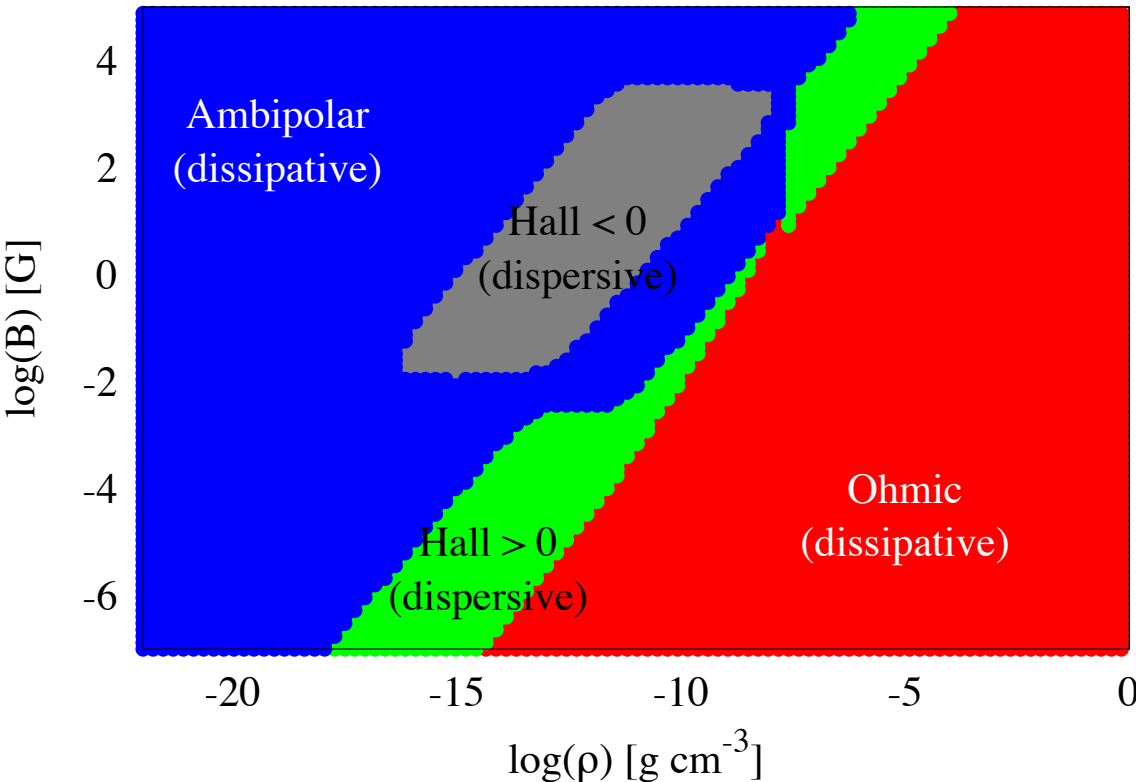


Ambipolar Diffusion

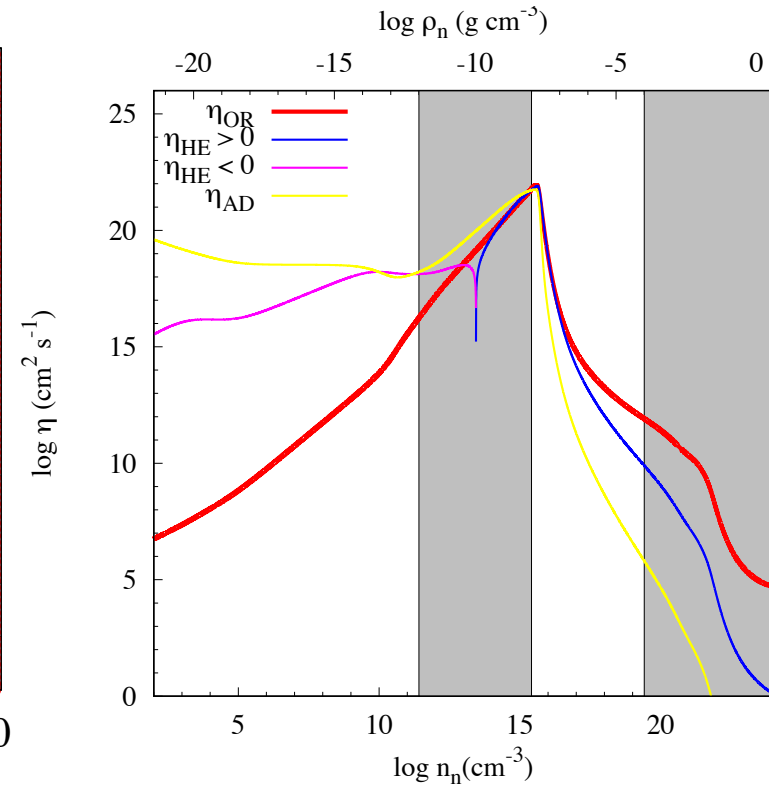


Non-ideal magnetohydrodynamics

Phase space diagram

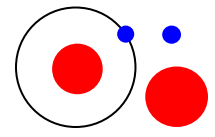


Coefficients
(for a star-forming model)



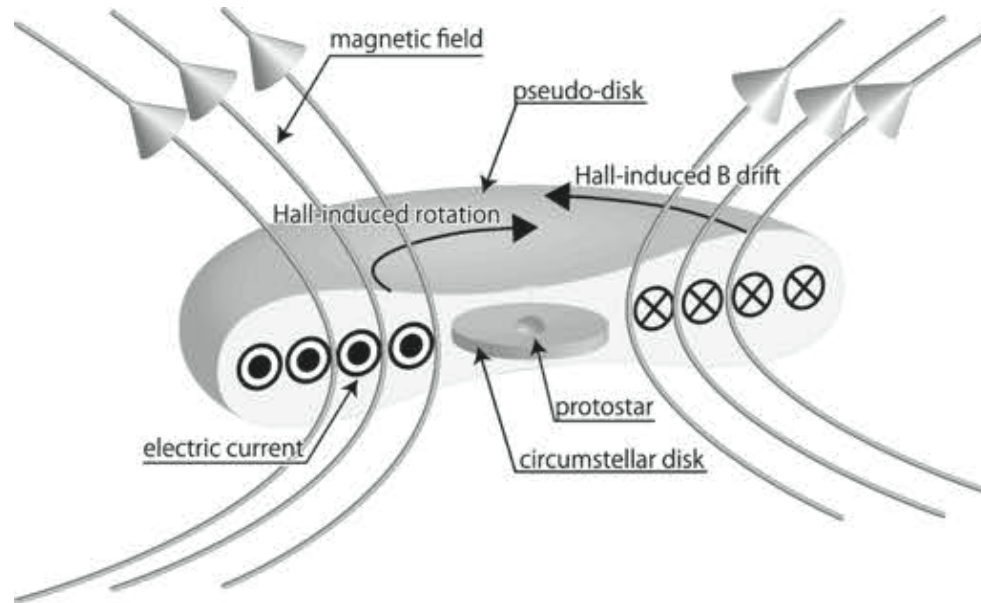
➤ Values dependent on microphysics:

➤ Grain size, ionised species, cosmic ray ionisation rate



Non-ideal magnetohydrodynamics: The Hall effect

➤ Image assumes $\eta_{\text{HE}} < 0$ (reasonable for star formation; Wurster 2016; Marchand + 2016)



$$\left. \frac{d\mathbf{B}}{dt} \right|_{\text{OR}} = -\nabla \times [\eta_{\text{OR}} (\nabla \times \mathbf{B})]$$

$$\left. \frac{d\mathbf{B}}{dt} \right|_{\text{HE}} = -\nabla \times [\eta_{\text{HE}} (\nabla \times \mathbf{B}) \times \hat{\mathbf{B}}]$$

$$\left. \frac{d\mathbf{B}}{dt} \right|_{\text{AD}} = \nabla \times \left\{ \eta_{\text{AD}} [(\nabla \times \mathbf{B}) \times \hat{\mathbf{B}}] \times \hat{\mathbf{B}} \right\}$$

For magnetic field reversal, substitute $\mathbf{B} \rightarrow -\mathbf{B}$:

$$\left. \frac{d(-\mathbf{B})}{dt} \right|_{\text{OR}} = -\nabla \times \{ \eta_{\text{OR}} [\nabla \times (-\mathbf{B})] \}$$

$$\left. \frac{d(-\mathbf{B})}{dt} \right|_{\text{HE}} = -\nabla \times \left\{ \eta_{\text{HE}} [\nabla \times (-\mathbf{B})] \times (-\hat{\mathbf{B}}) \right\}$$

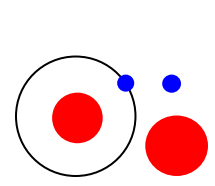
$$\left. \frac{d(-\mathbf{B})}{dt} \right|_{\text{AD}} = \nabla \times \left\{ \eta_{\text{AD}} \left[[\nabla \times (-\mathbf{B})] \times (-\hat{\mathbf{B}}) \right] \times (-\hat{\mathbf{B}}) \right\}$$

Simplify:

$$\left. \frac{d\mathbf{B}}{dt} \right|_{\text{OR}} = -\nabla \times [\eta_{\text{OR}} (\nabla \times \mathbf{B})]$$

$$\left. \frac{d\mathbf{B}}{dt} \right|_{\text{HE}} = \nabla \times [\eta_{\text{HE}} (\nabla \times \mathbf{B}) \times \hat{\mathbf{B}}]$$

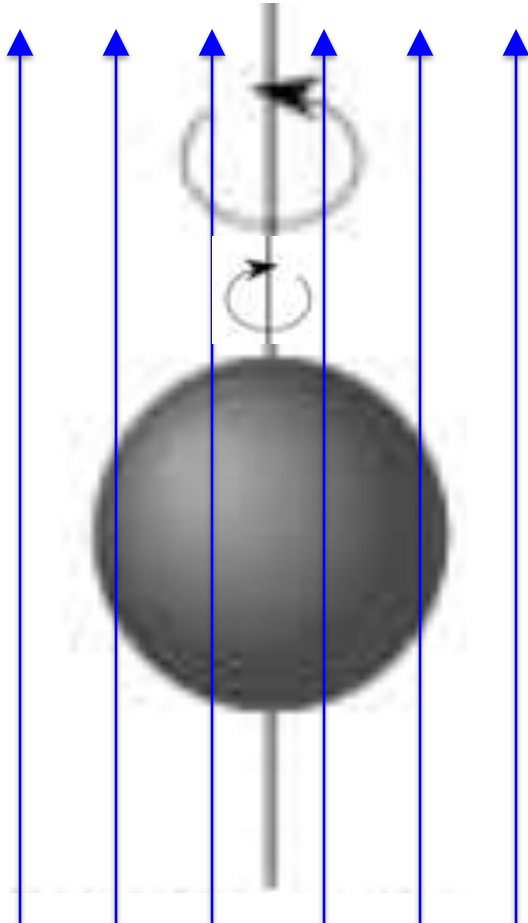
$$\left. \frac{d\mathbf{B}}{dt} \right|_{\text{AD}} = \nabla \times \left\{ \eta_{\text{AD}} [(\nabla \times \mathbf{B}) \times \hat{\mathbf{B}}] \times \hat{\mathbf{B}} \right\}$$



Non-ideal magnetohydrodynamics: The Hall effect

➤ Depending on the relative orientation of L & B , the Hall-induced rotation will contribute to or detract from the initial rotation

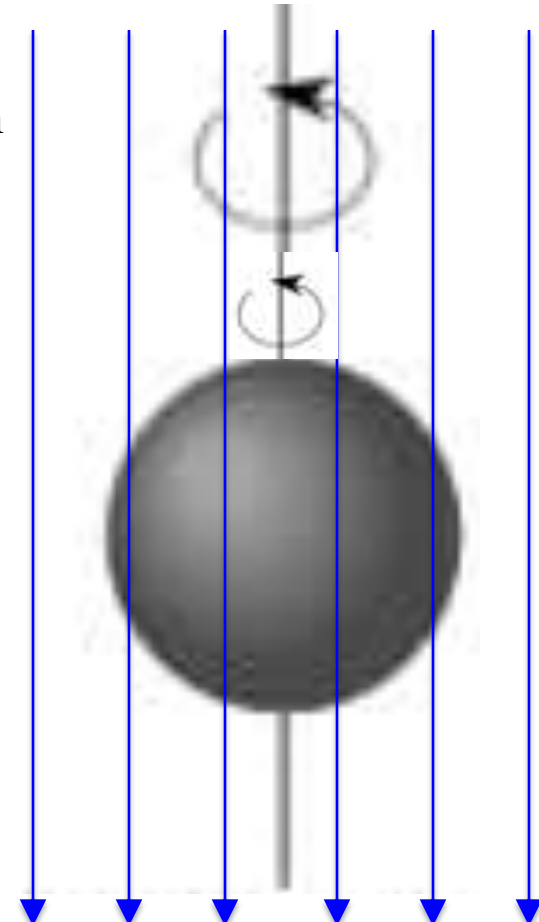
L & B are aligned

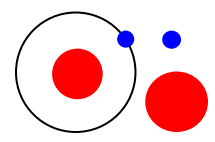


Direction of initial rotation

Hall-induced rotation

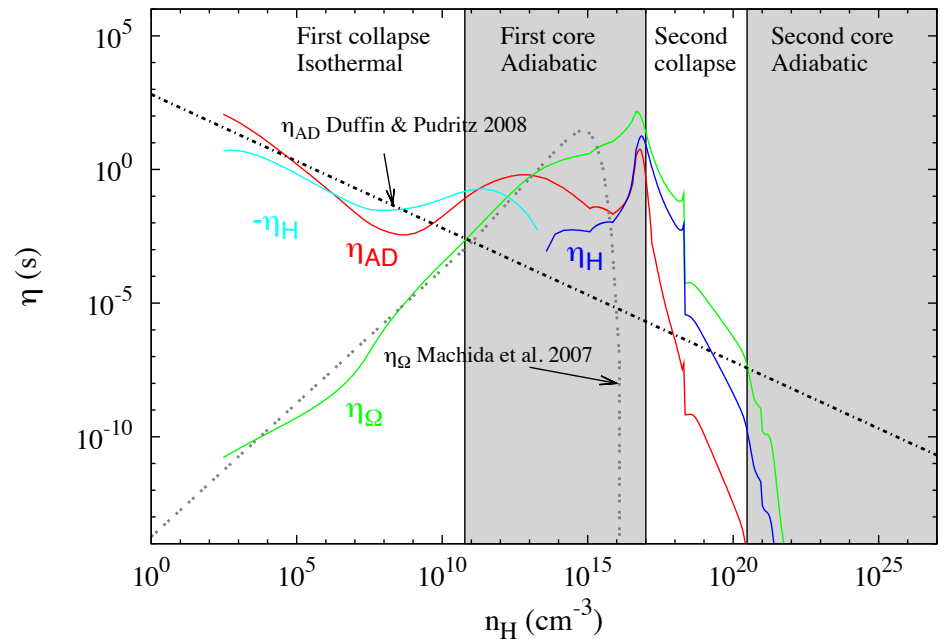
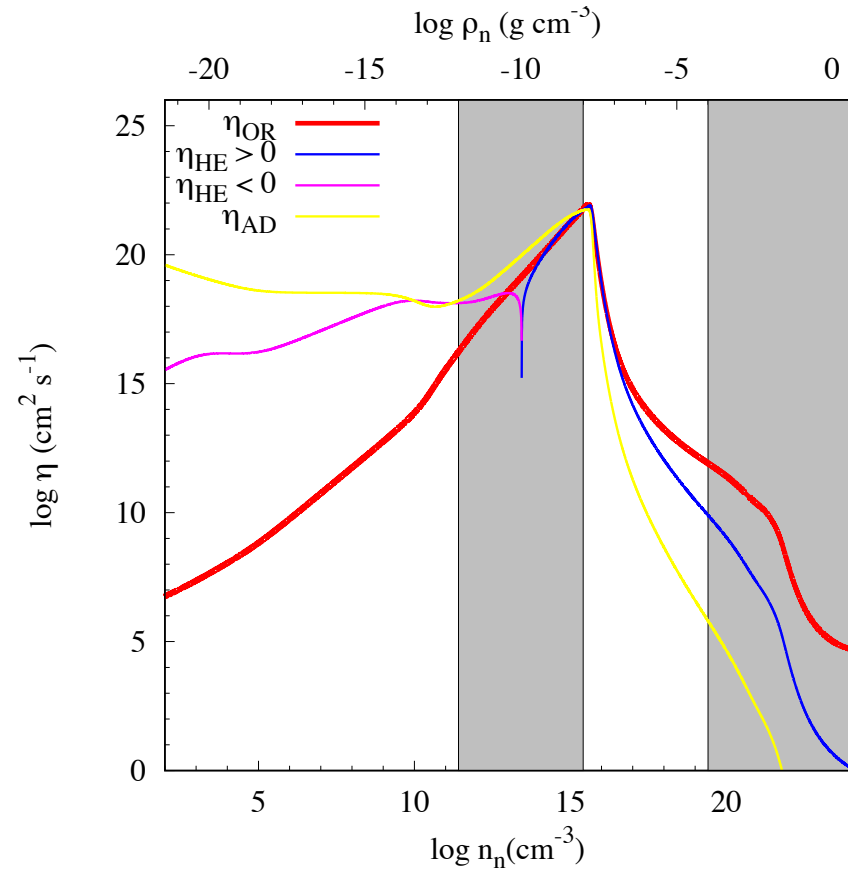
L & B are anti-aligned

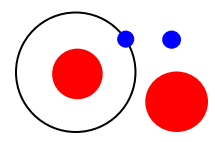




Non-ideal magnetohydrodynamics: Calculations

➤ Algorithm comparison (both models use their default parameters)



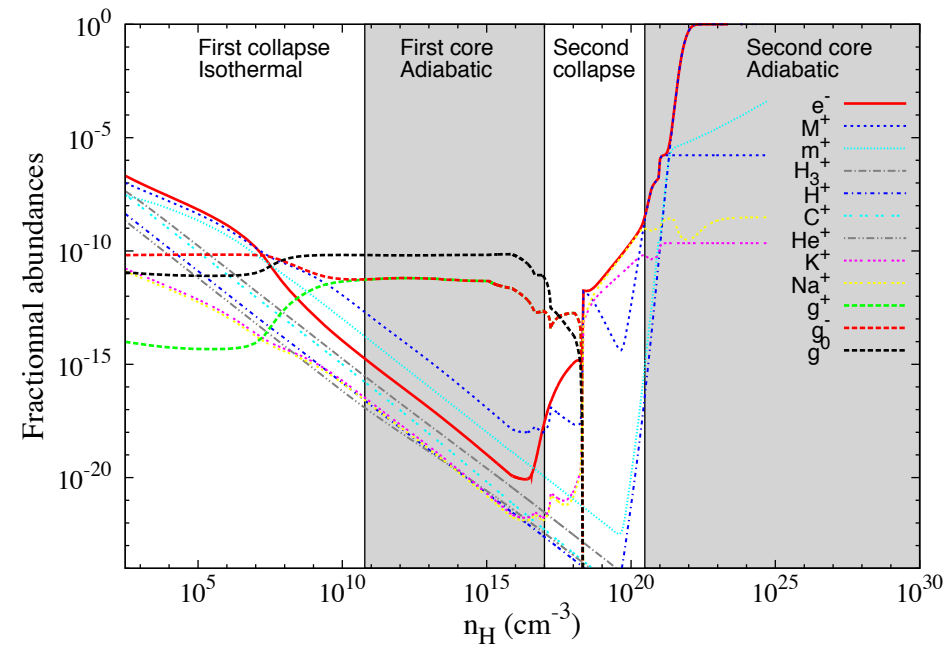
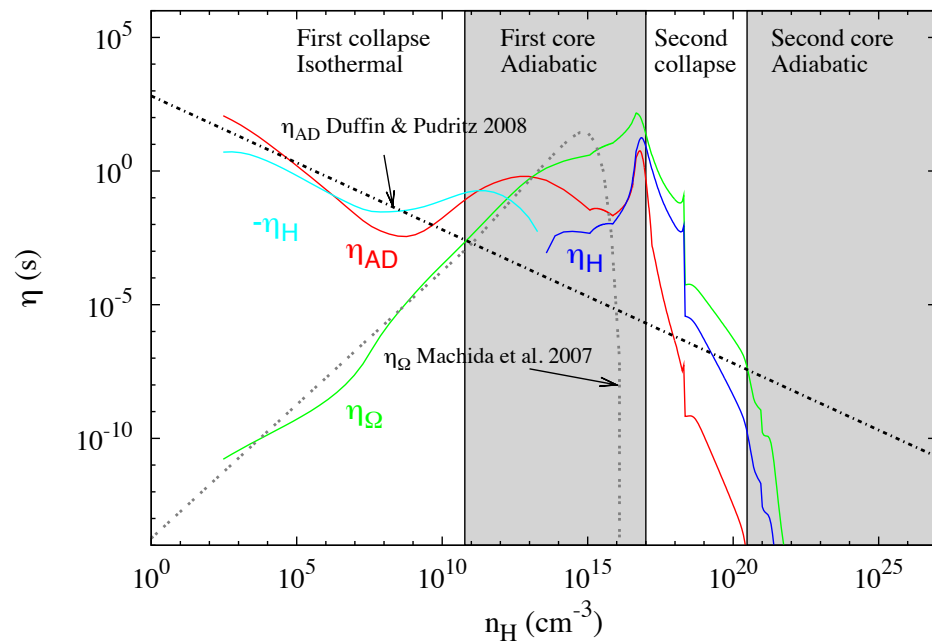


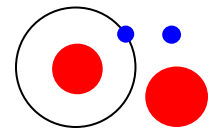
Non-ideal magnetohydrodynamics: Chemical models

➤ Models are chemically dependent

➤ More precise chemical network and abundance yields more precise coefficients

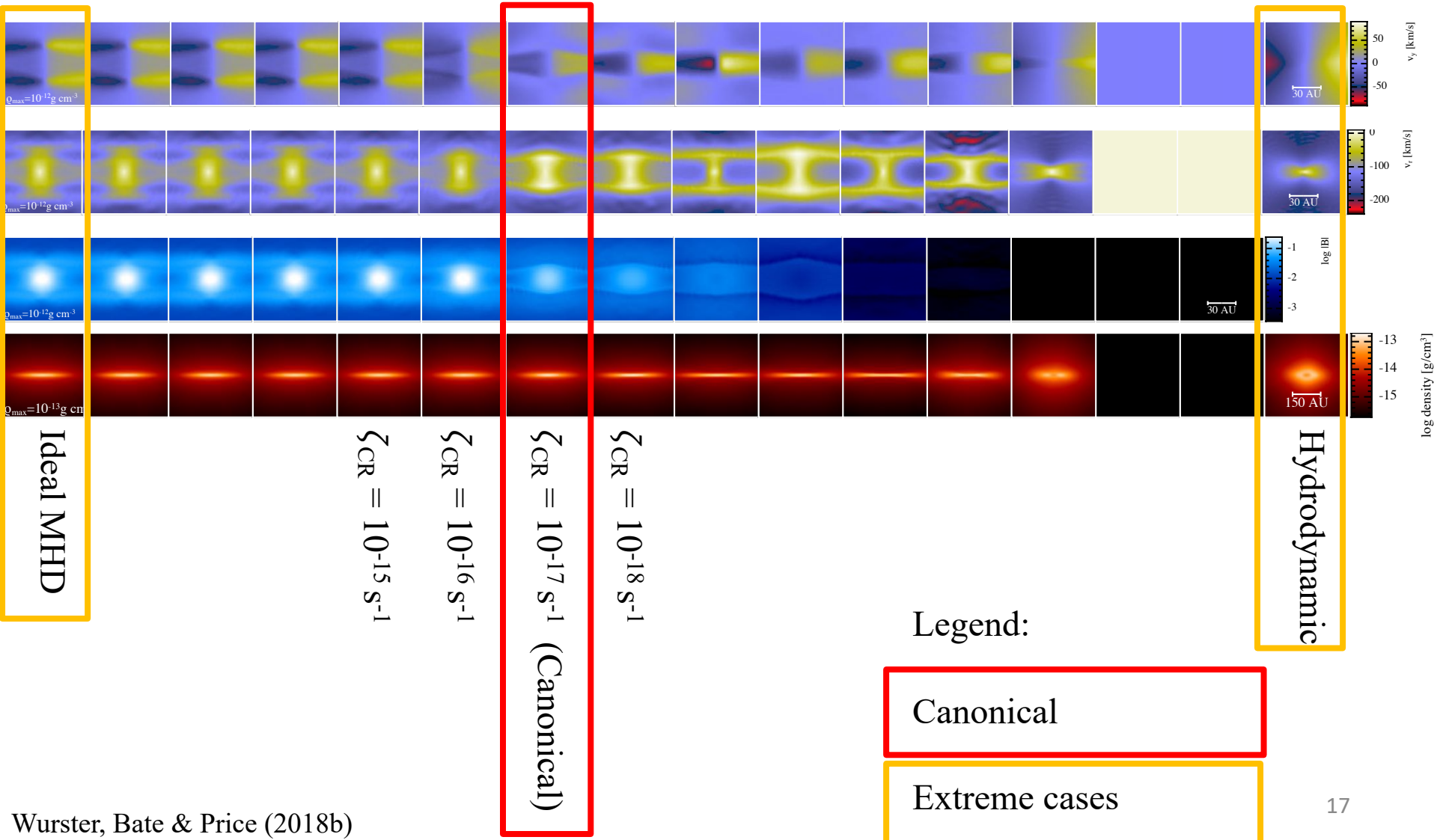
➤ Still highly dependent on cosmic ray ionisation rate (results not shown here)

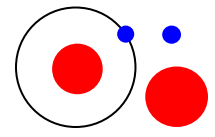




Non-ideal magnetohydrodynamics: Cosmic ray ionisation rate

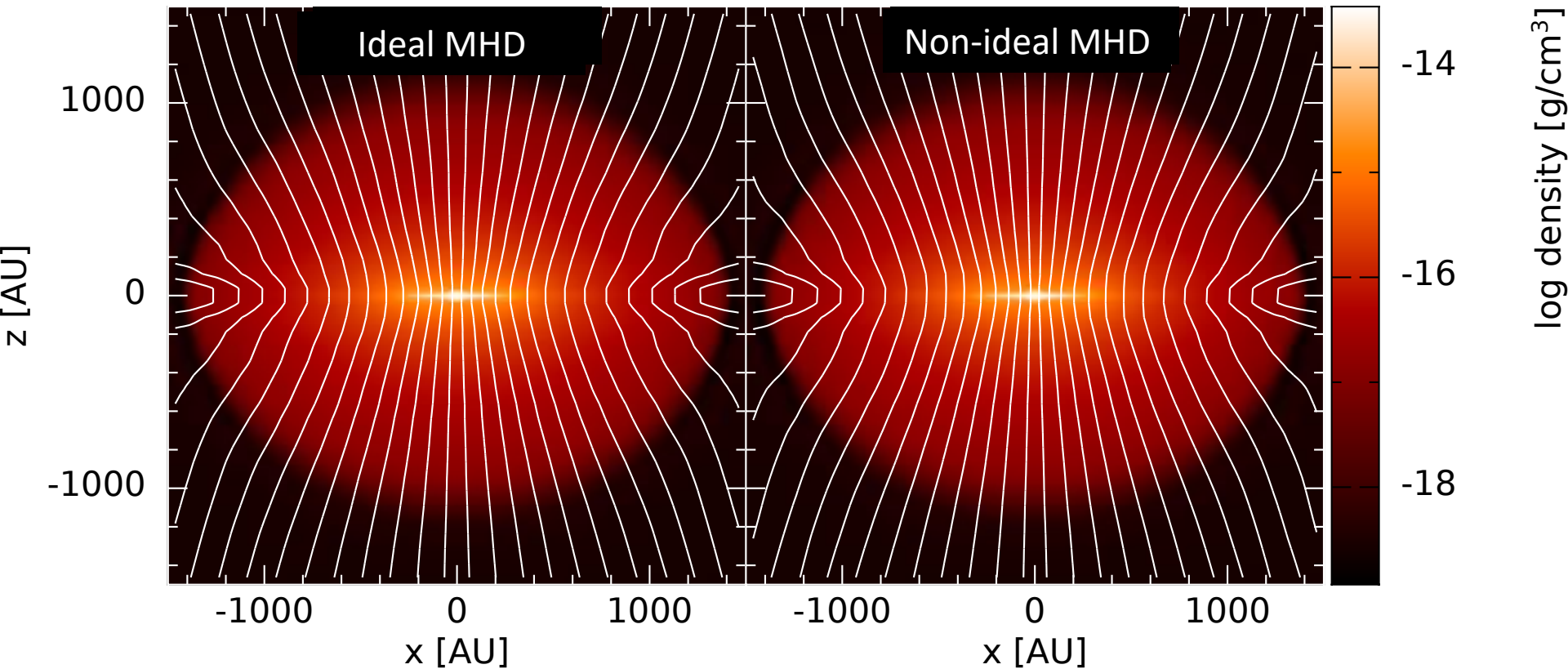
➤ Images: v_y , v_r , $\log(B)$, $\log(\rho)$ at $\rho_{\max} = 10^{-12} \text{ g cm}^{-3}$

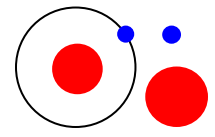




Non-ideal magnetohydrodynamics

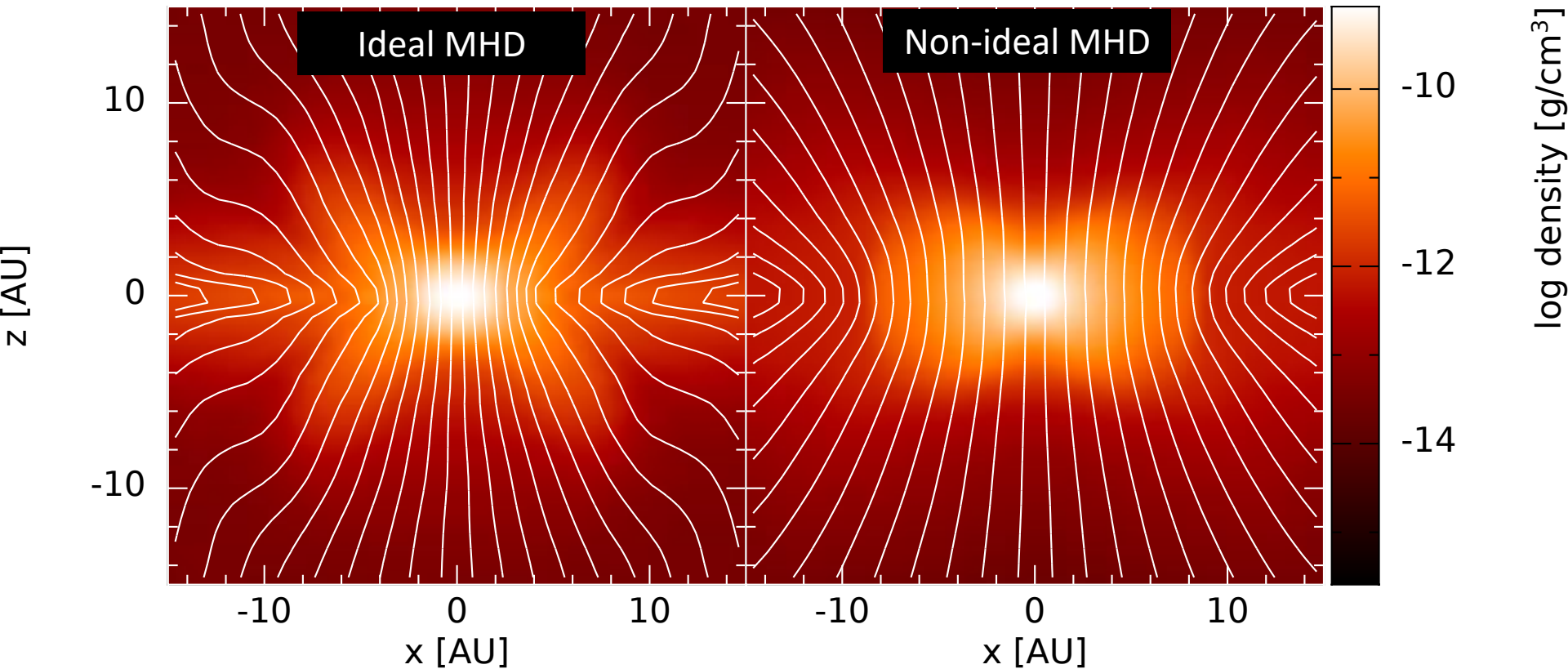
- Strong field; large scale structure

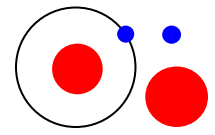




Non-ideal magnetohydrodynamics

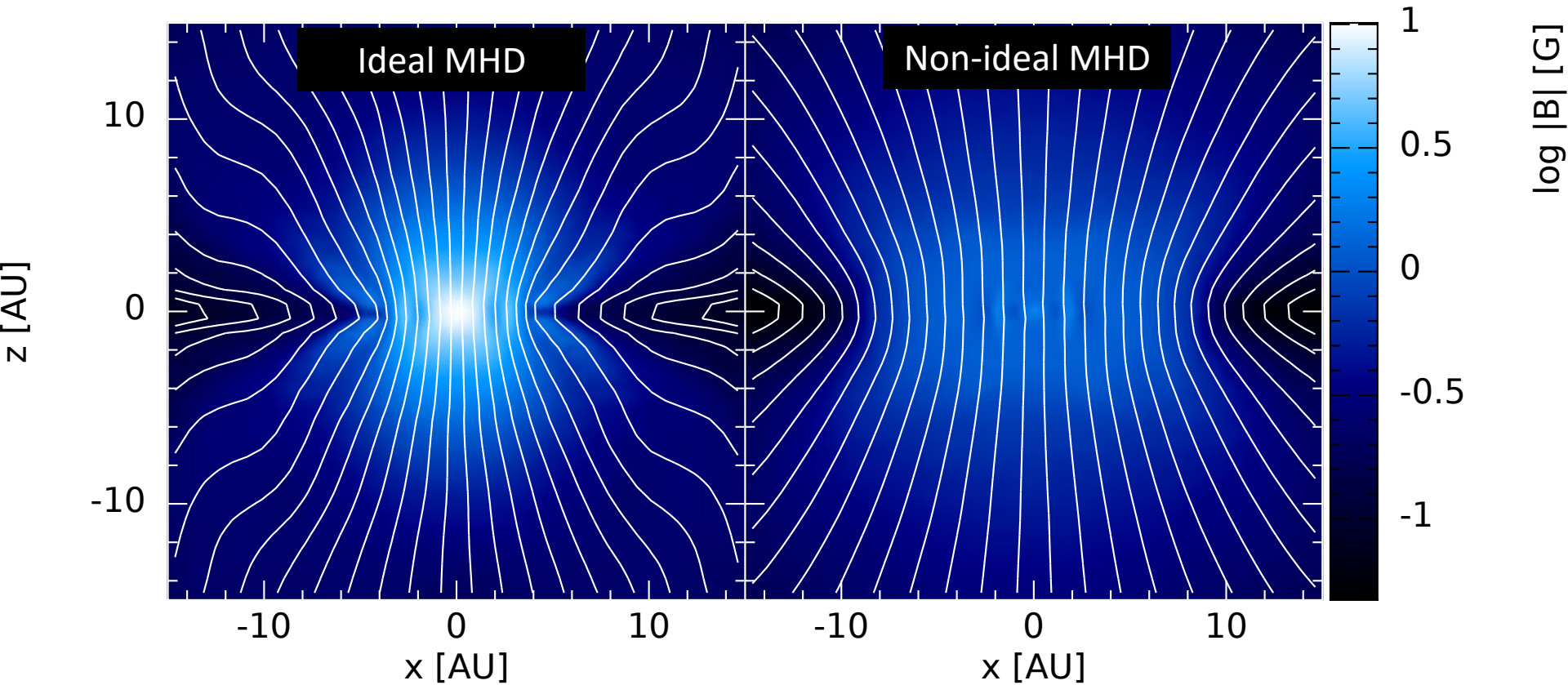
- Strong field; small scale structure



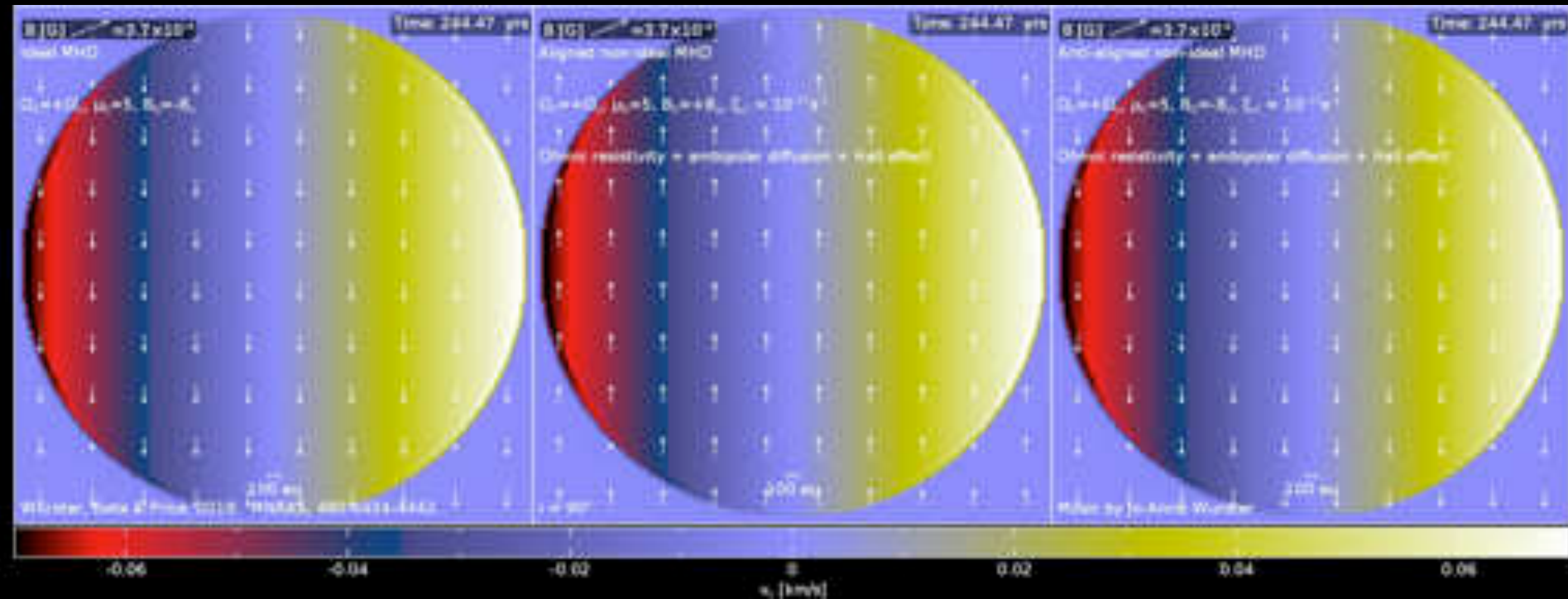


Non-ideal magnetohydrodynamics

- Strong field; small scale structure



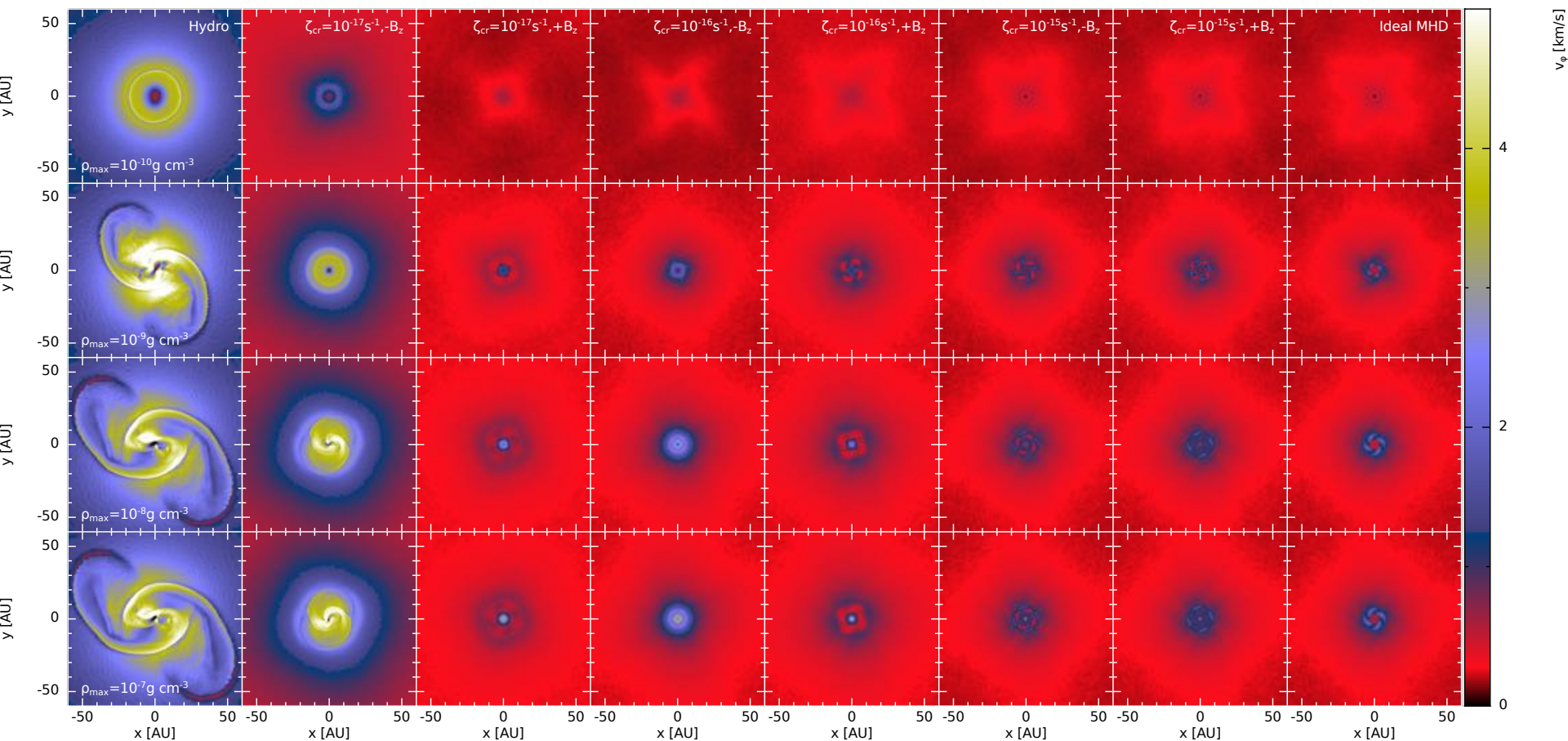
Formation of a low-mass star



<https://www.youtube.com/watch?v=2SQxgXbdJyg&t=4s>

Rotationally supported discs

➤ Discs form in the hydrodynamics model and the non-ideal model with $\zeta_{\text{cr}} = 10^{-17} \text{ s}^{-1}$ with $-B_z$



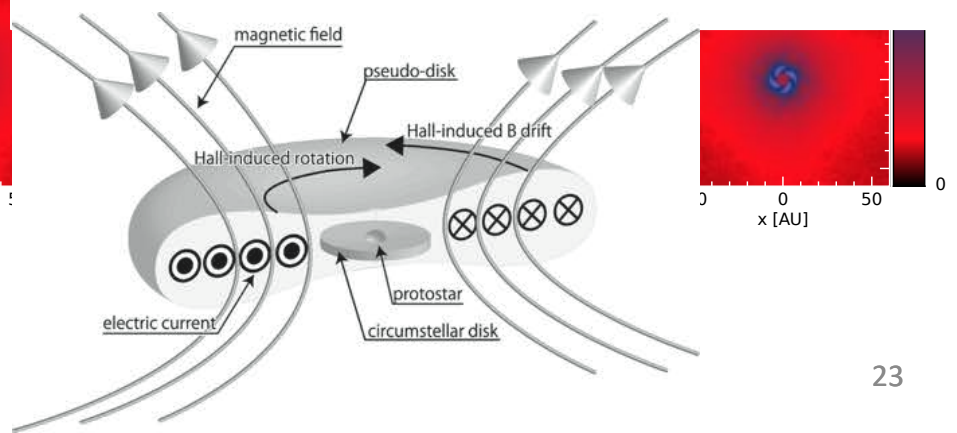
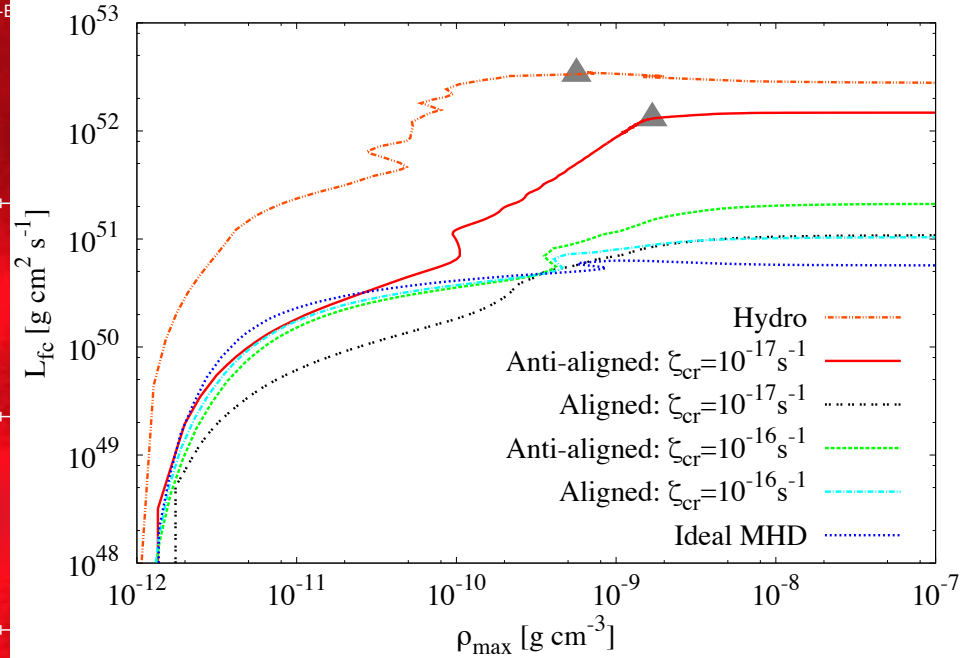
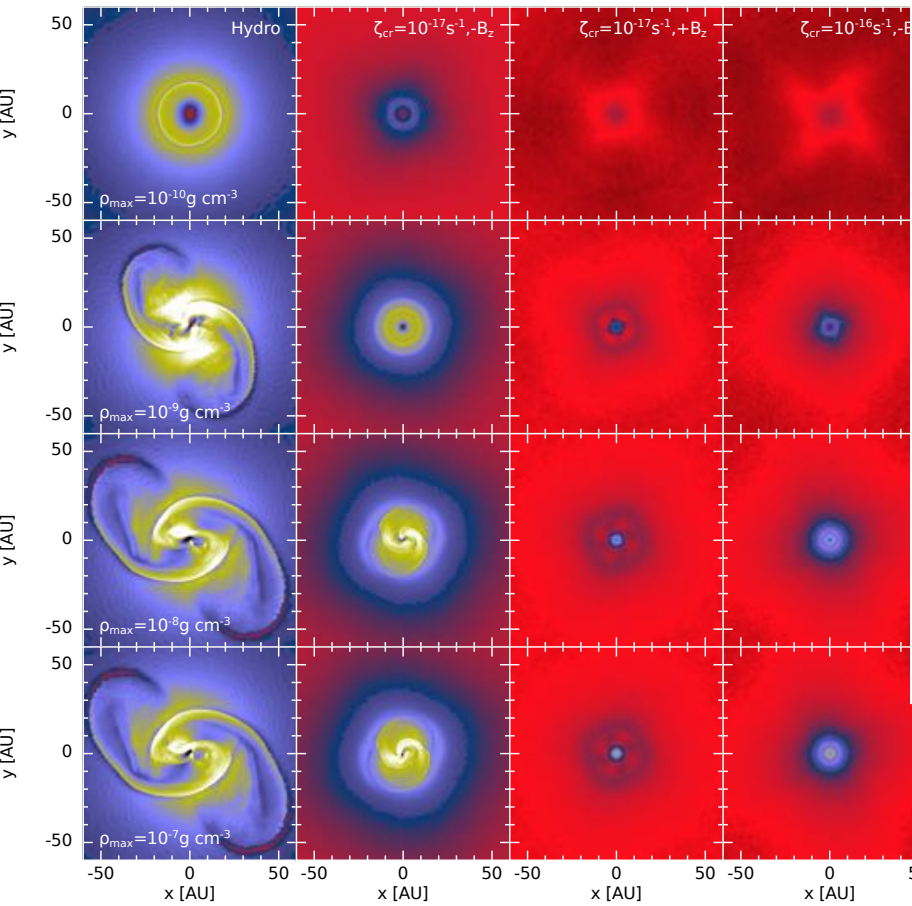
➤ Discs form during the first hydrostatic core phase

➤ Similar disc structure obtained by Tsukamoto+ (2015a) for $\zeta_{\text{cr}} = 10^{-17} \text{ s}^{-1}$ with $\pm B_z$

Wurster, Bate & Price (2018a,c) +

Rotationally supported discs

➤ Discs form in the hydrodynamics model and the non-ideal model with $\zeta_{\text{cr}} = 10^{-17} \text{ s}^{-1}$ with $-B_z$

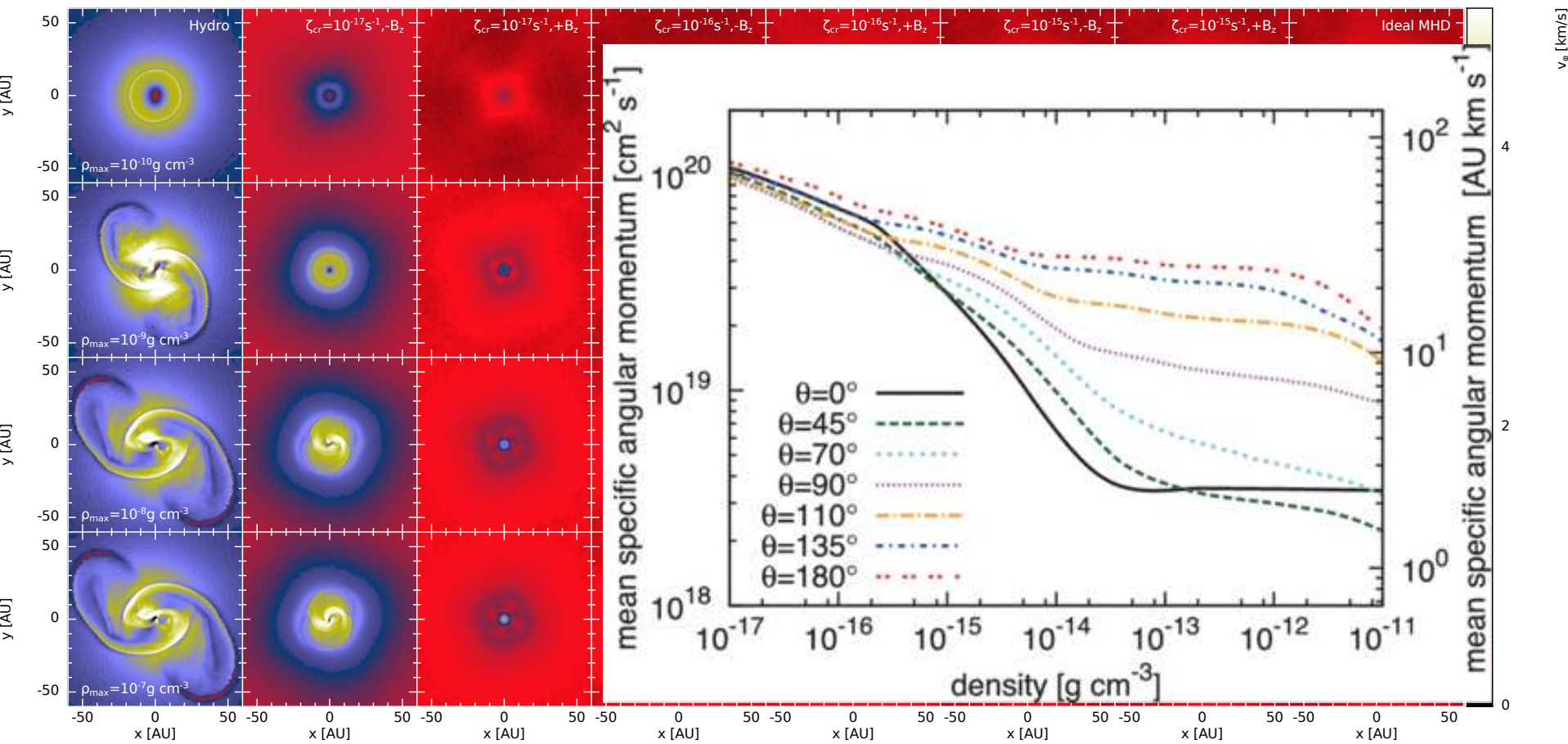


v_e [km/s]

0
50
x [AU]

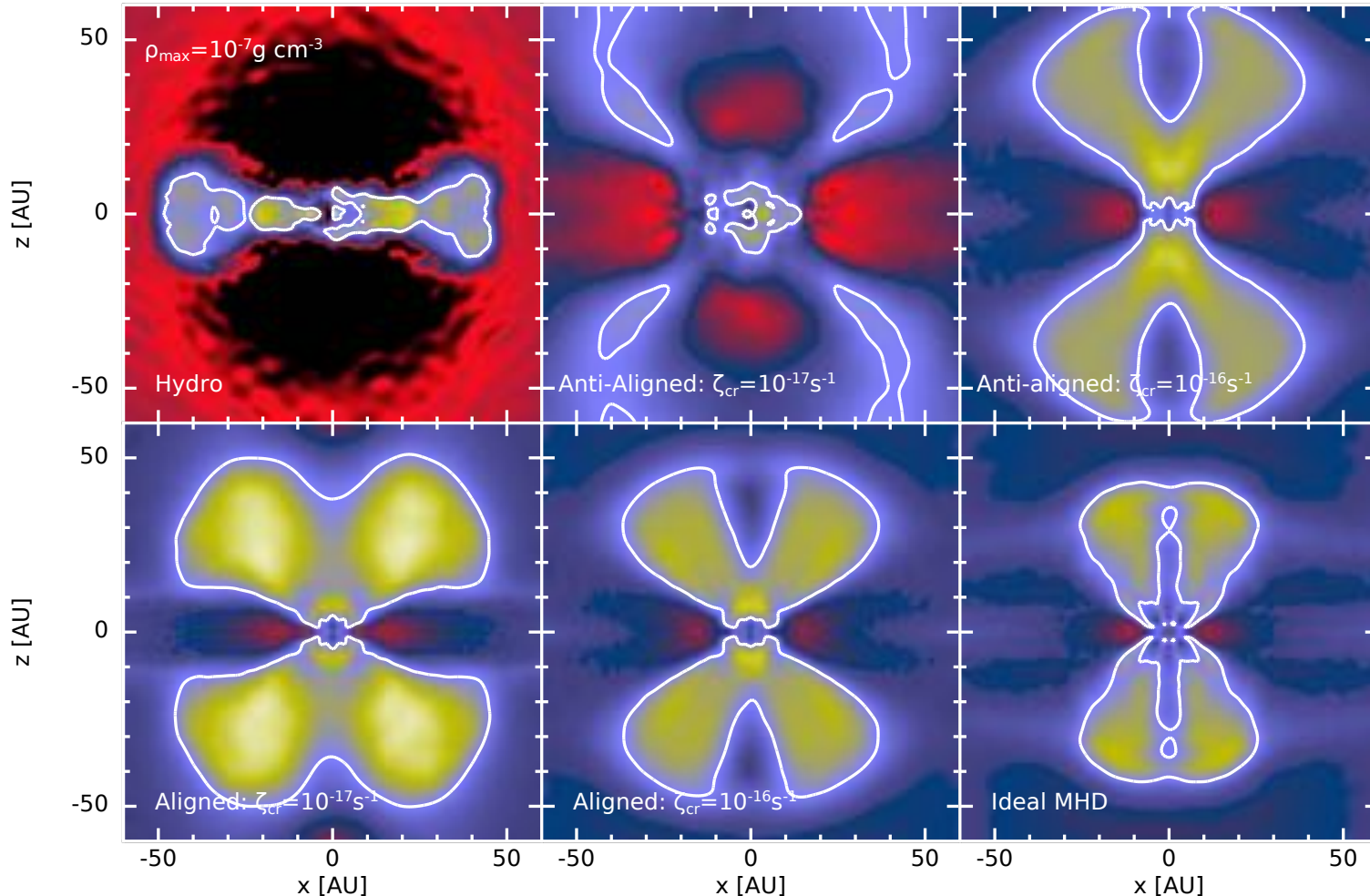
Rotationally supported discs

➤ Discs form in the hydrodynamics model and the non-ideal model with $\zeta_{cr} = 10^{-17} \text{ s}^{-1}$ with $-B_z$



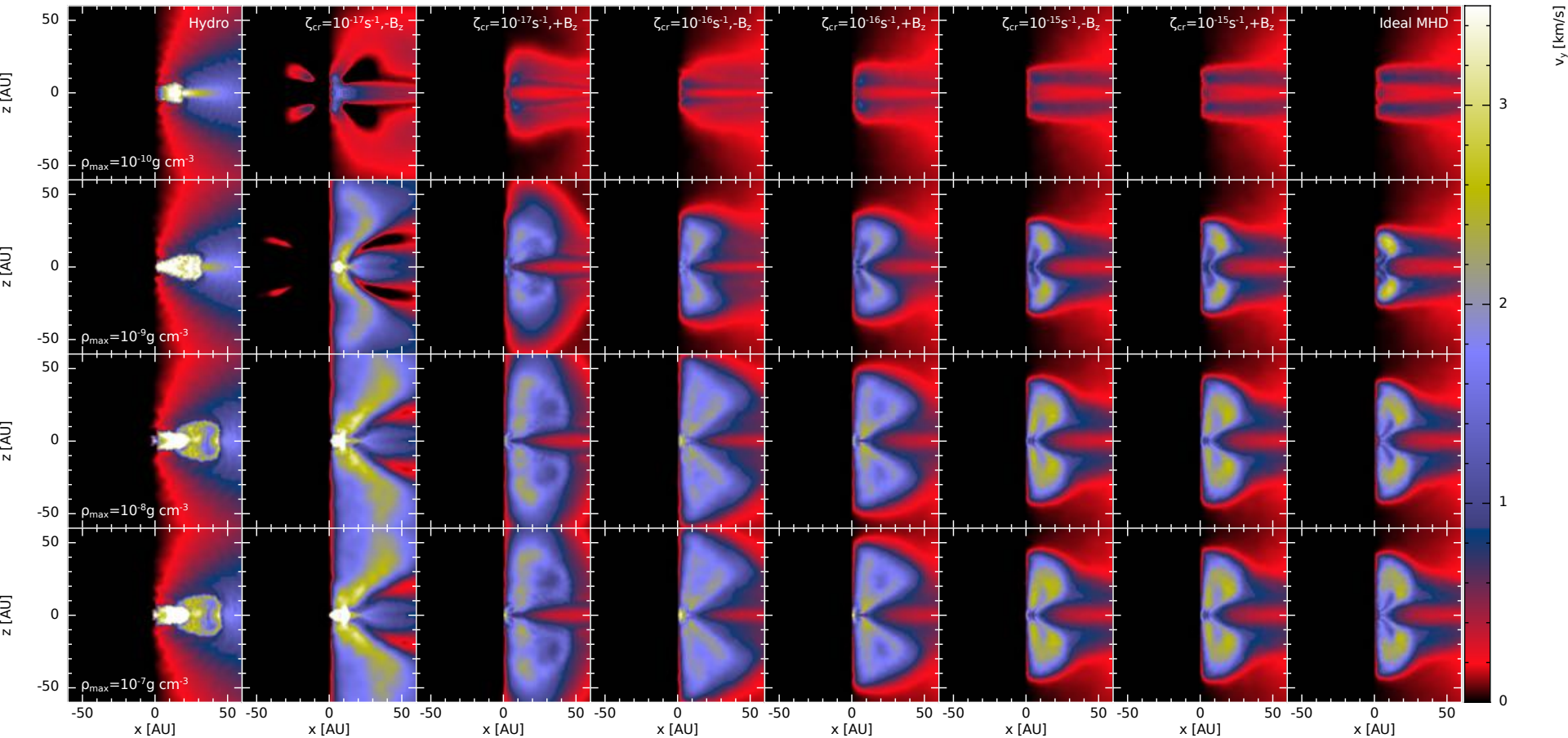
First core outflows

- Aligned magnetic fields enhance outflows; Anti-aligned magnetic fields suppress outflows

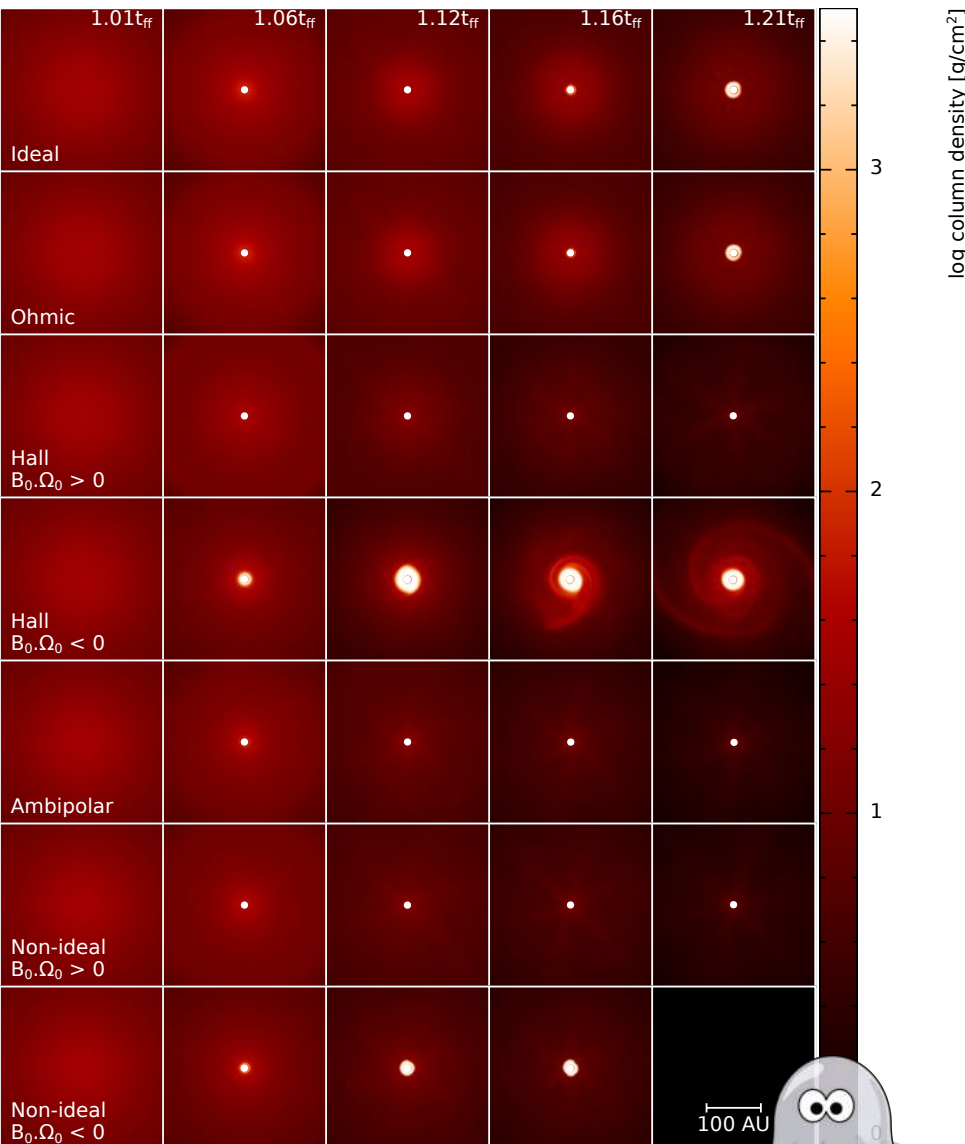


Large scale rotational velocity

- Rotational speed increases as ionisation rate decreases
- Counter-rotating envelopes are a transient feature in the model with $\zeta_{\text{cr}} = 10^{-17} \text{ s}^{-1}$ with $-B_z$



Non-Ideal MHD Components

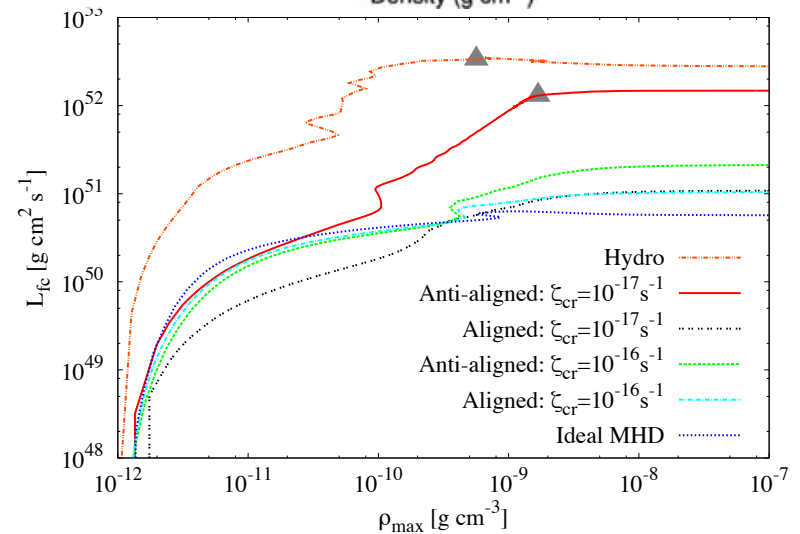
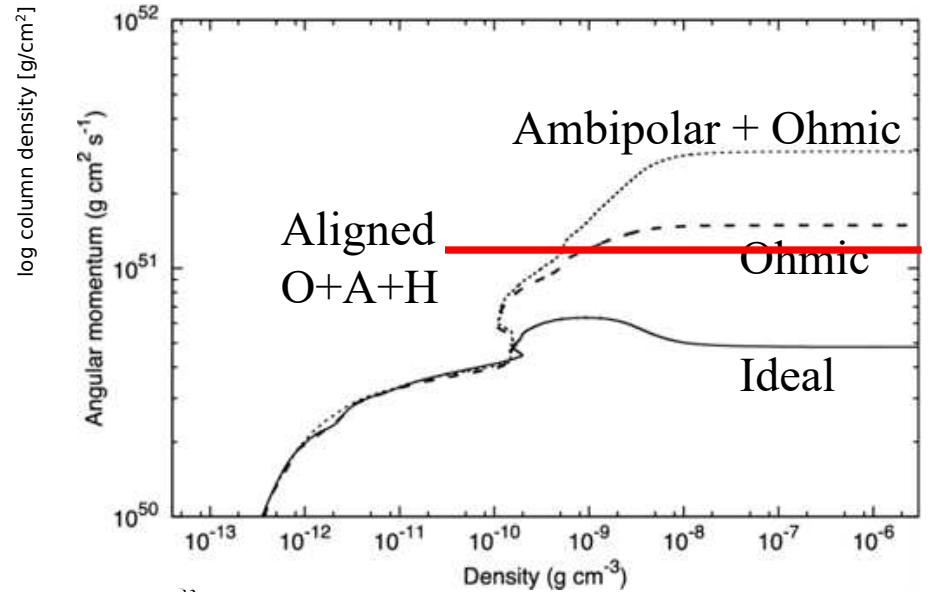
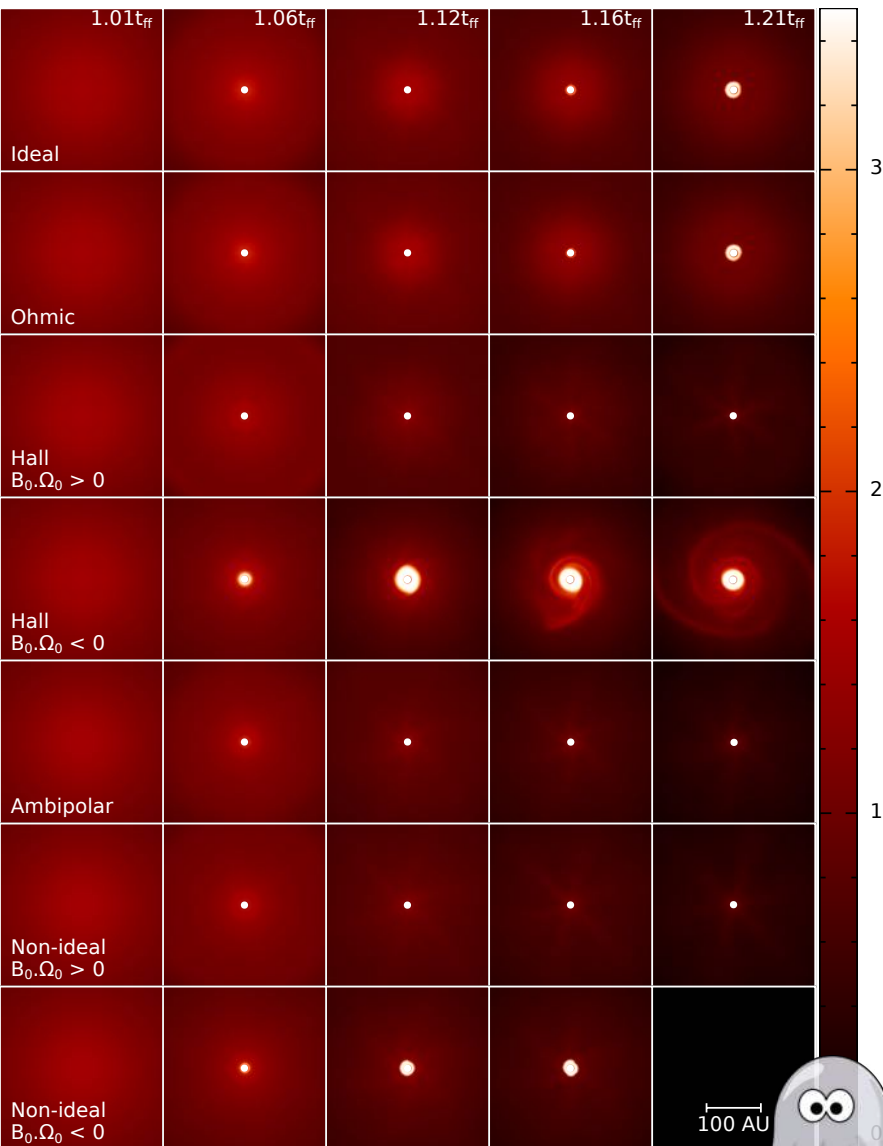


- Multiple conclusions in the literature regarding disc formation with Ohmic resistivity and/or ambipolar diffusion
- Likely possible to form small 1-5au discs in the long term with only Ohmic and/or ambipolar (Dapp and Basu 2010, Machida+ 2011, Dapp+ 2012, Tomida+ 2015, Tsukamoto+ 2015a, Masson+ 2016)
- Hennebelle et al. (2016) predicts 18au discs for ambipolar diffusion only
- Models to the left include a 6.7au sink particle
- Open question: *When do discs form?*



Non-Ideal MHD Components

Anti-aligned O+A+H



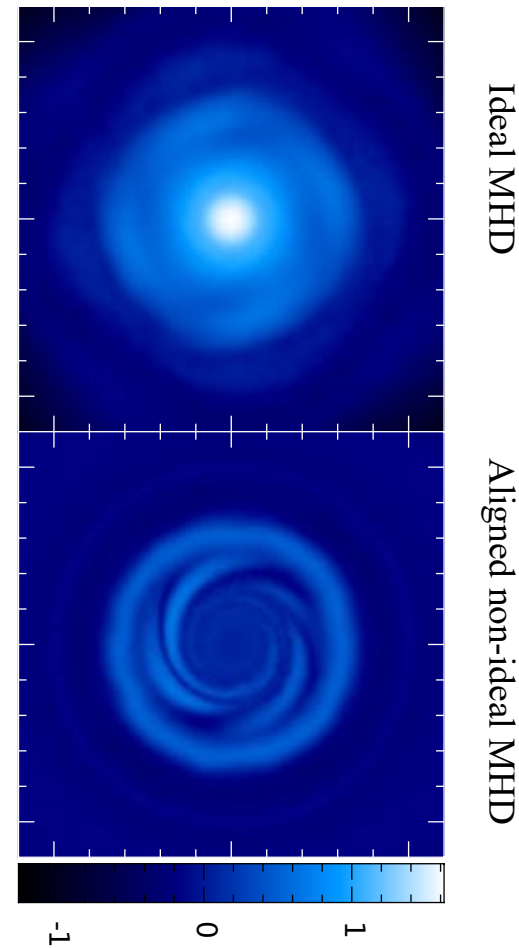
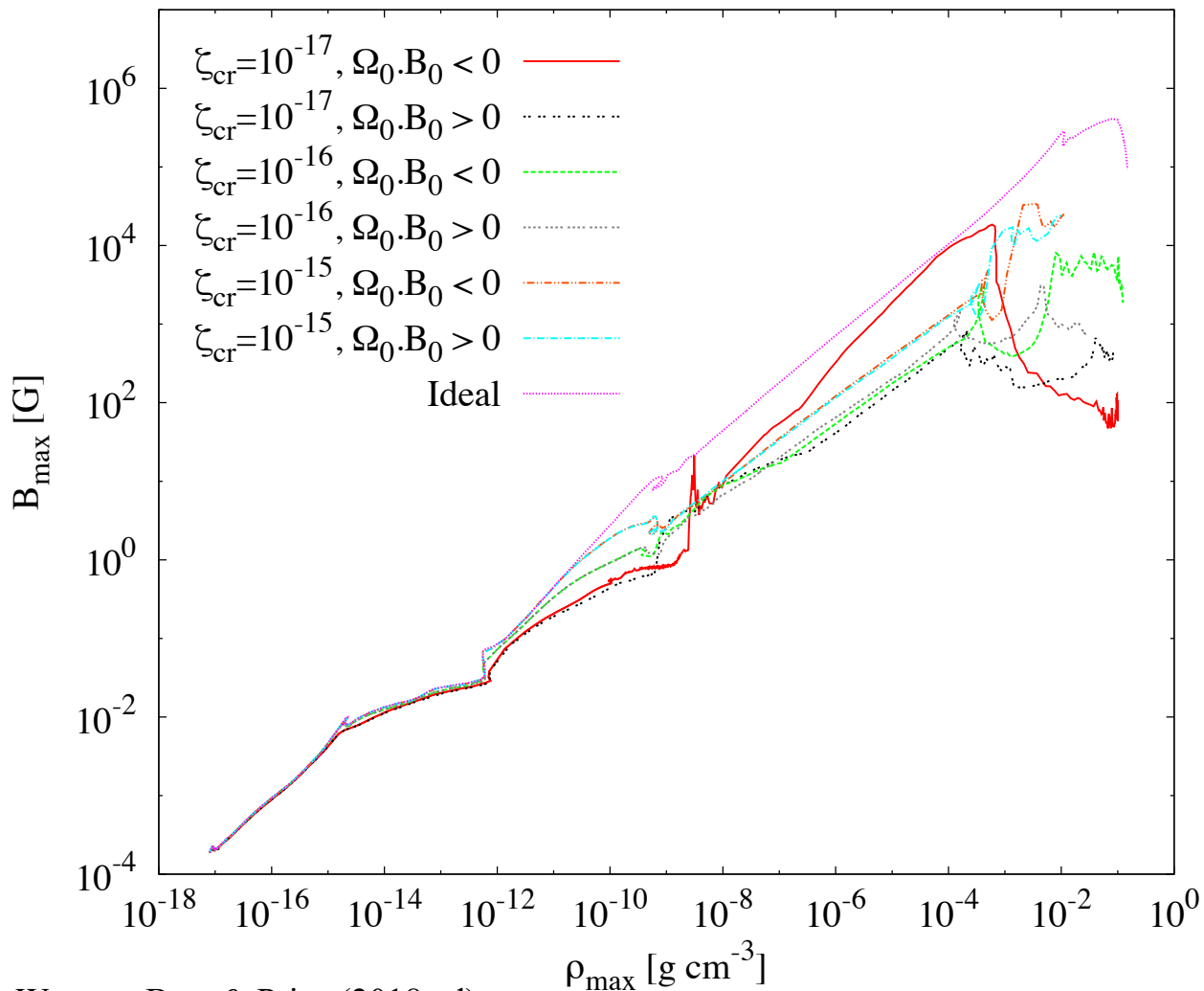
Top: Tsukamoto+ (2015b)

Bottom: Wurster, Bate & Price (2018c)



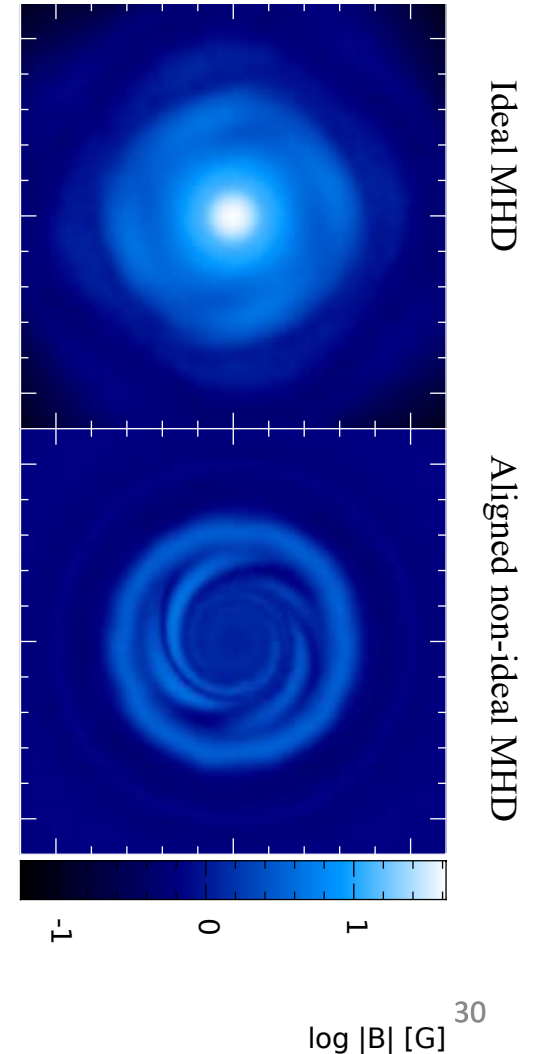
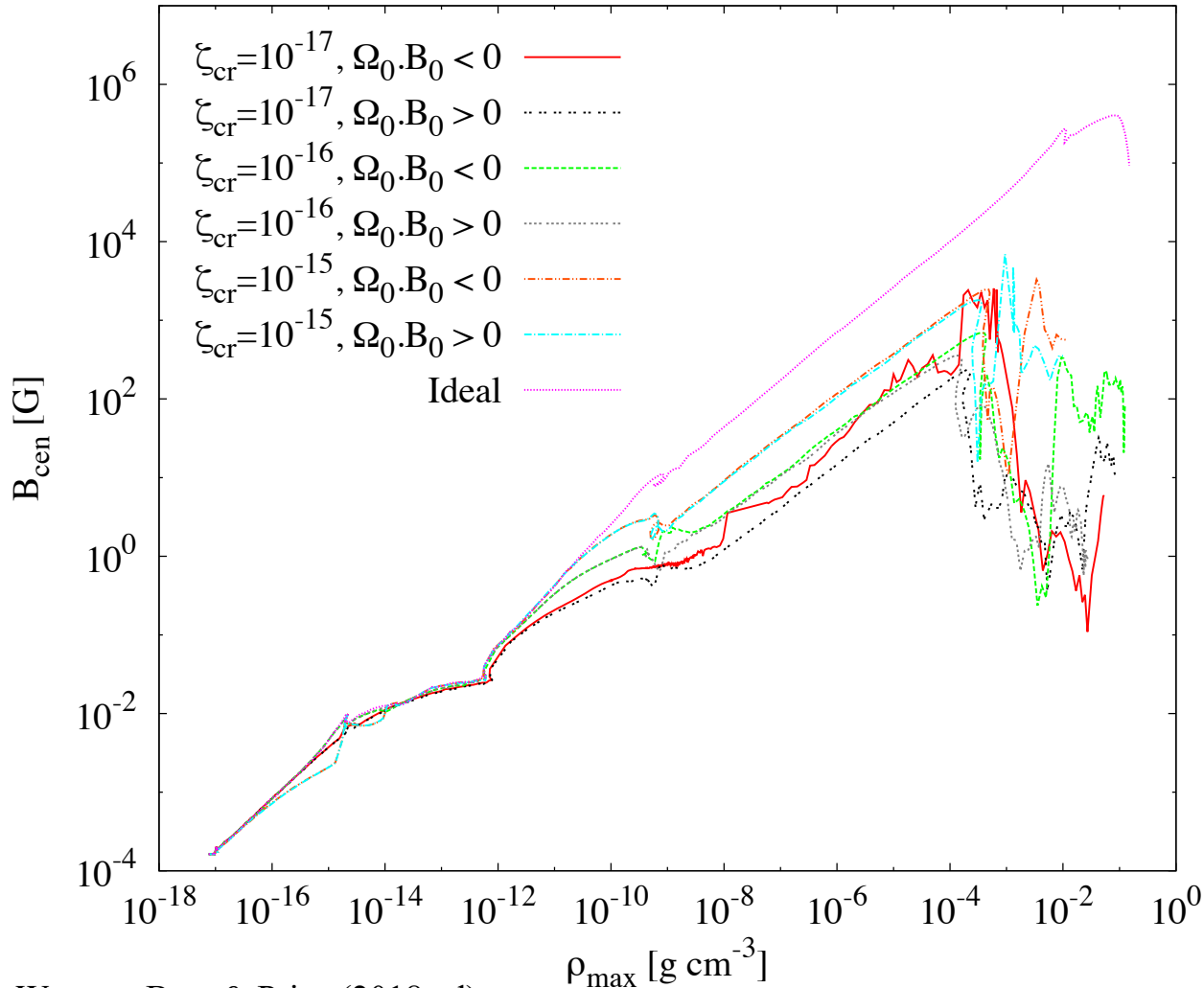
Magnetic field evolution

- Non-ideal effects decrease the magnetic field strength, starting in the first core phase



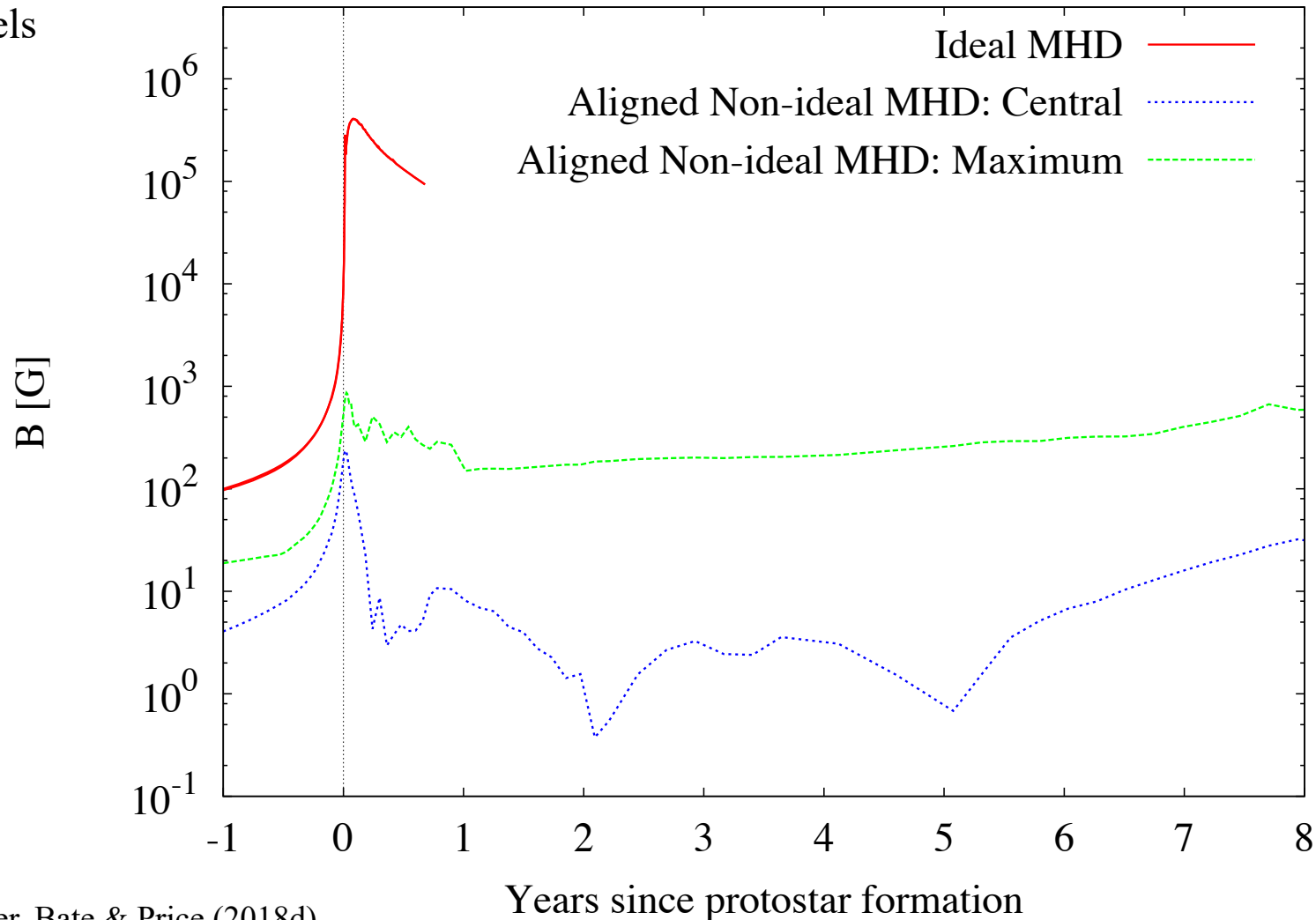
Magnetic field evolution

- The maximum magnetic field strength is not at the centre of the core in the non-ideal models
- Magnetic wall forms in non-ideal MHD models (Tassis & Mouschovias, 2005)

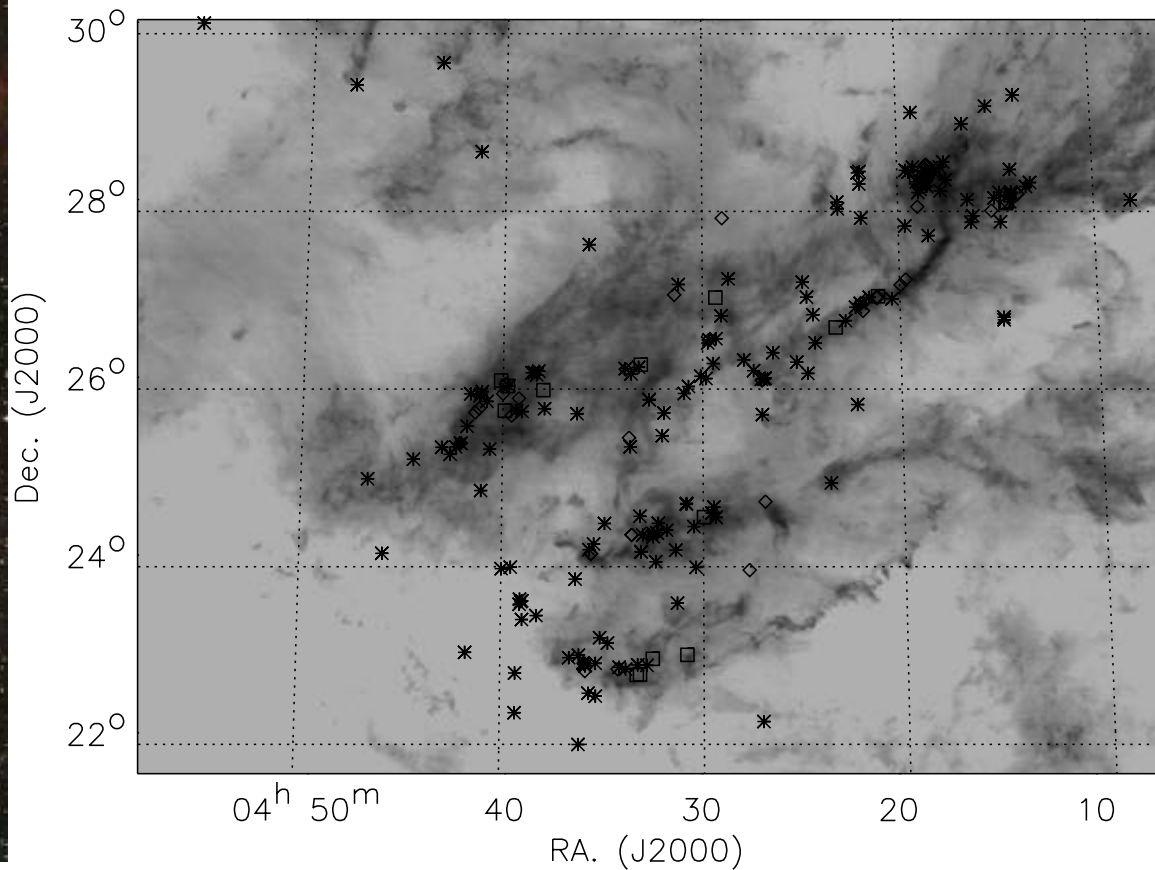
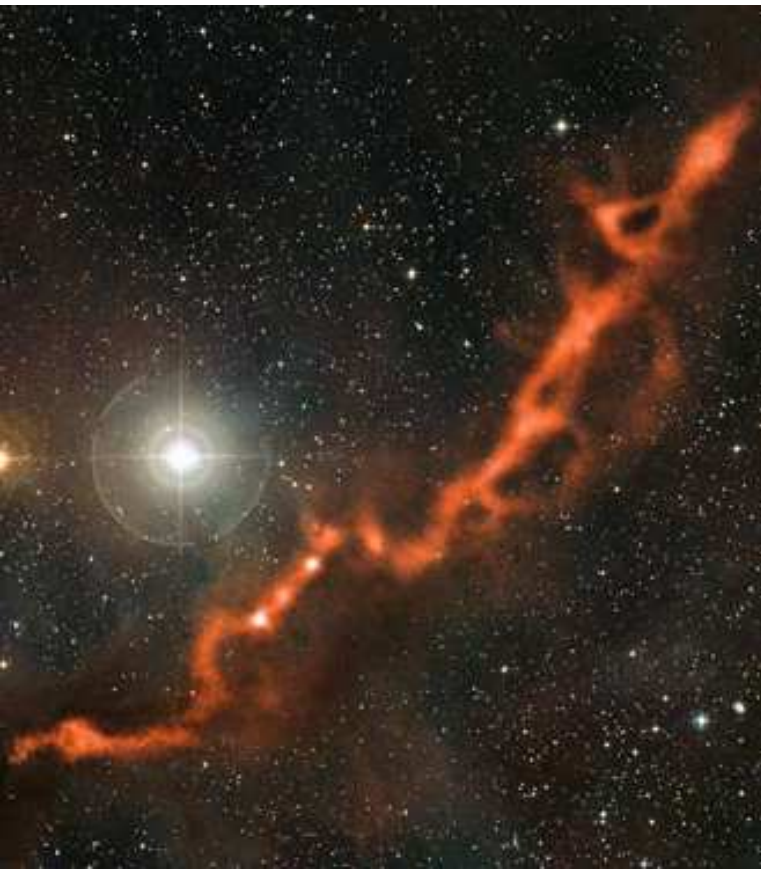


Magnetic field evolution

- Strong kG magnetic fields are observed in stars. Are they fossil, or dynamo-generated?
- Most likely dynamo-generated since the fossil magnetic field is $\ll 1000\text{G}$ in the non-ideal models

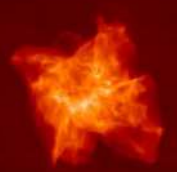


Importance of stars: Stellar nurseries

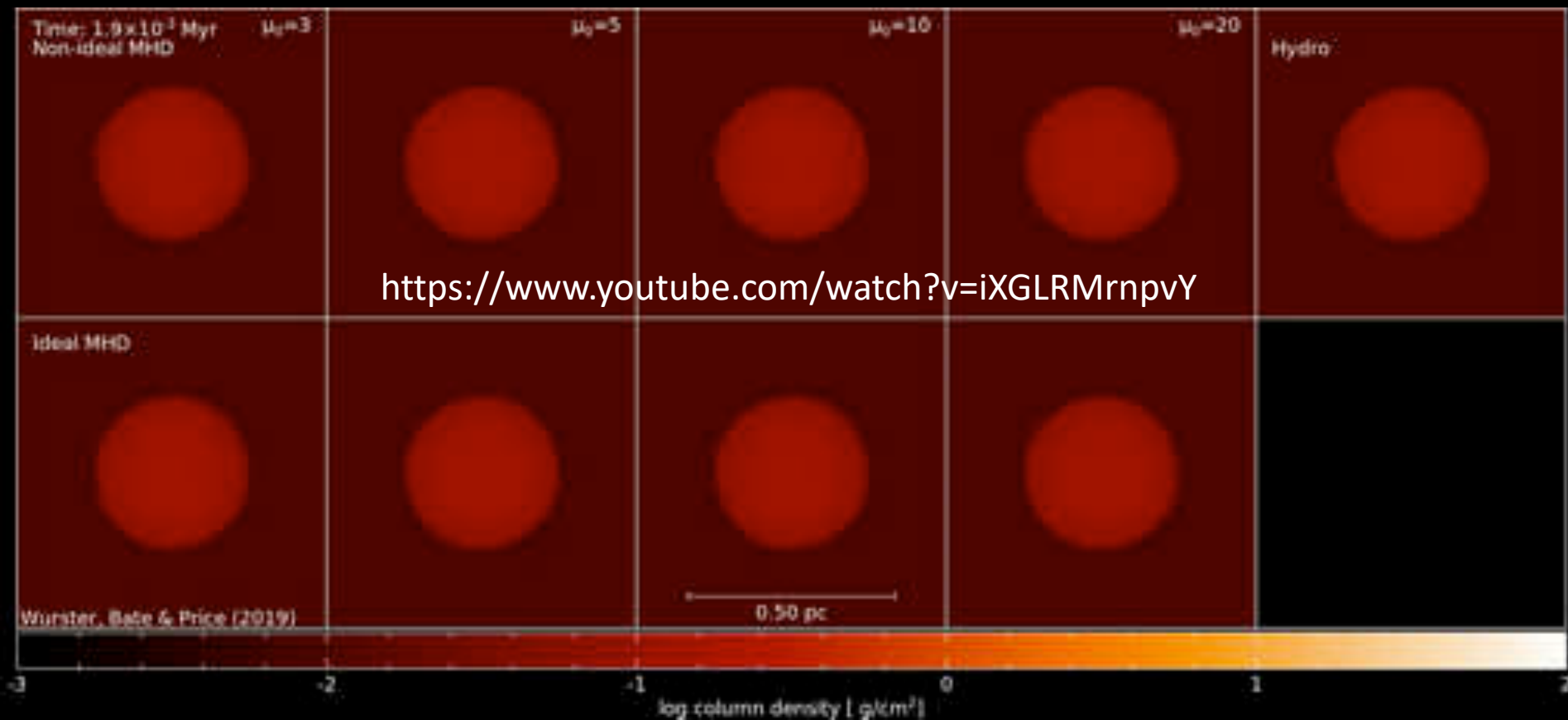


Taurus Molecular Cloud
(Credit: ESO/APEX (MPIfR/ESO/OSO)/A. Hacar et al./Digitized Sky Survey 2.
Acknowledgment: Davide De Martin)

Taurus Molecular Cloud: H₂ column density map with positions of young stars (Goldsmith et. al., 2008)



Cluster Formation: Effect of Magnetic Fields





Cluster Formation: Effect of non-ideal MHD

Time: 1.9×10^3 Myr

Non-ideal MHD, $\mu_0=5$

Ideal MHD, $\mu_0=5$

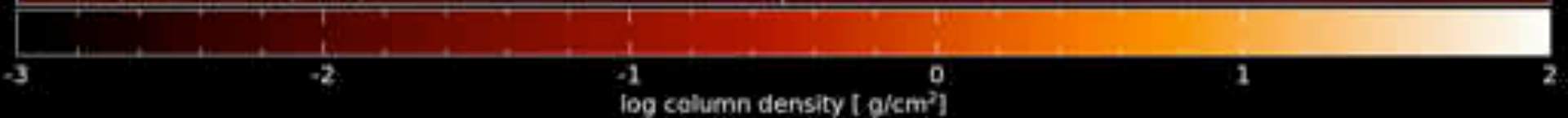
<https://www.youtube.com/watch?v=dHiUm7deOBM&t=8s>



0.50 pc

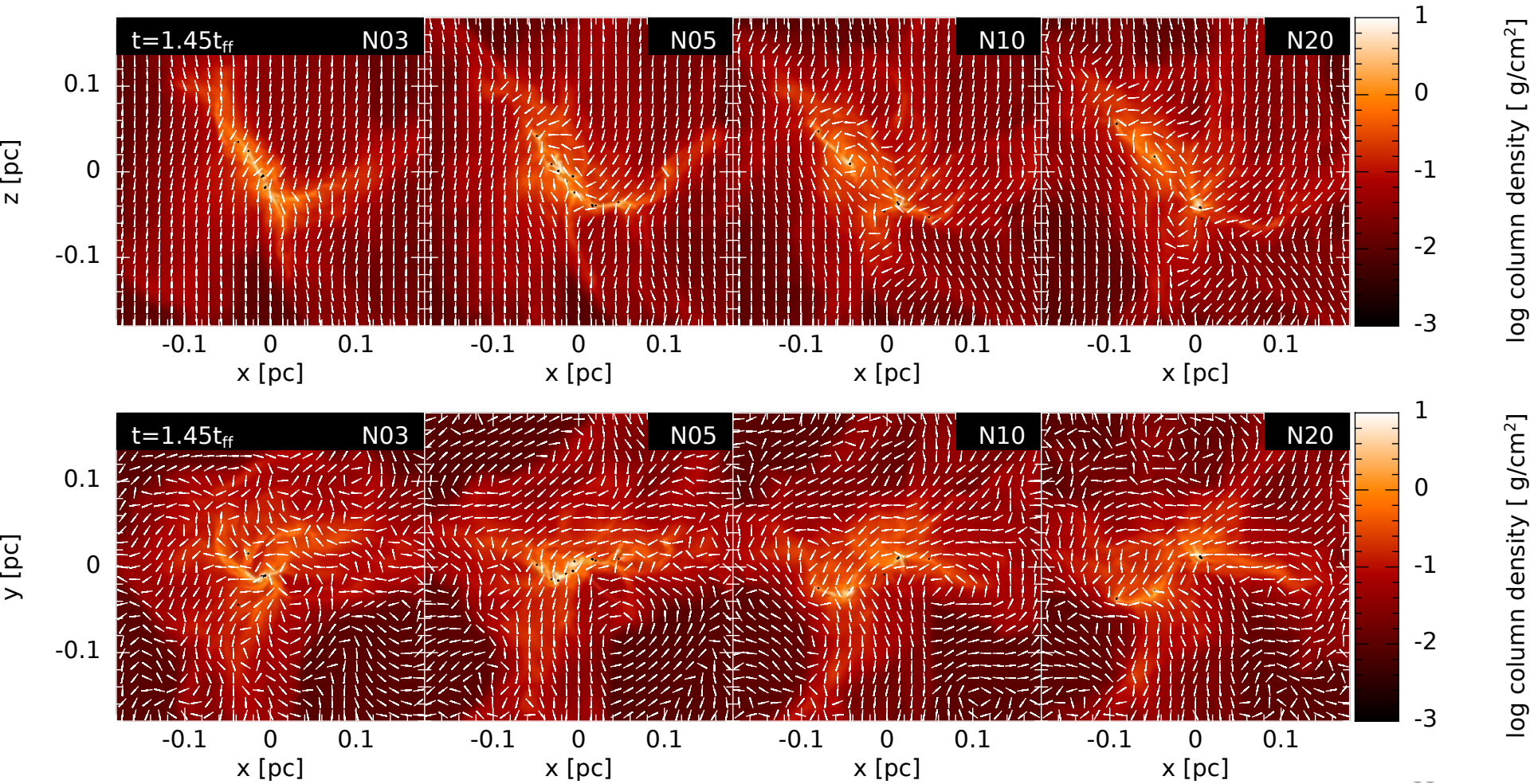
0.50 pc

Wurster, Bate & Price (2019)



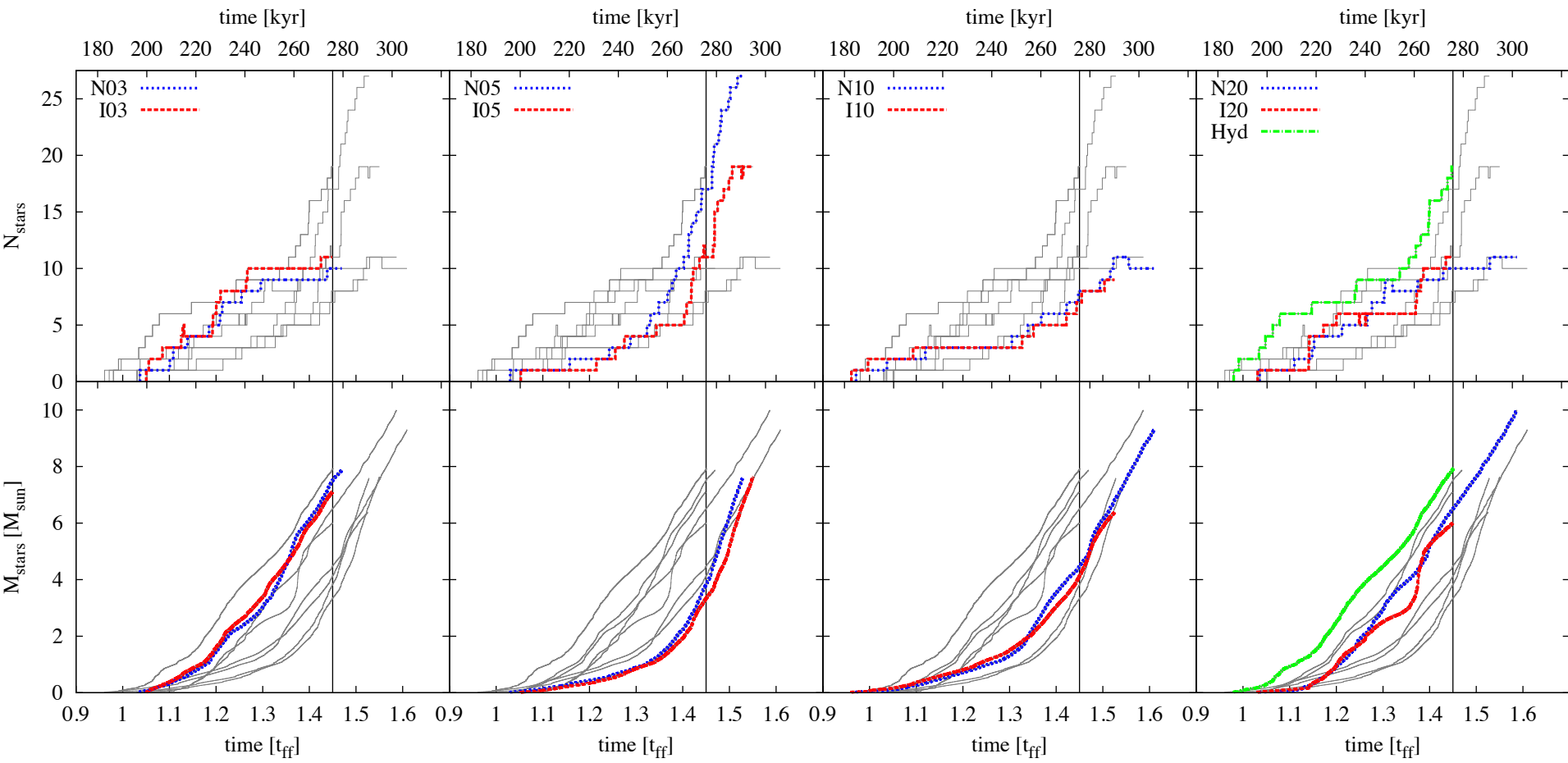
Cluster Formation: Magnetic field lines

- Magnetic fields cross dense filaments approximately perpendicularly
- Magnetic fields are approximately parallel to low-density filaments



Cluster Formation: Stellar Mass

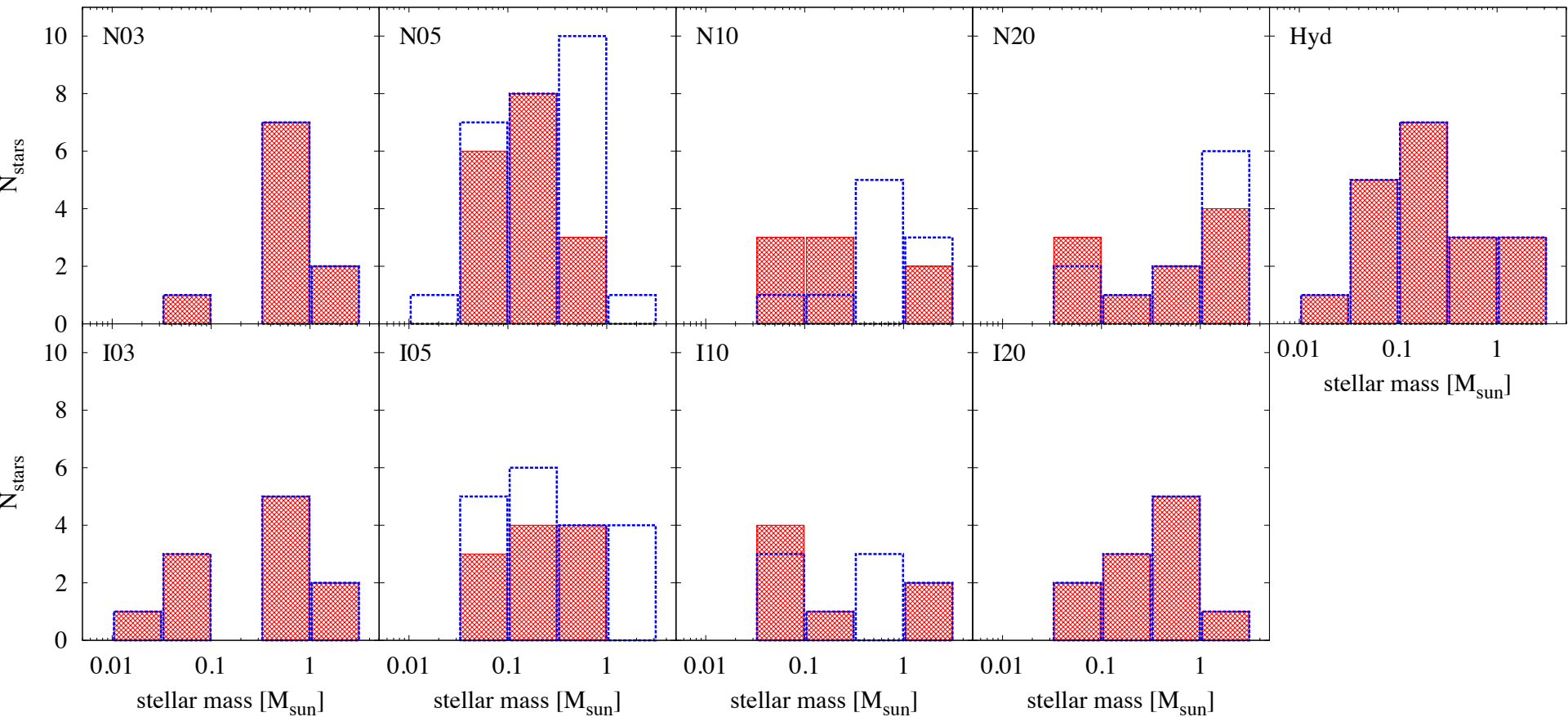
- No trend when stars form
- Excluding N03 & I03, there is more mass in stars with weaker initial magnetic field strengths





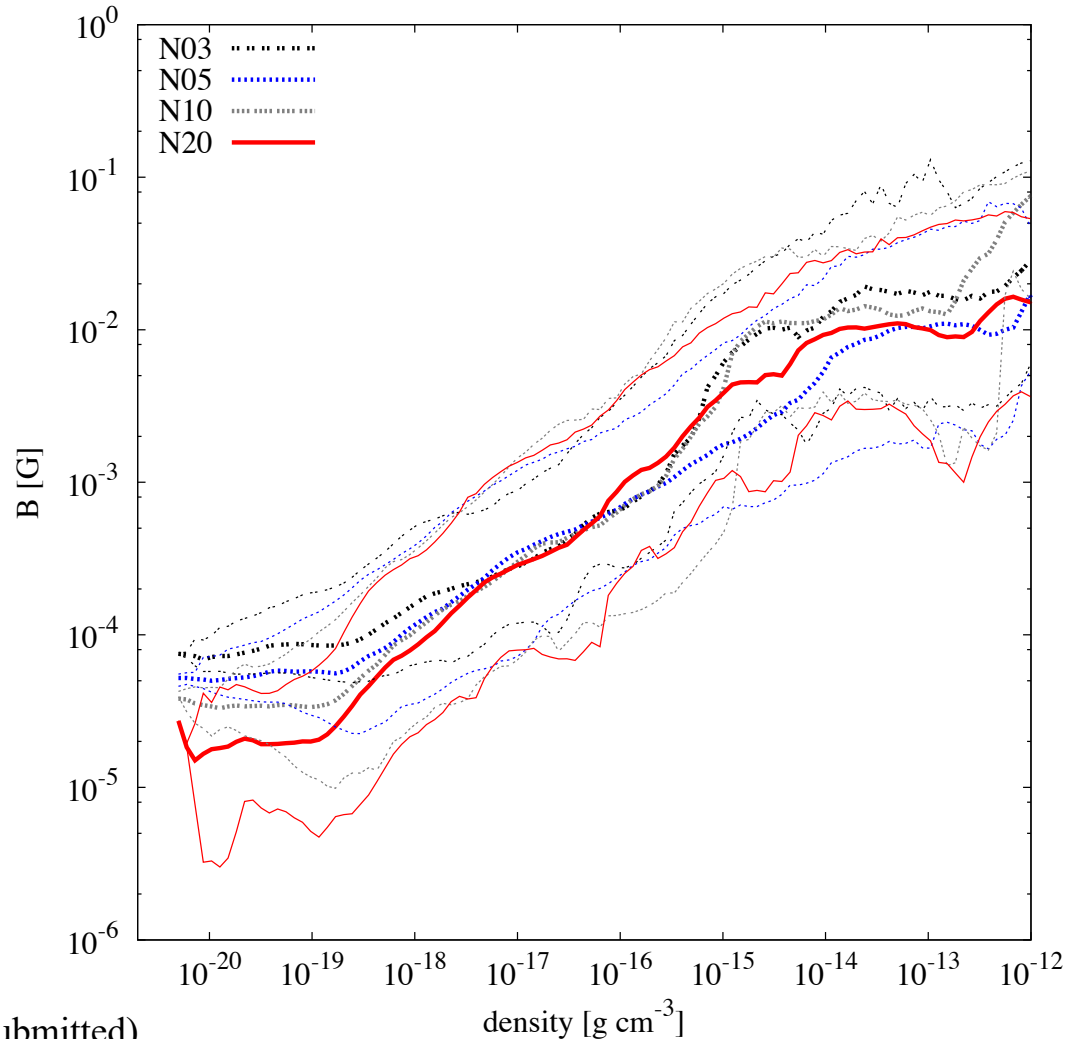
Cluster Formation: Stellar Mass

- No trend in IMF (although this is low-number statistics)
- red is at common time of $1.45t_{\text{ff}}$; blue is at end of the respective simulations



Cluster Formation: Star forming regions

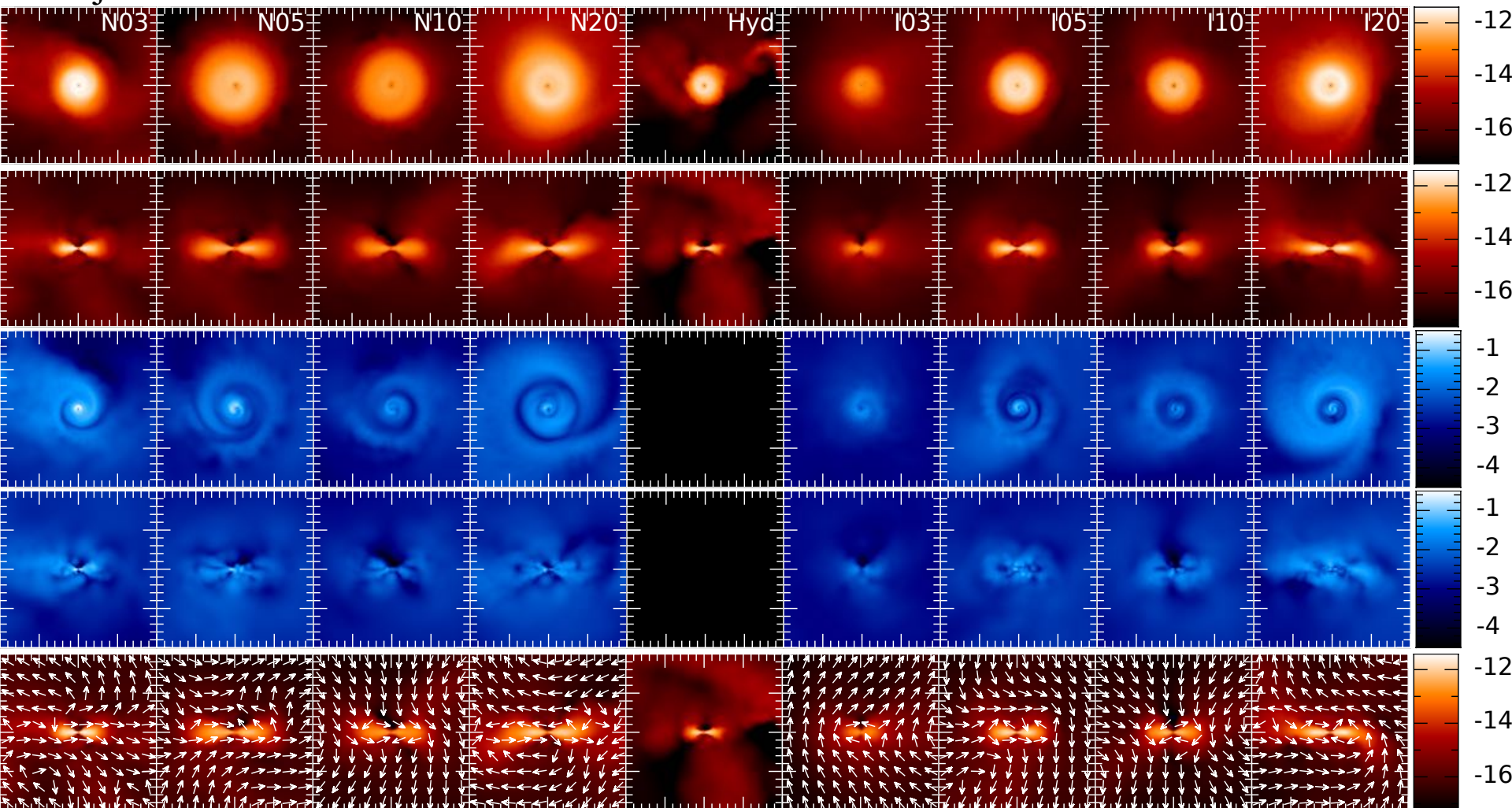
➤ Star forming regions have a wide range of initial magnetic field strengths, that are approximately independent of the global environment





Cluster Formation: Protostellar discs

- Large protostellar discs form in *all* our models
- Major tics are 103au



Conclusions

- Isolated, low-mass star formation:
 - Large discs only form in the hydrodynamic and $\zeta_{\text{cr}} = 10^{-17} \text{ s}^{-1}$ with $-B_z$ models.
 - *this resolved the magnetic braking catastrophe*
 - When using non-ideal MHD, the maximum magnetic field strength is not coincident with the central magnetic field strength
 - The magnetic fields in stars must be generated by a dynamo action, rather than being fossil in origin
- Star cluster formation:
 - No trends amongst most of our parameters
 - Discs form in all of our models, *suggesting that the magnetic braking catastrophe is a result of poor initial conditions*